



UNIVERSITÉ
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OBSERVATOIRE
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Stochastic acceleration in blazars

Andrea Tramacere

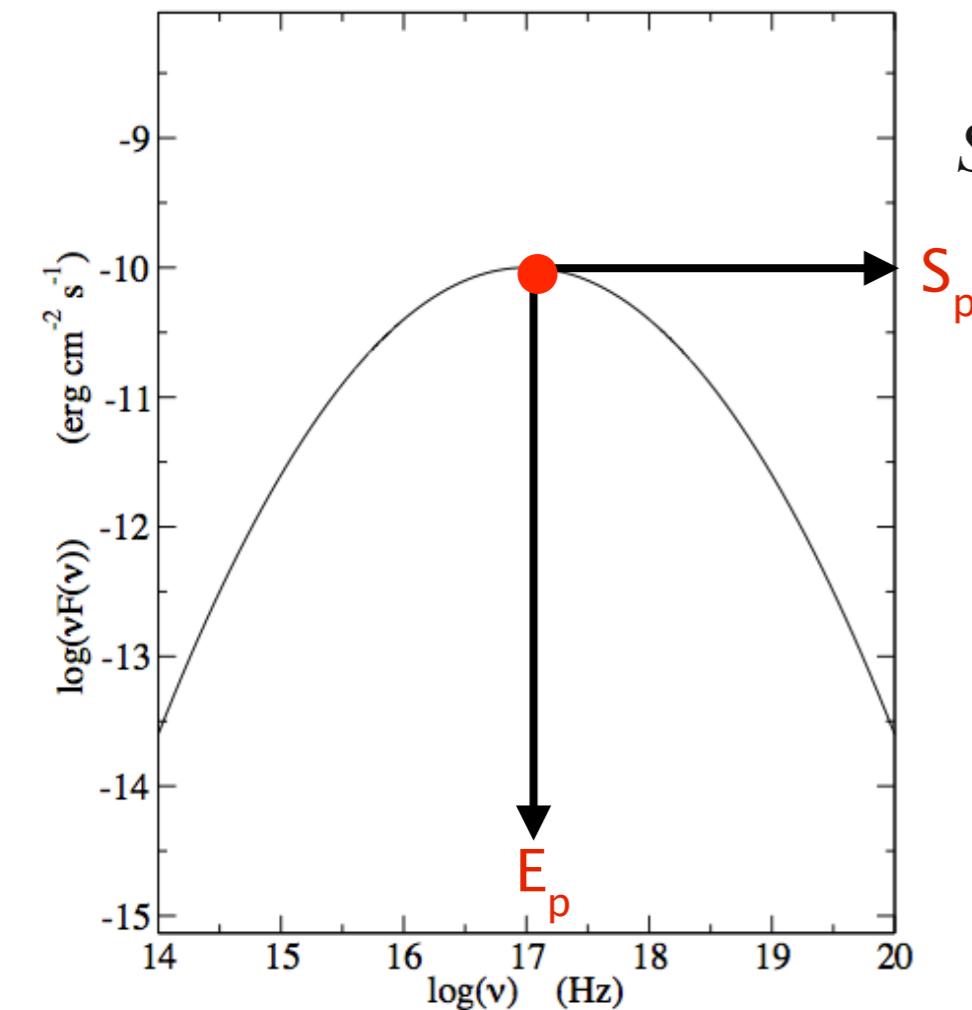
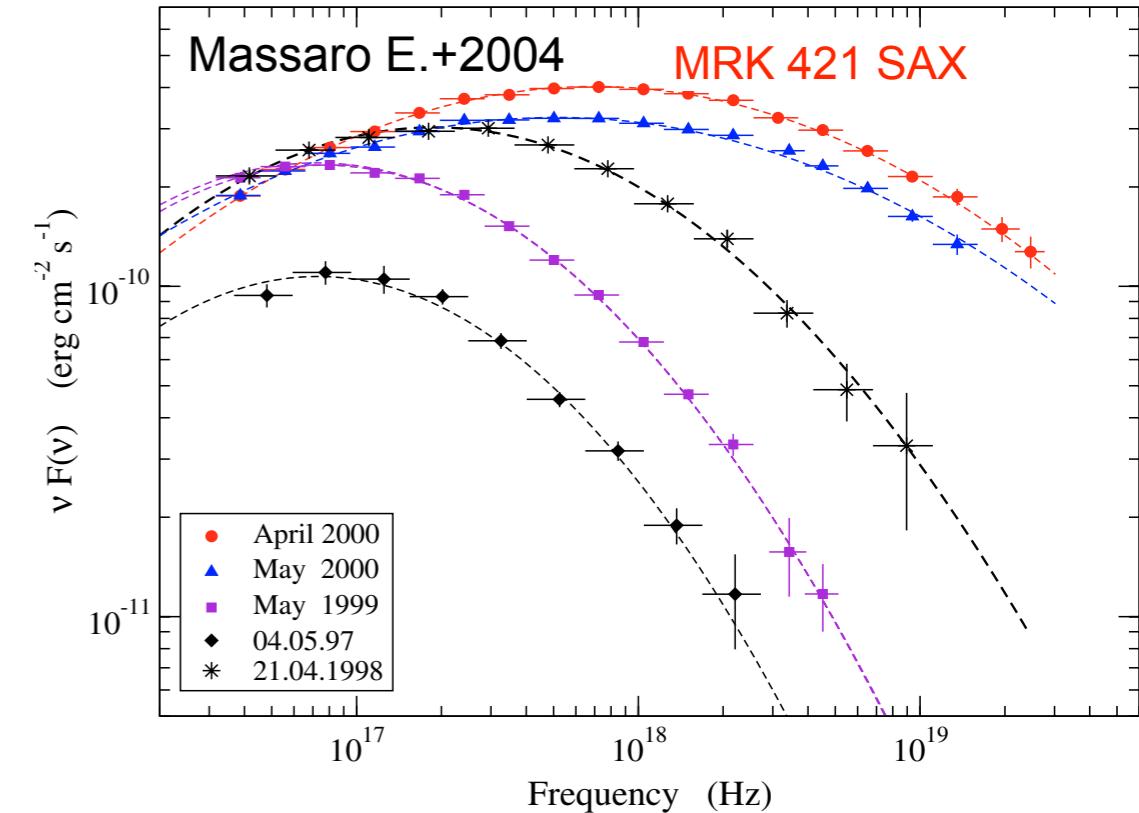
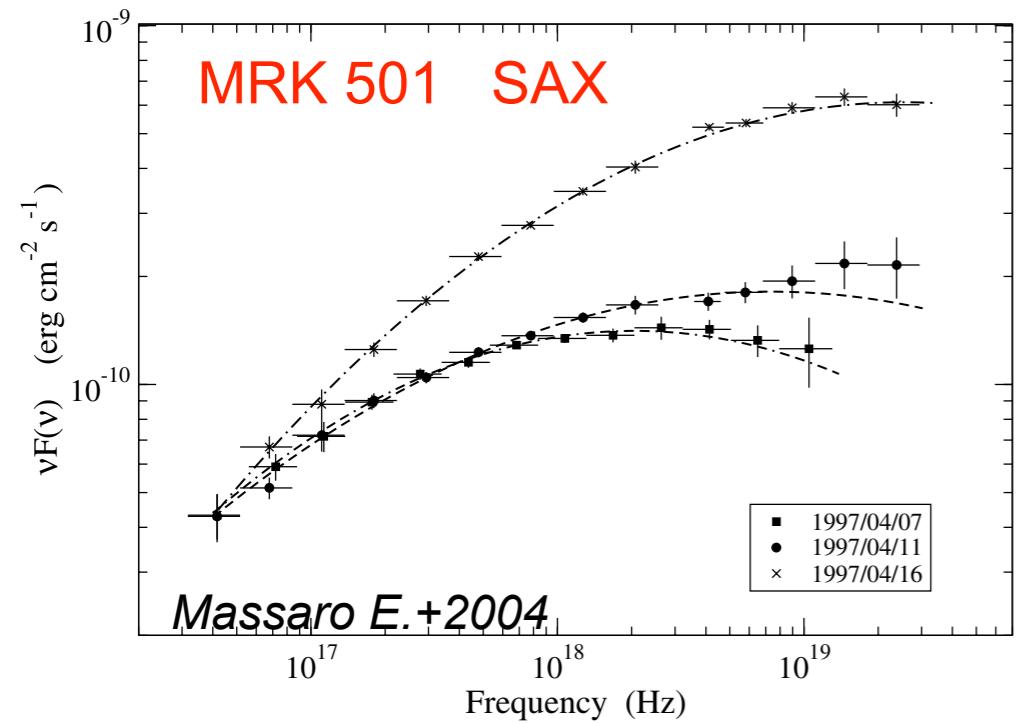
Geneva

12-February 2019

Outline

- Phenomenological signatures
- setup of Theory/Numerical framework for stochastic acceleration
- Self-consistent reproduction of Long Term Trends
- numerical modeling, numerical fit (no eyeball fit) no analytical approximations

SPECTRAL DISTRIBUTION OF HBLs

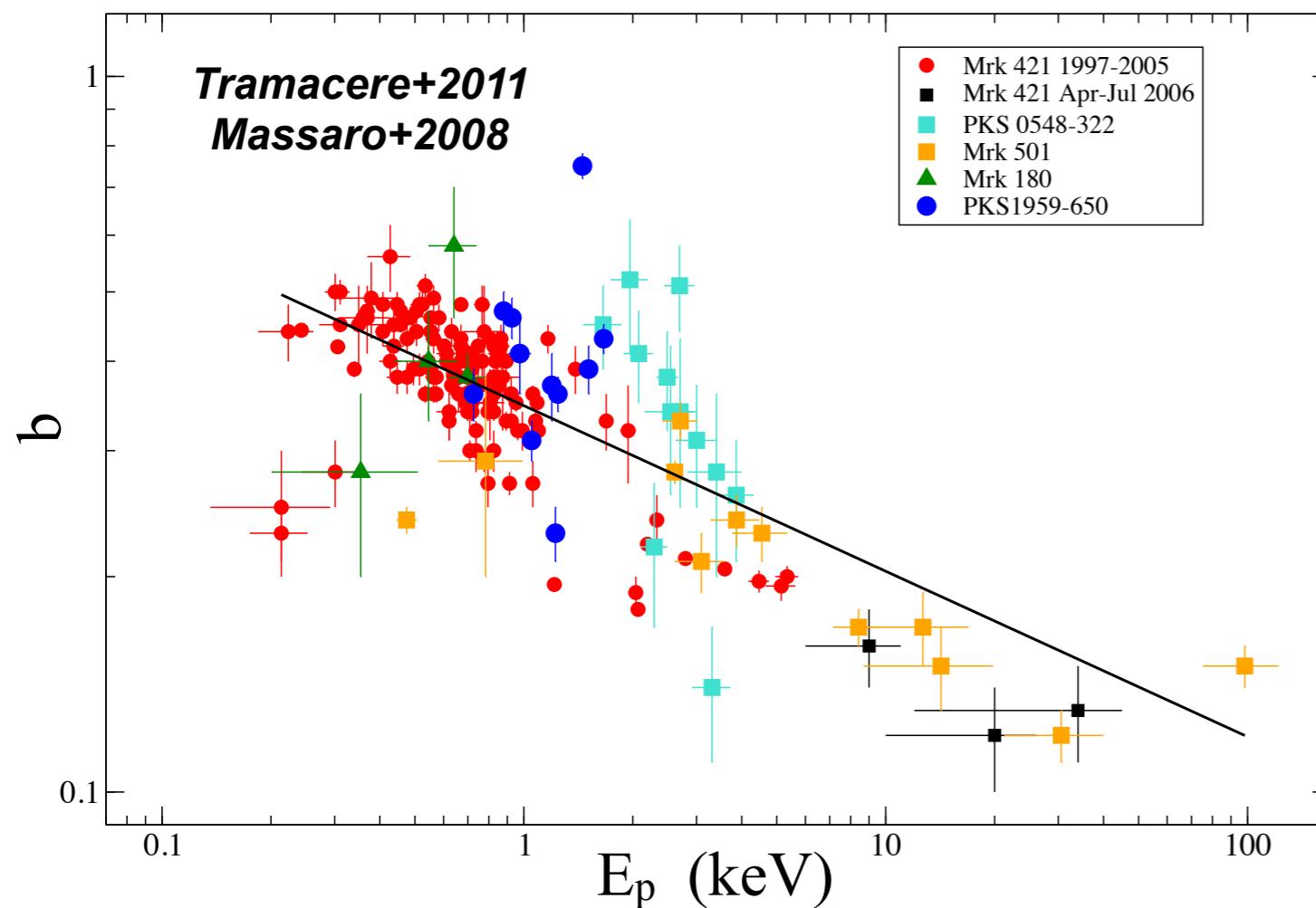
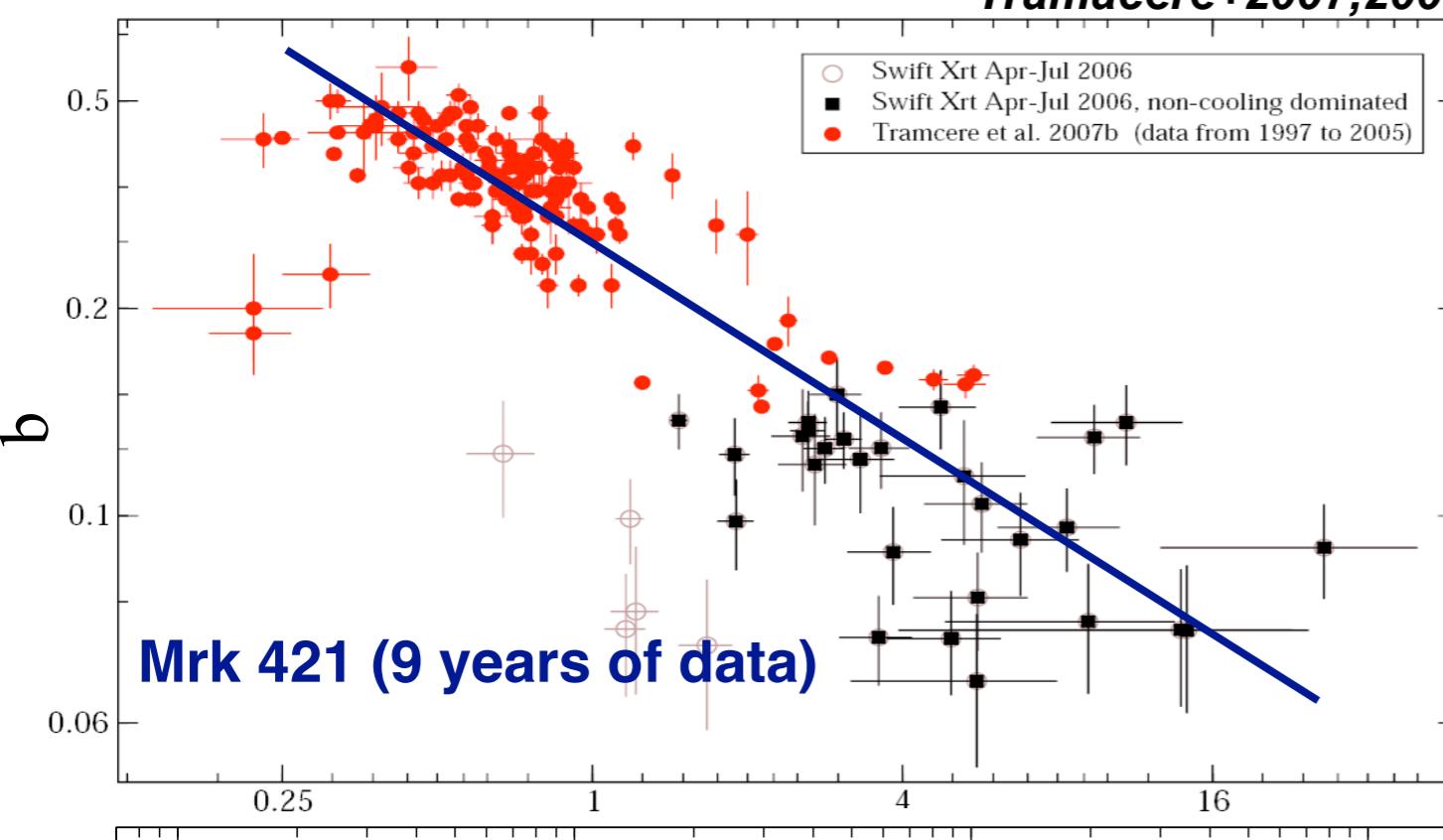


$$S(E) = S_p 10^{-b} (\log(E/E_p))^2$$

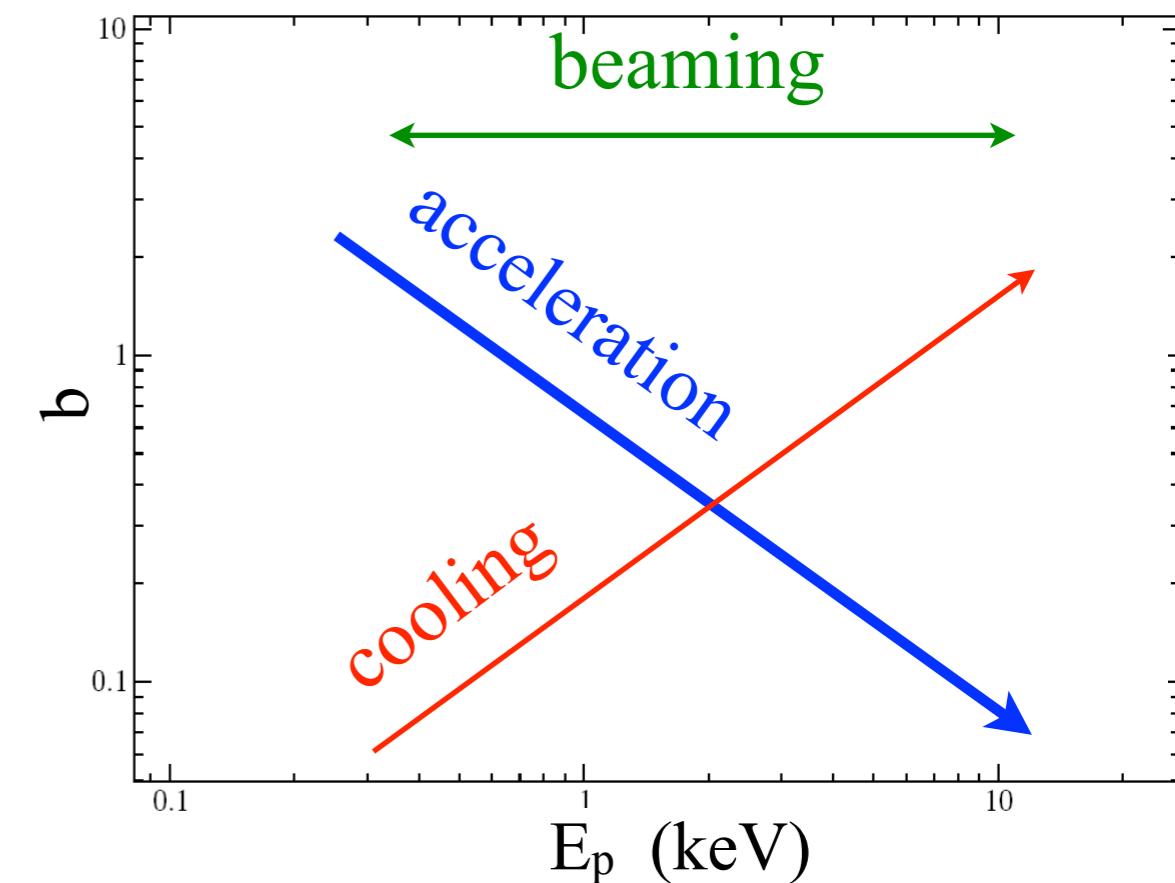
- b : curvature at peak
- E_p : peak energy
- S_p : SED height @ E_p

acceleration signature in the Es-vs-b trend

Tramacere+2007, 2009



Ep-vs-b, different scenarios



11 years of data:

PKS 0548-322, 1H1426+418,

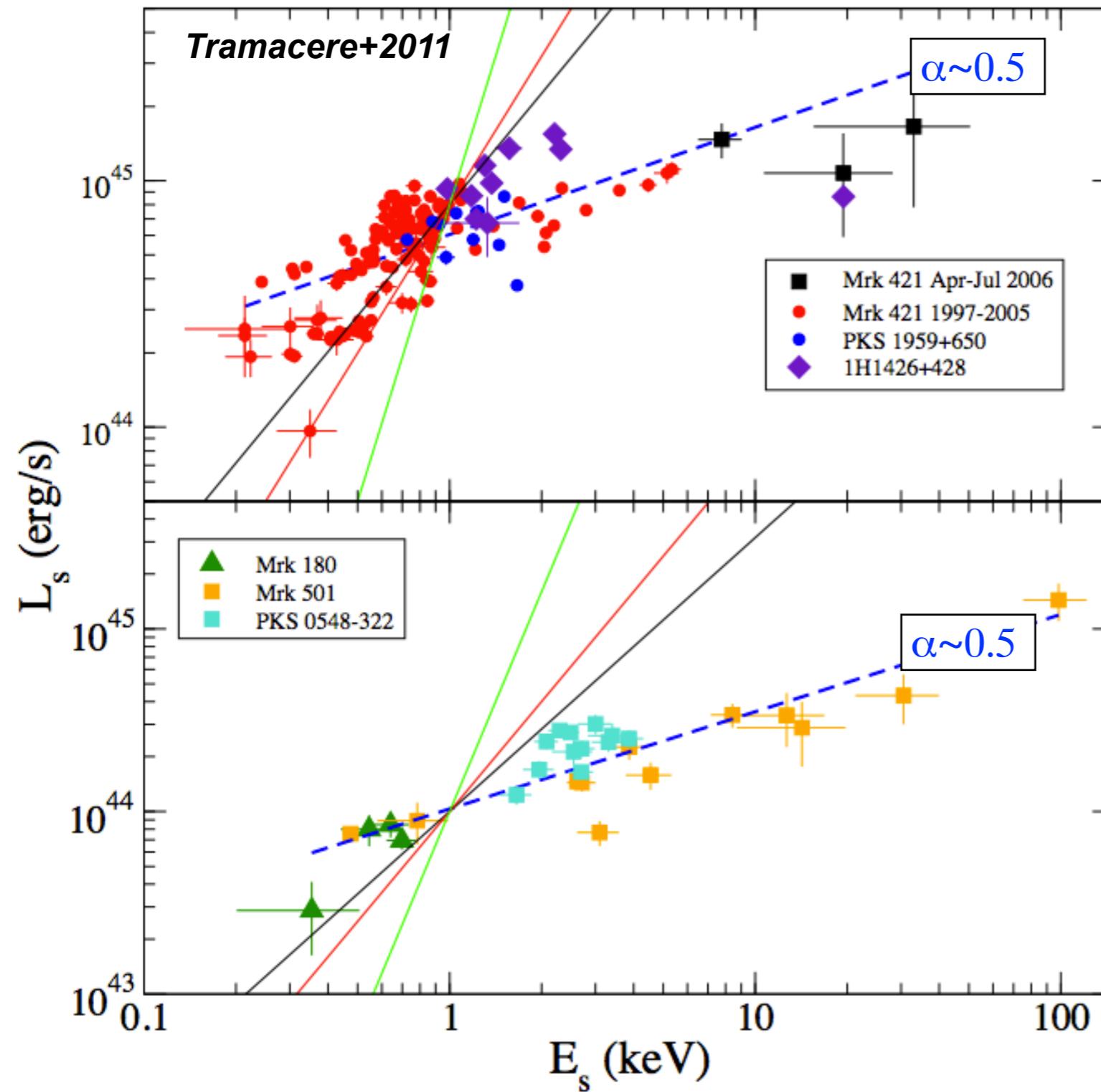
Mrk 501 , 1ES1959+650,

PKS2155-34

**Long term (overall 13 years of data)
Ep-vs-b trends hint for an acceleration
dominated scenario**

acceleration signature in the Es-vs-Ls trend

long-trend main drivers



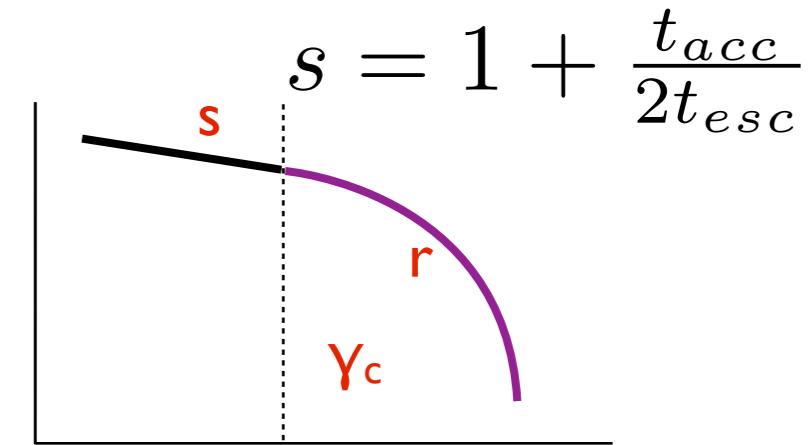
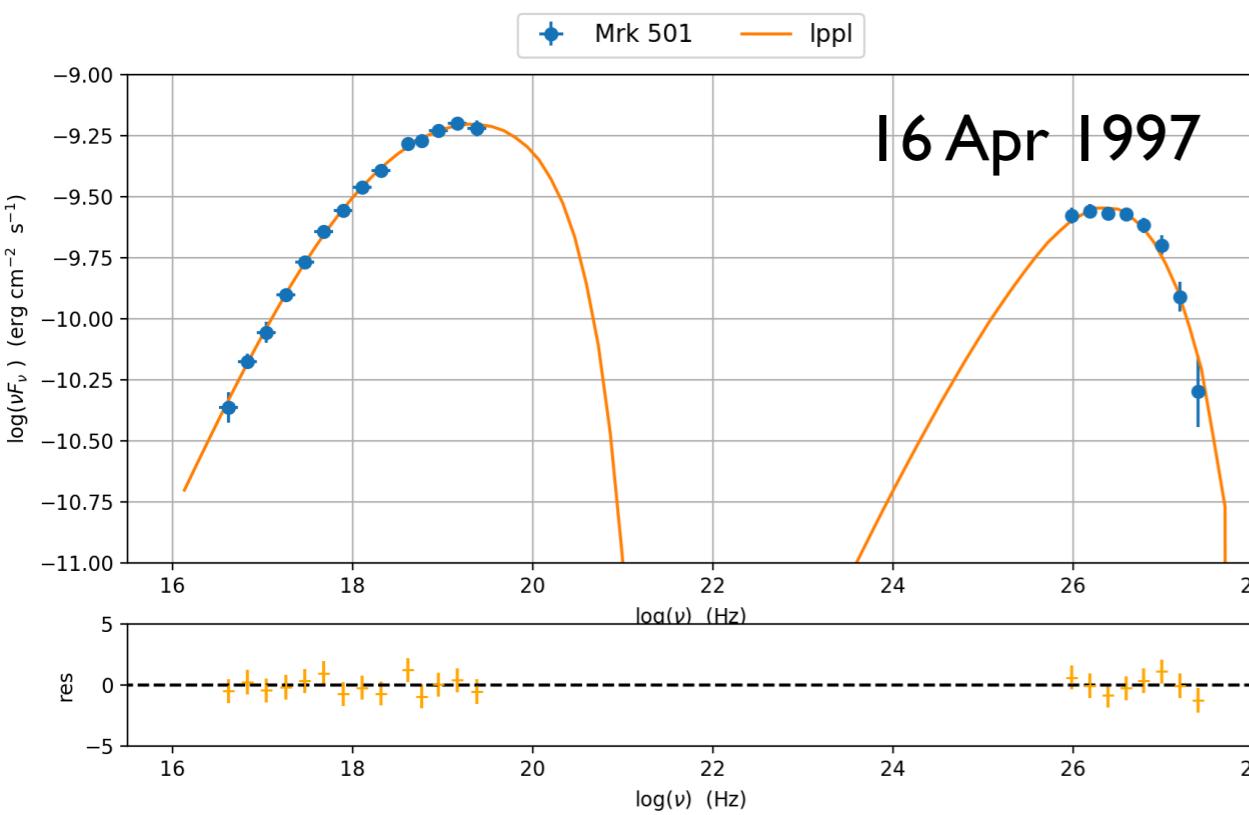
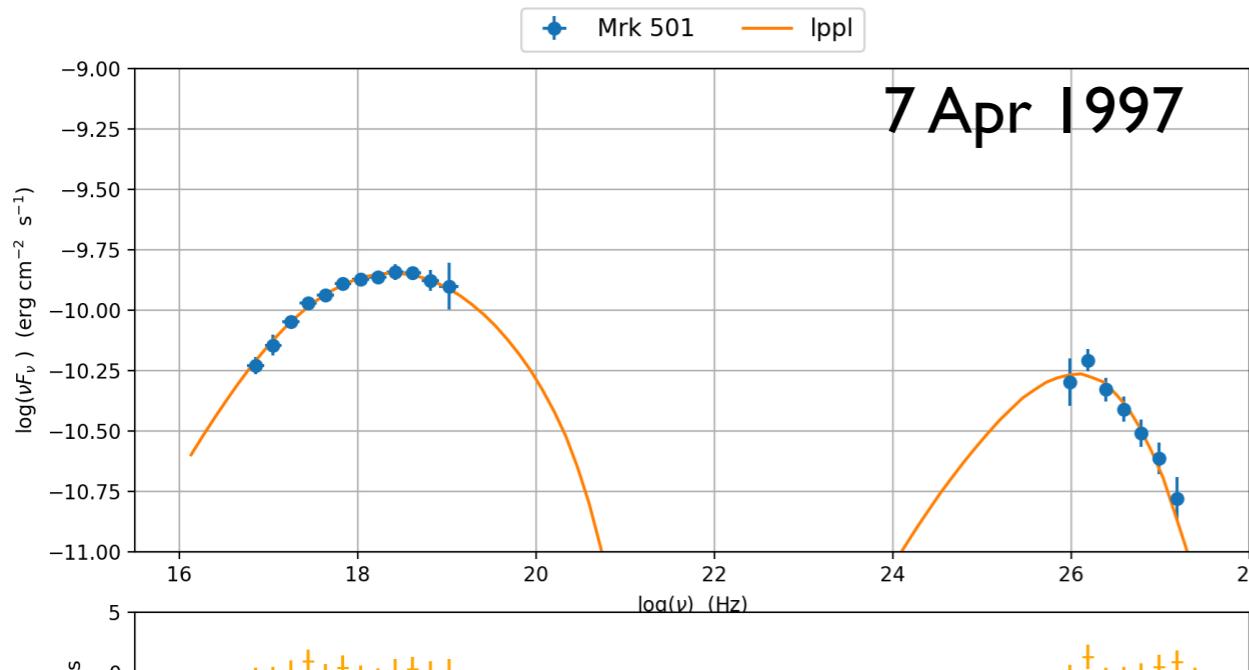
• $\gamma_{3p} \uparrow$ and $n(\gamma_{3p}) \downarrow \Rightarrow \alpha < 1.5$
acceleration+energy conservation

• $B \rightarrow \alpha = 2.0$, incompatible as long-trend main driver
• $\delta \rightarrow \alpha = 4$

Mrk 501 1997 Flare

Hard spectra $s << 2.00$

Massaro & Tramacere +2006



best fit pars

best-fit parameters:

Name	best-fit value	best-fit err +
B	+1.072178e-01	+5.436622e-03
N	+4.585348e+00	+4.756569e-01
R	Frozen	Frozen
beam_obj	+2.450884e+01	+7.642113e-01
gamma0_log_parab	+6.609649e+04	+7.427709e+03
gmax	+1.860044e+14	+5.881595e+14
gmin	+1.404527e+03	+2.198648e+02
r	+7.513452e-01	+5.059815e-02
s	+1.638026e+00	+3.170384e-02
z_cosm	Frozen	Frozen

best-fit parameters:

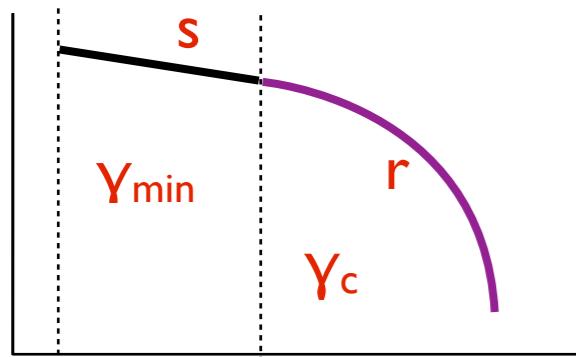
Name	best-fit value	best-fit err +
B	+3.065207e-01	+1.159567e-02
N	+1.079944e+02	+7.375385e+00
R	Frozen	Frozen
beam_obj	+2.722013e+01	+5.889626e-01
gamma0_log_parab	+6.493888e+04	+5.410315e+03
gmax	+1.902146e+06	+2.216666e+02
gmin	+3.003970e+02	+5.686711e+01
r	+6.778727e-01	+3.526656e-02
s	+1.321307e+00	+1.844825e-02
z_cosm	Frozen	Frozen

Fermi I+Fermi II

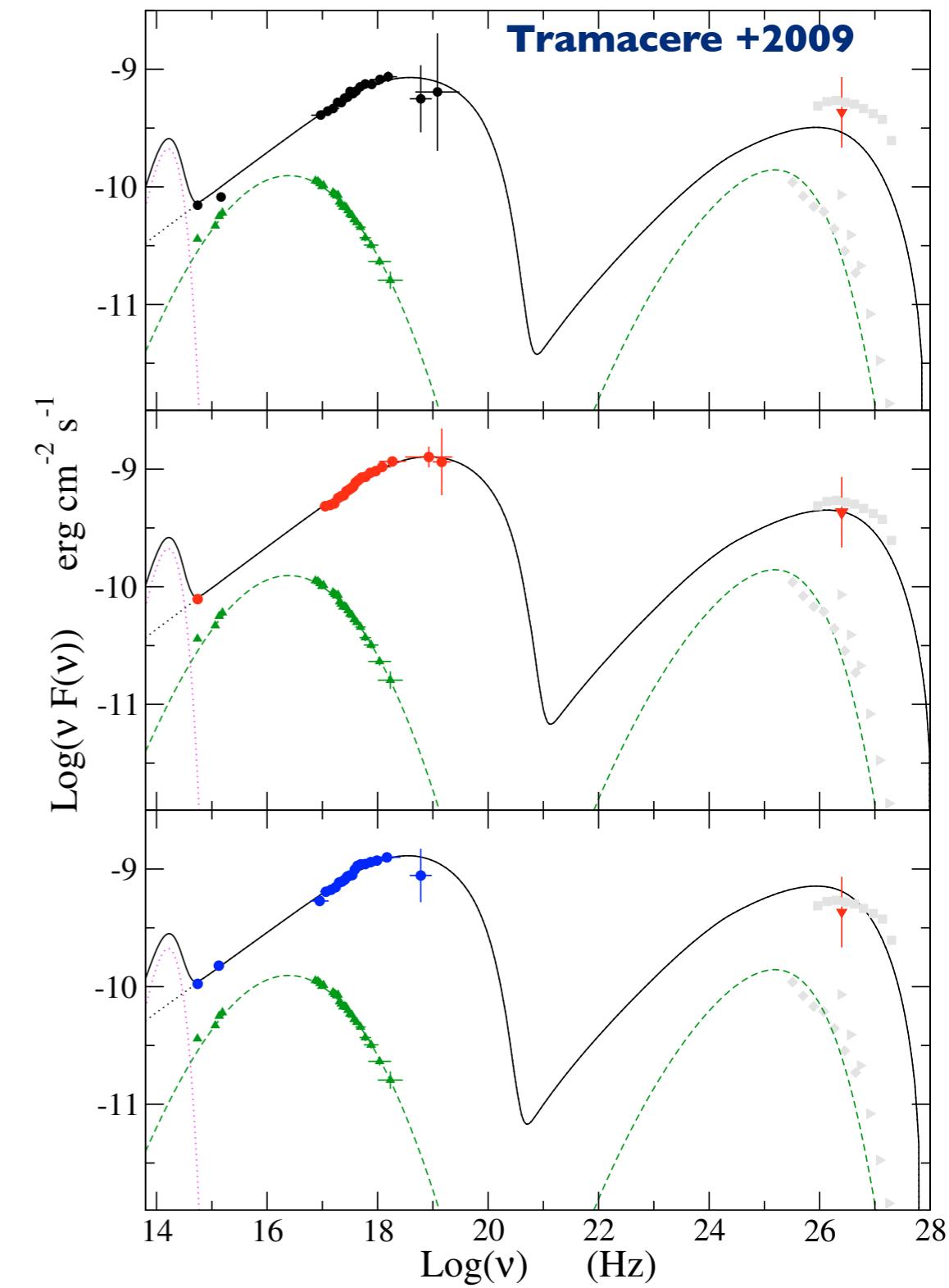
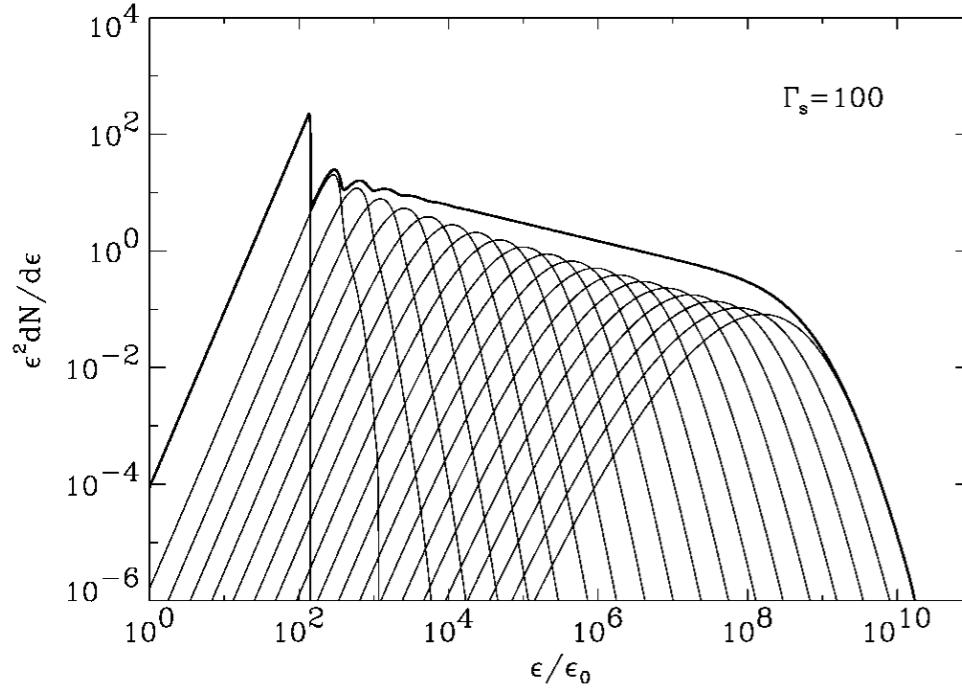
Mrk 421 2006

LP+PL spectra

Synch index~[1.6-1.7]=> $s \sim [2.2-2.4]$

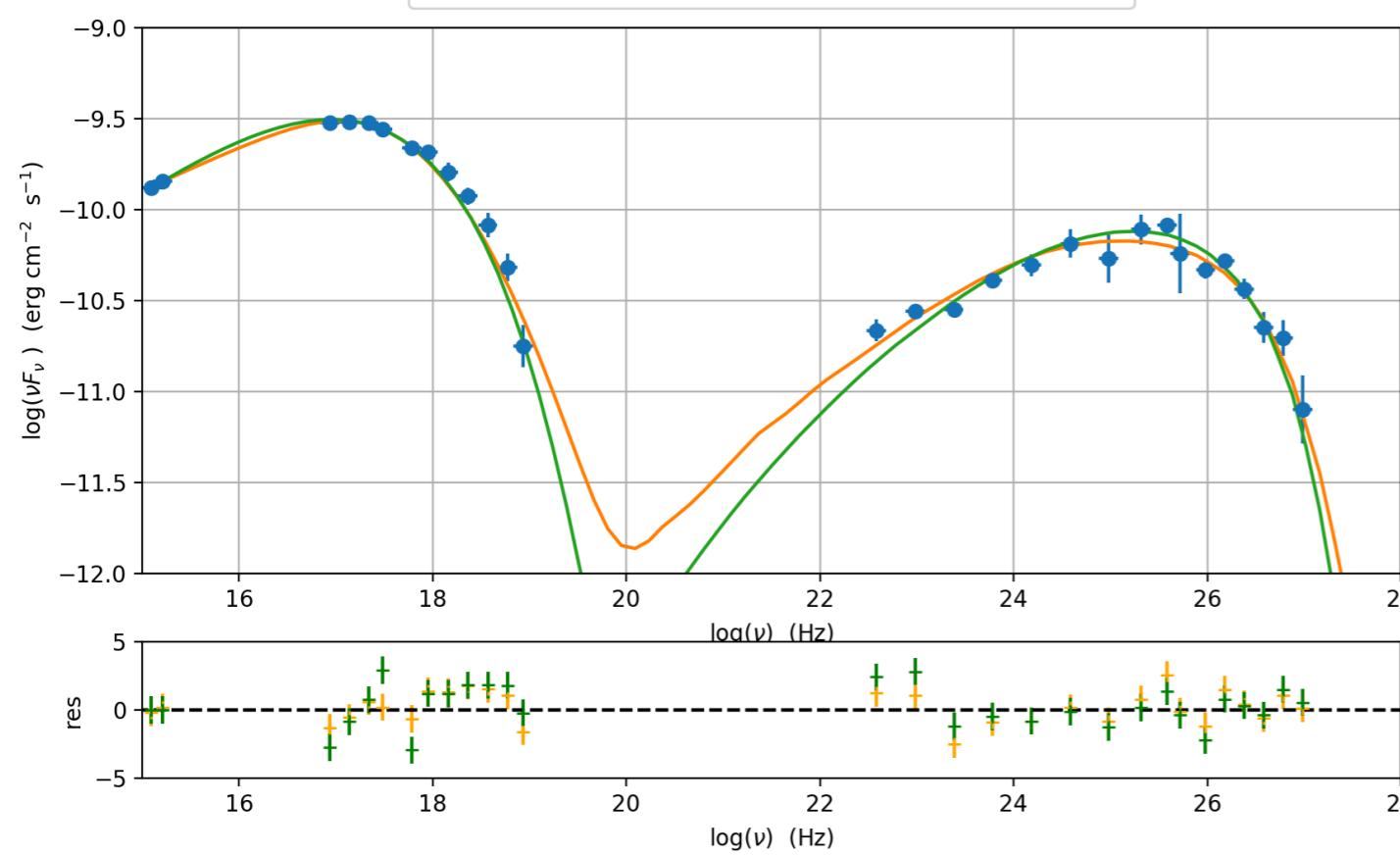


Lemoine,Pelletier 2003



Mrk 421 2009 data

data from Abdo et al 2011
Fermi-LAT+Magic coll.



```
dof=21
chisq=39.696427, chisq/red=1.890306 null hypothesis
```

```
best fit pars
```

```
-----
```

```
best-fit parameters:
```

Name	best-fit value	best-fit err +
B	+2.096016e-02	+5.744998e-05
N	+1.152143e-01	+1.545857e-03
R	Frozen	Frozen
beam_obj	+2.619674e+01	+8.501912e-02
gamma0_log_parab	+1.884210e+05	+1.891713e+03
gmax	+3.492780e+08	+6.130842e+08
gmin	+1.929302e+03	+2.109472e+01
r	+1.681768e+00	+3.032664e-02
s	+2.509224e+00	+2.902511e-03
z_cosm	Frozen	Frozen

```
*****
```

Ippl/plc p-value = 6.8E-6

The log-parabola origin: physical insight

The origin of the log-parabolic shape: statistical derivation

fluctuation

$$\varepsilon = \bar{\varepsilon} + \chi$$

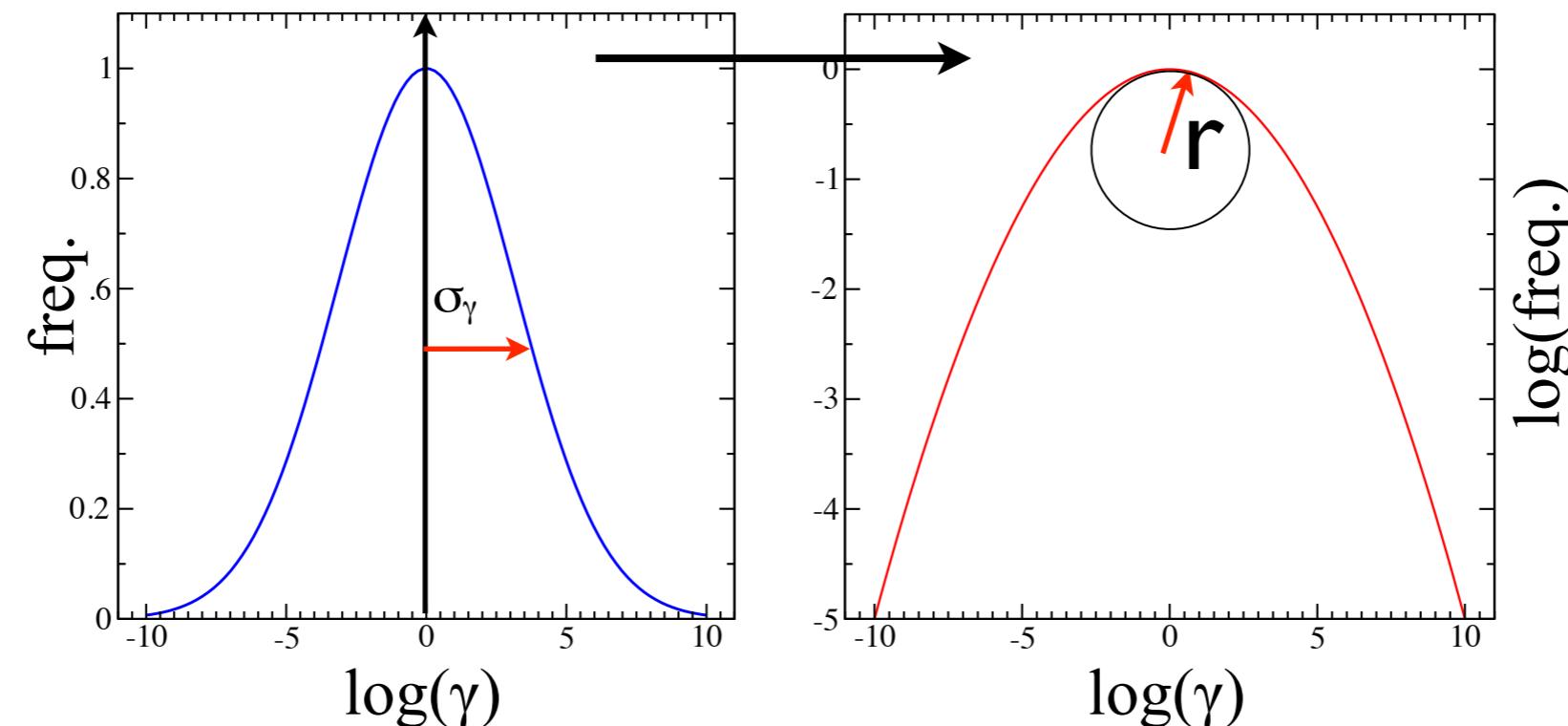
ε_i is a R.V.

systematic

log-normal distribution

$$\gamma_{n_s} = \gamma_0 \prod_{i=1}^{n_s} \varepsilon_i$$

C.L. Theorem
multipl. case



$$\log(n(\gamma)) \propto \frac{(\log \gamma - \mu)^2}{2\sigma_\gamma^2} \propto r [\log(\gamma) - \mu]^2$$

$$\frac{\partial n(\gamma, t)}{\partial t} = \frac{\partial}{\partial \gamma} \left\{ -[S(\gamma, t) + D_A(\gamma, t)]n(\gamma, t) + D_p(\gamma, t) \frac{\partial n(\gamma, t)}{\partial \gamma} \right\} - \frac{n(\gamma, t)}{T_{esc}(\gamma)} + Q(\gamma, t)$$

analytical solution for:

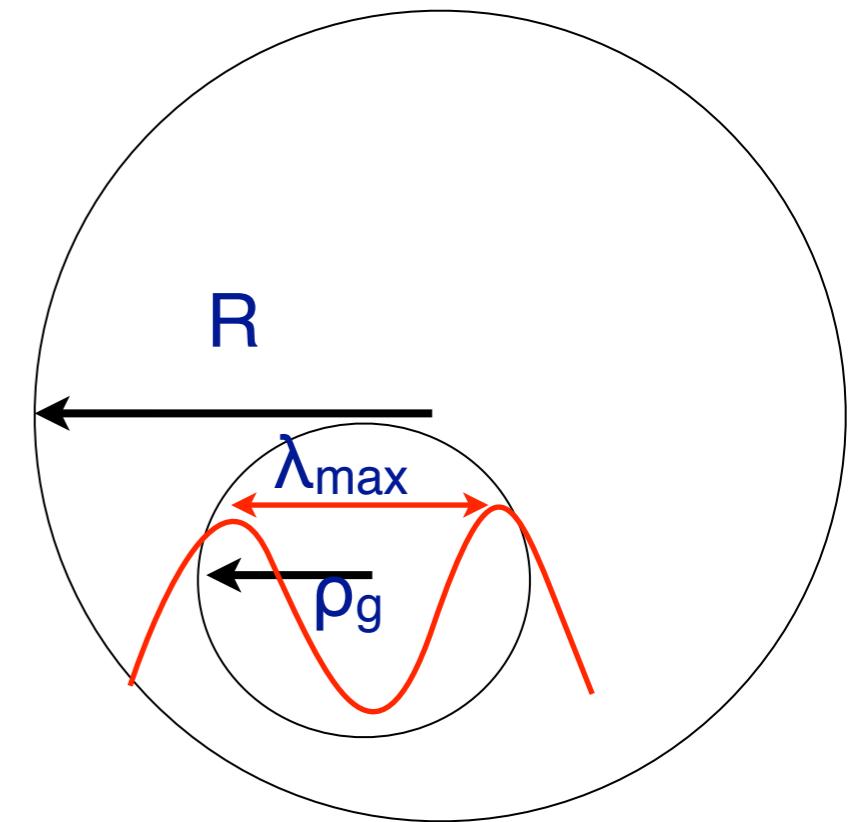
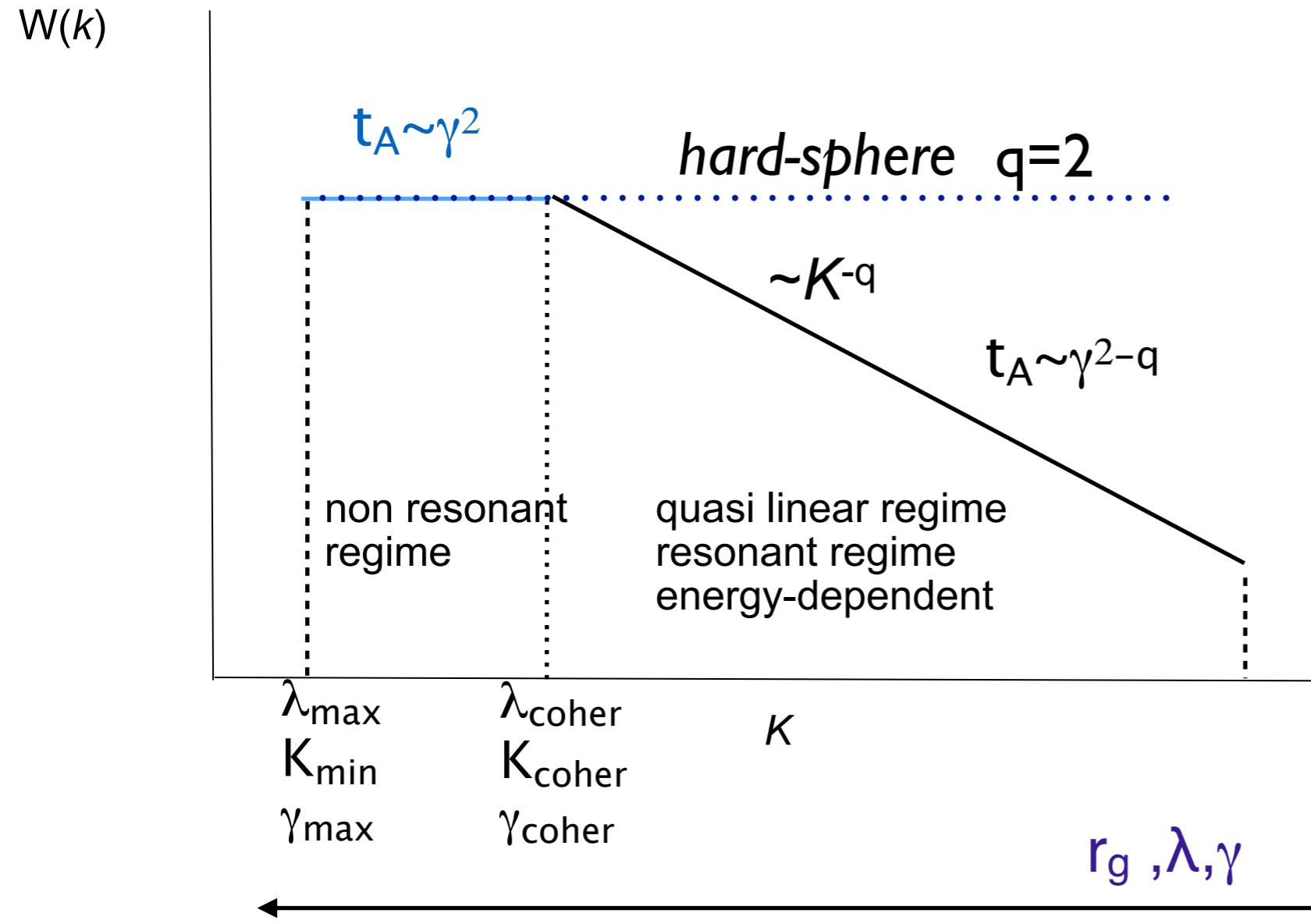
$$D_p \sim \gamma^q, \quad q=2$$

“hard-sphere” case no cooling

Melrose 1968,

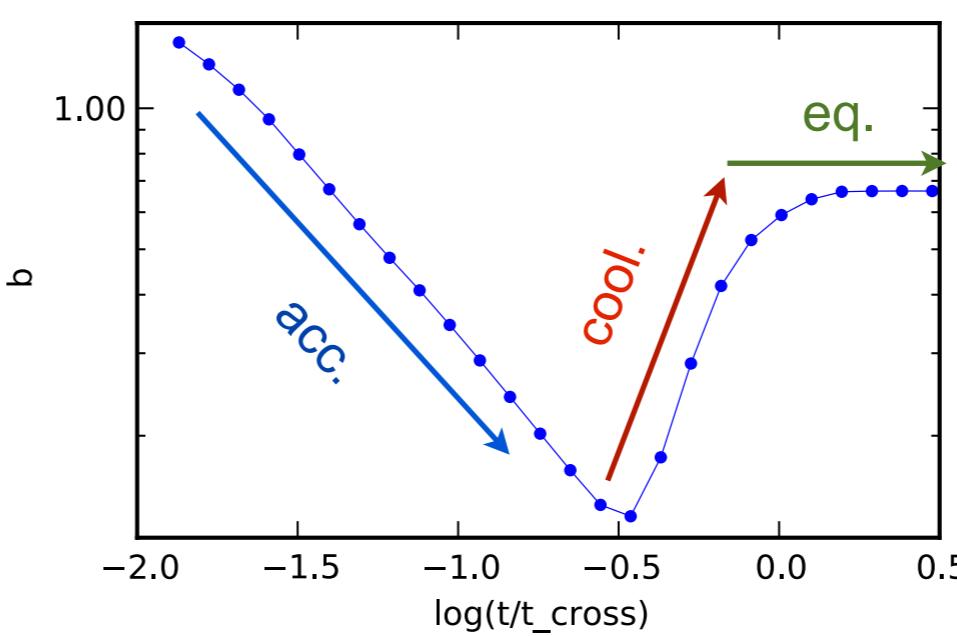
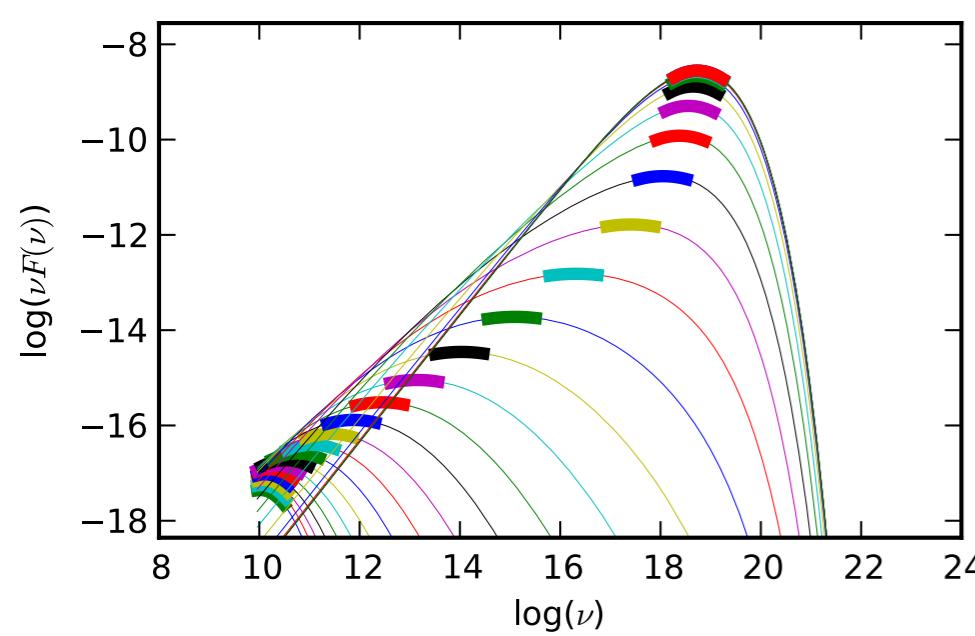
$$n(\gamma, t) = \frac{N_0}{\gamma \sqrt{4\pi D_{p0} t}} \exp \left\{ - \frac{[\ln(\gamma/\gamma_0) - (A_{p0} - D_{p0})t]^2}{4D_{p0}t} \right\}$$

set-up of the accelerator

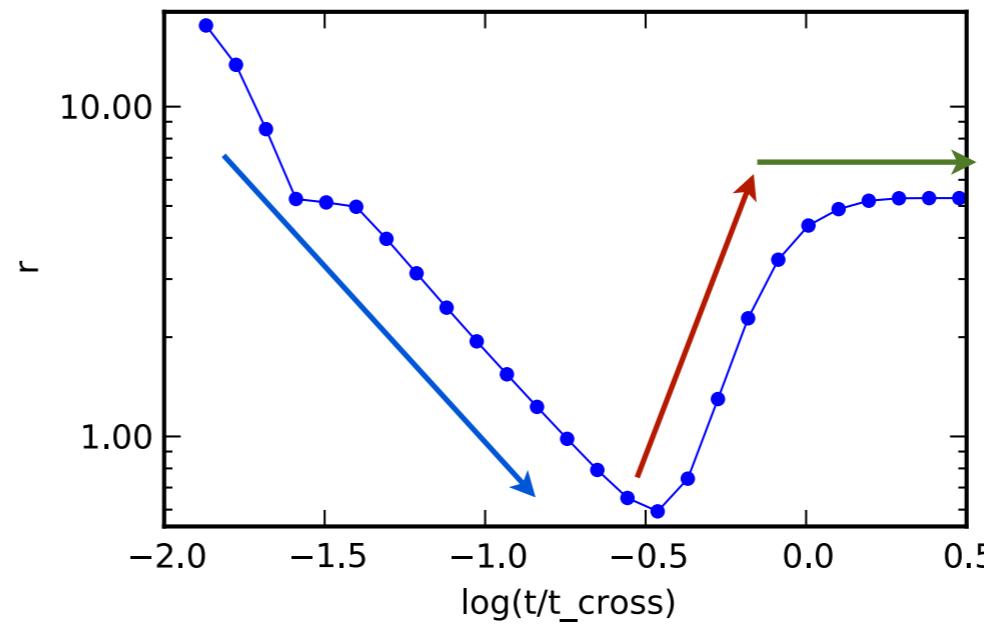
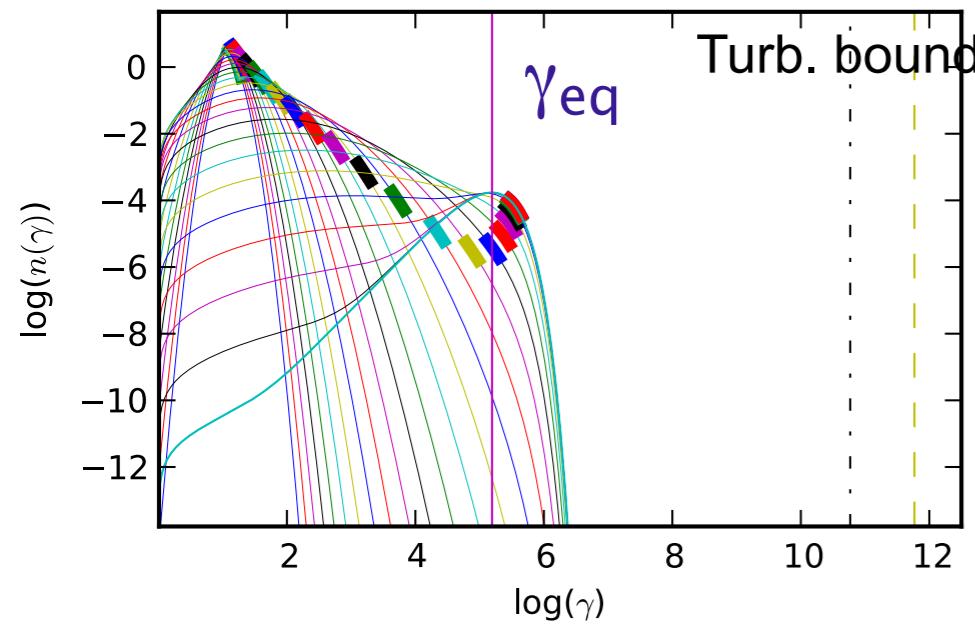


spectral trends

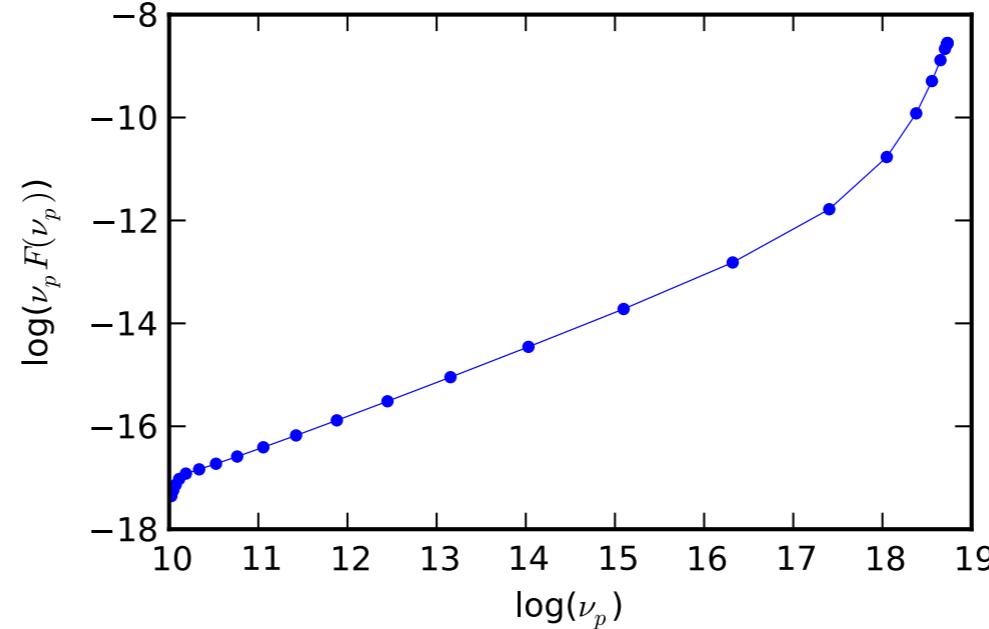
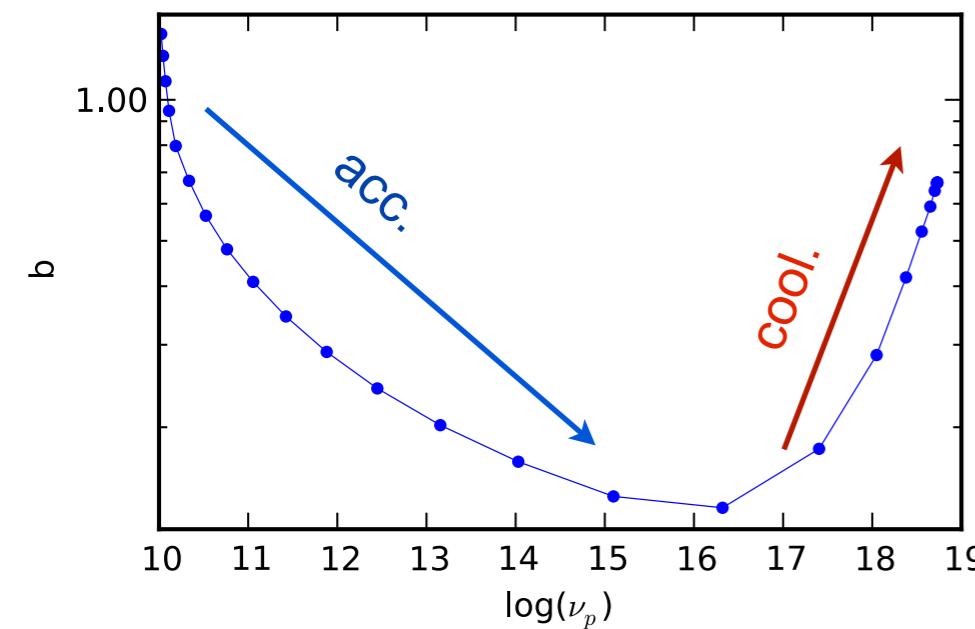
single flare



Synchrotron



electrons

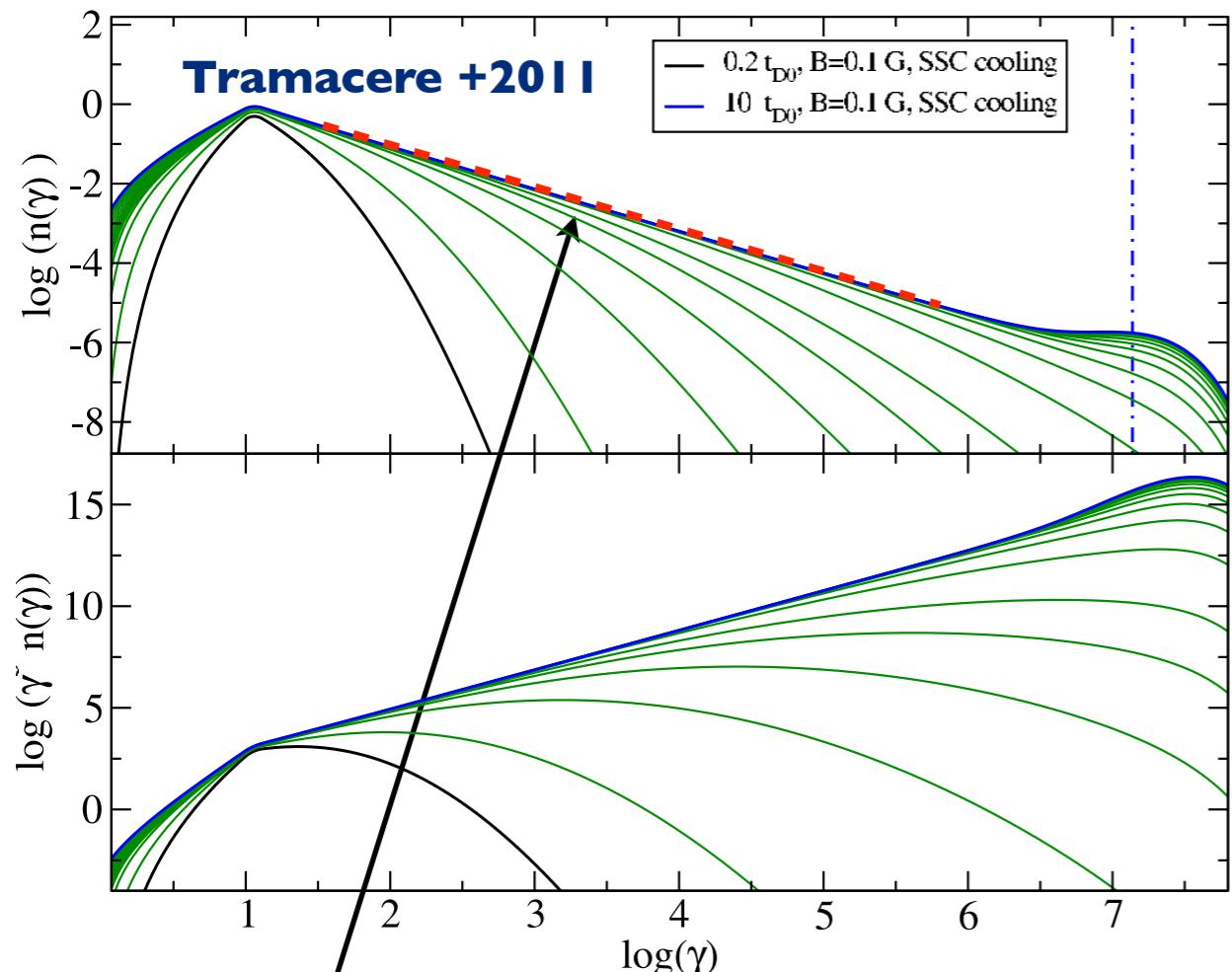


Synchrotron
spectral trends

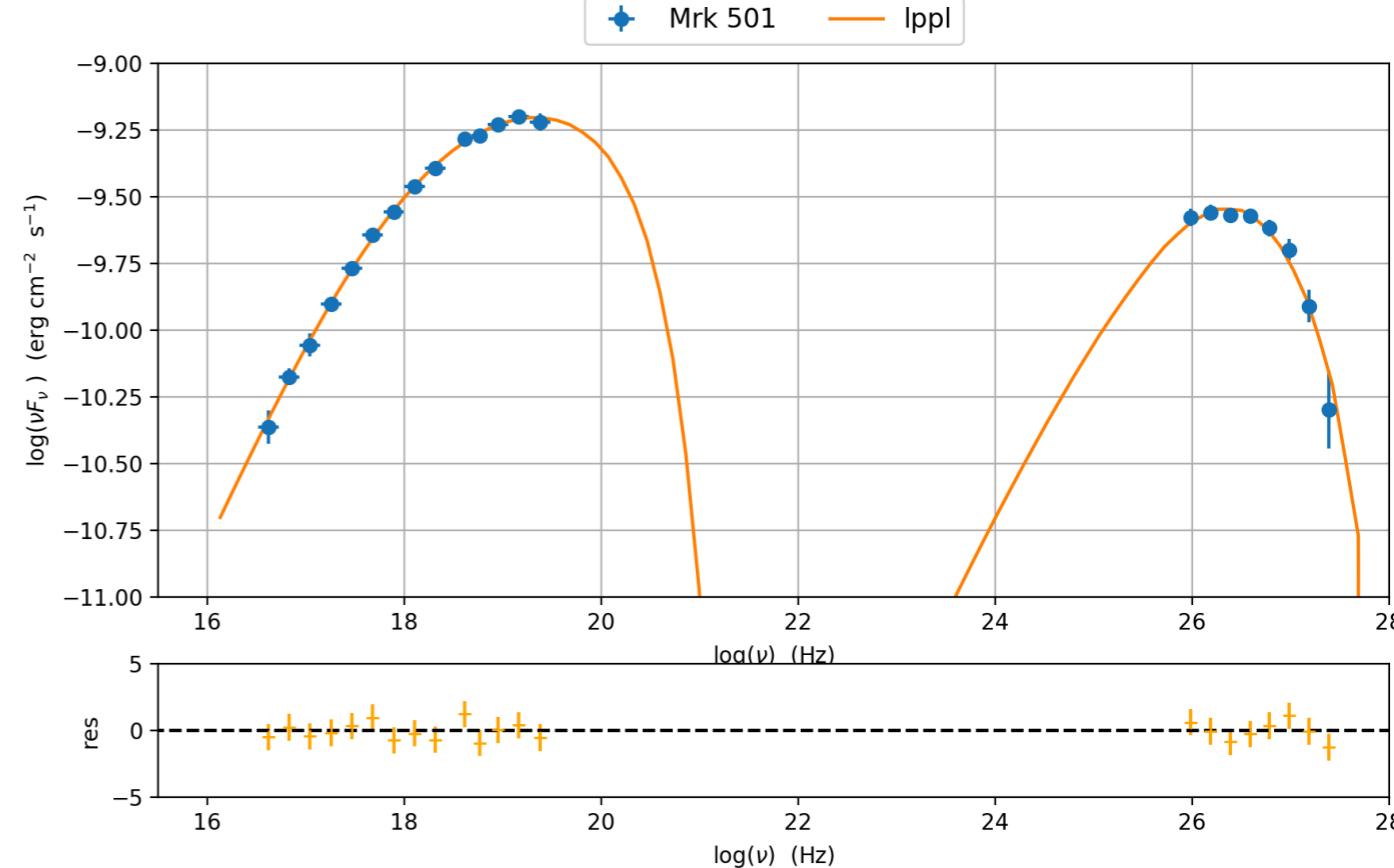
Pile-up and hard spectra

$q=2$, $R=10^{15}$ cm, $B=0.1$ G, $t_{\text{inj}}=t_D=10^4$ s

Mrk 501 1997



$$s \text{ in agreement with } s = 1 + \frac{t_{acc}}{2t_{esc}}$$



Massaro & Tramacere +2006

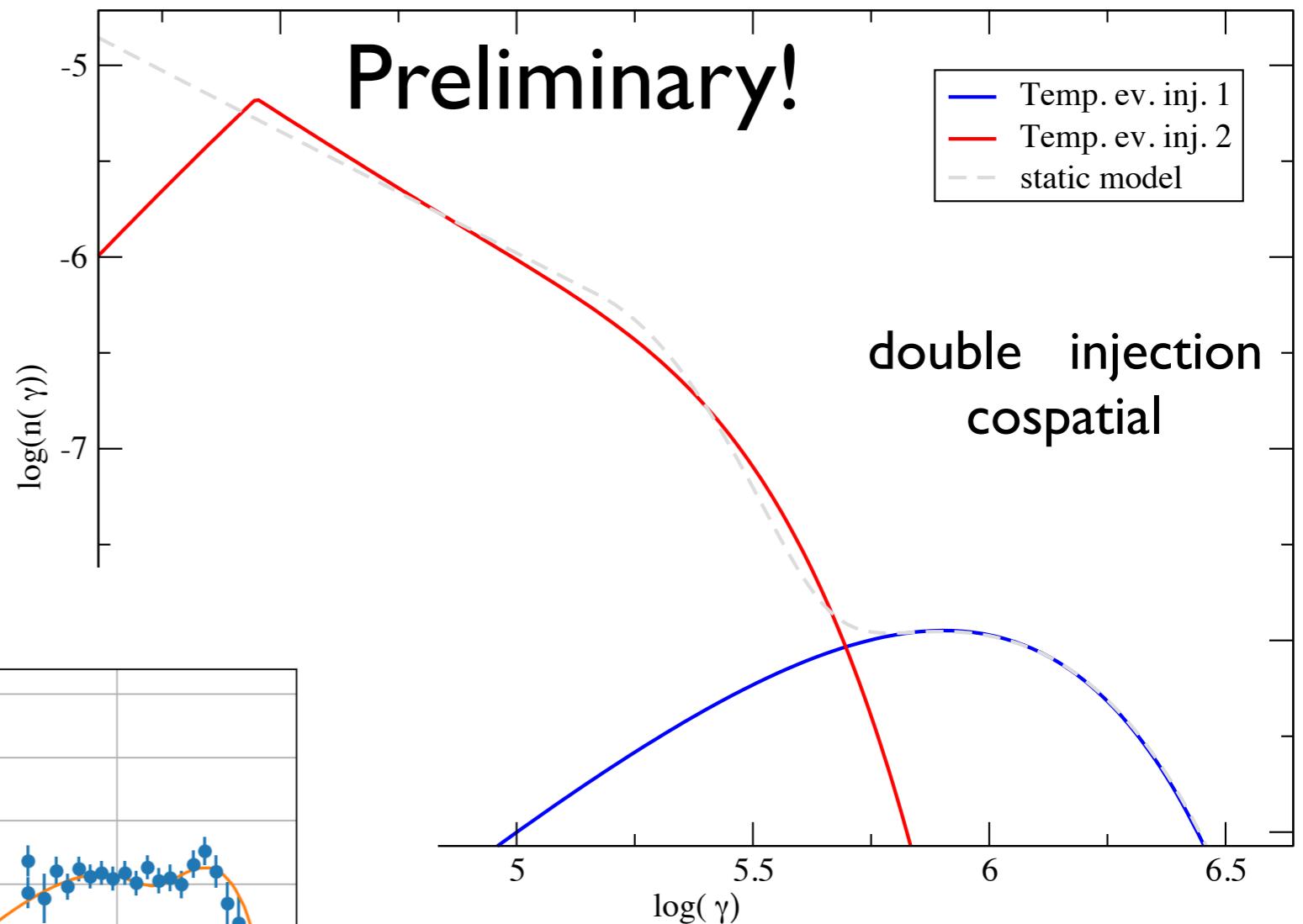
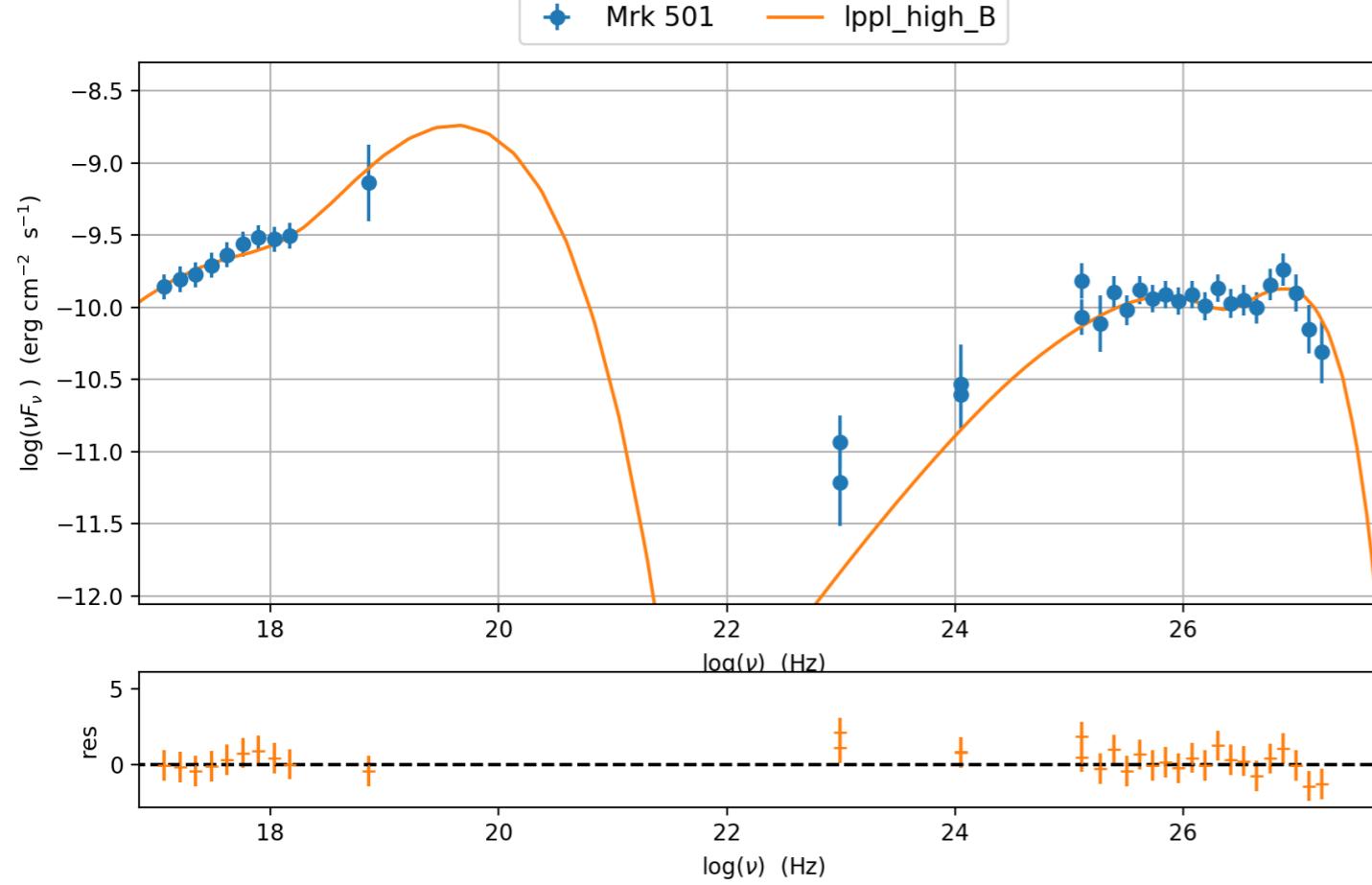
s~1.6

r~0.7-0.8<<r_{eq}~6

s<<s_{FI}~2.3

Pile-up and hard spectra

Mrk 501 2014 Flare
MAGIC paper
(submitted)



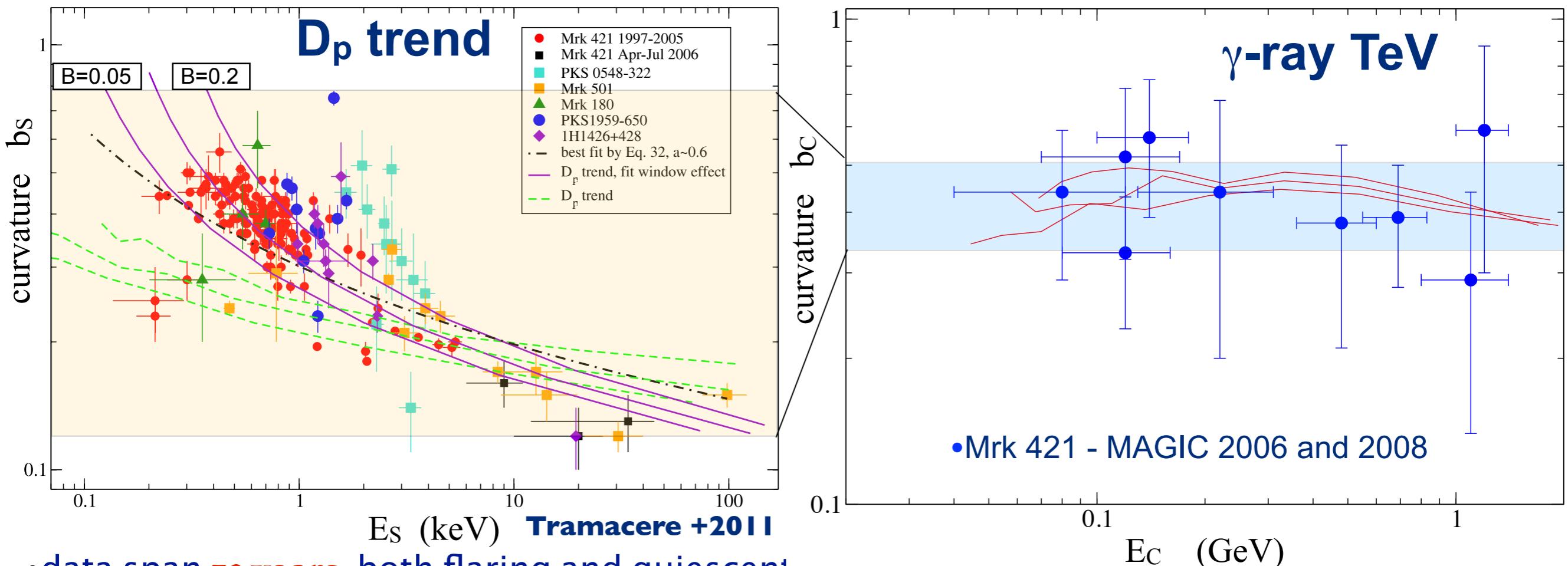
Summary of Stochastic signatures from self-consistent modeling

	Acceleration dominated	Equilibrium
curvature trend	curvature decreasing trend <i>b-Ep</i>	curvature stable or increasing (r~7,b~1.3)
spectral shape	LPPL or LP	PL+exp-cutoff or Maxwellian

spectral trends

multiple flares and population trends

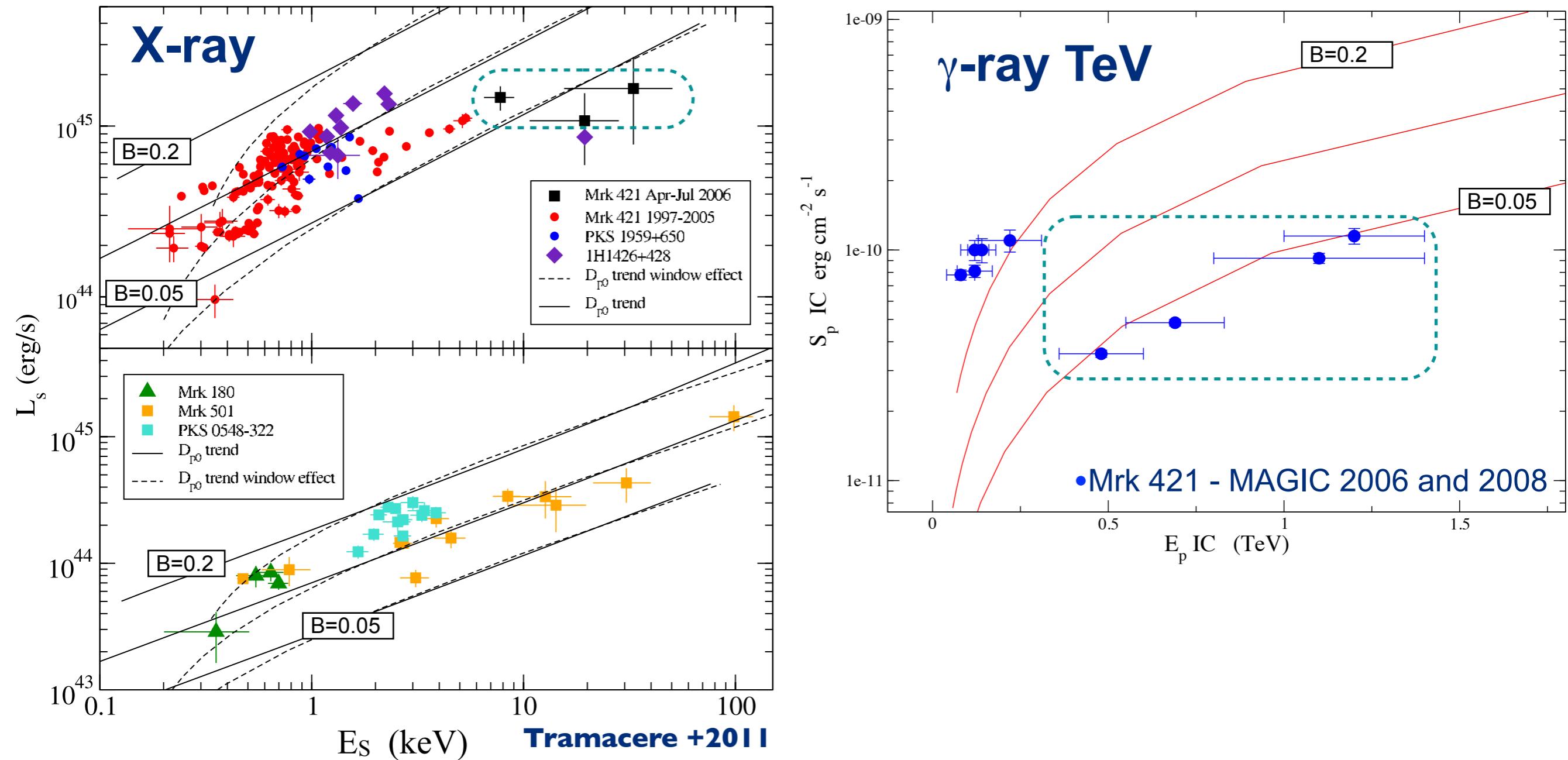
E_s - b_s X-ray trend and γ -ray predictions



- data span **13 years**, both flaring and quiescent states
- We are able to reproduce these long-term behaviours, by changing the value of only one parameter (D_p)
- for $q=2$, curvature values imply distribution far from the equilibrium ($b \sim [1.0-0.7]$)
- More data needed at GeV/TeV, curvature seems to be cooling-dominated
- Similar trend observed in GRBs (Massaro & Grindlay 2001)

L_{inj} (E_s - b_s trend) (erg s $^{-1}$)	5×10^{39}
L_{inj} (E_s - L_s trend) (erg s $^{-1}$)	$5 \times 10^{38}, 5 \times 10^{39}$
q	2
t_A (s)	1.2×10^3
$t_{D_0} = 1/D_{P0}$ (s)	$[1.5 \times 10^4, 1.5 \times 10^5]$
T_{inj} (s)	10^4
T_{esc} (R/c)	2.0

E_s - L_s X-ray trend and γ -ray predictions



- the E_s - S_s (E_s - L_s) relation follows naturally from that between E_s and b_s
- the low L_{inj} objects (Mrk 501 vs Mrk 421) reach a larger E_s , compatibly with larger γ_{eq}
- Mrk 421 MAGIC data on 2006 match very well the Synchrotron prediction with simultaneous X-ray data
- the average index of the trend $L_s \propto E_s^\alpha$ with $\alpha \sim 0.6$, is compatible with the data, and with a scenario in which a typical constant energy ($L_{\text{inj}} \times t_{\text{inj}}$) is injected for any flare (jet-feeding problem), whilst the peak dynamic is ruled by the turbulence in the magnetic field.

<https://jetset.readthedocs.io/en/latest/>

<https://github.com/andreatramacere/jetset/archive/stable.tar.gz>

to get the beta release
write to

- andrea.tramacere@gmail.com
- andrea.tramacere@unige.ch

 JetSeT 1.0 JetSeT ▾ Page ▾ Installation » Source Search

JetSeT Documentation



JetSeT

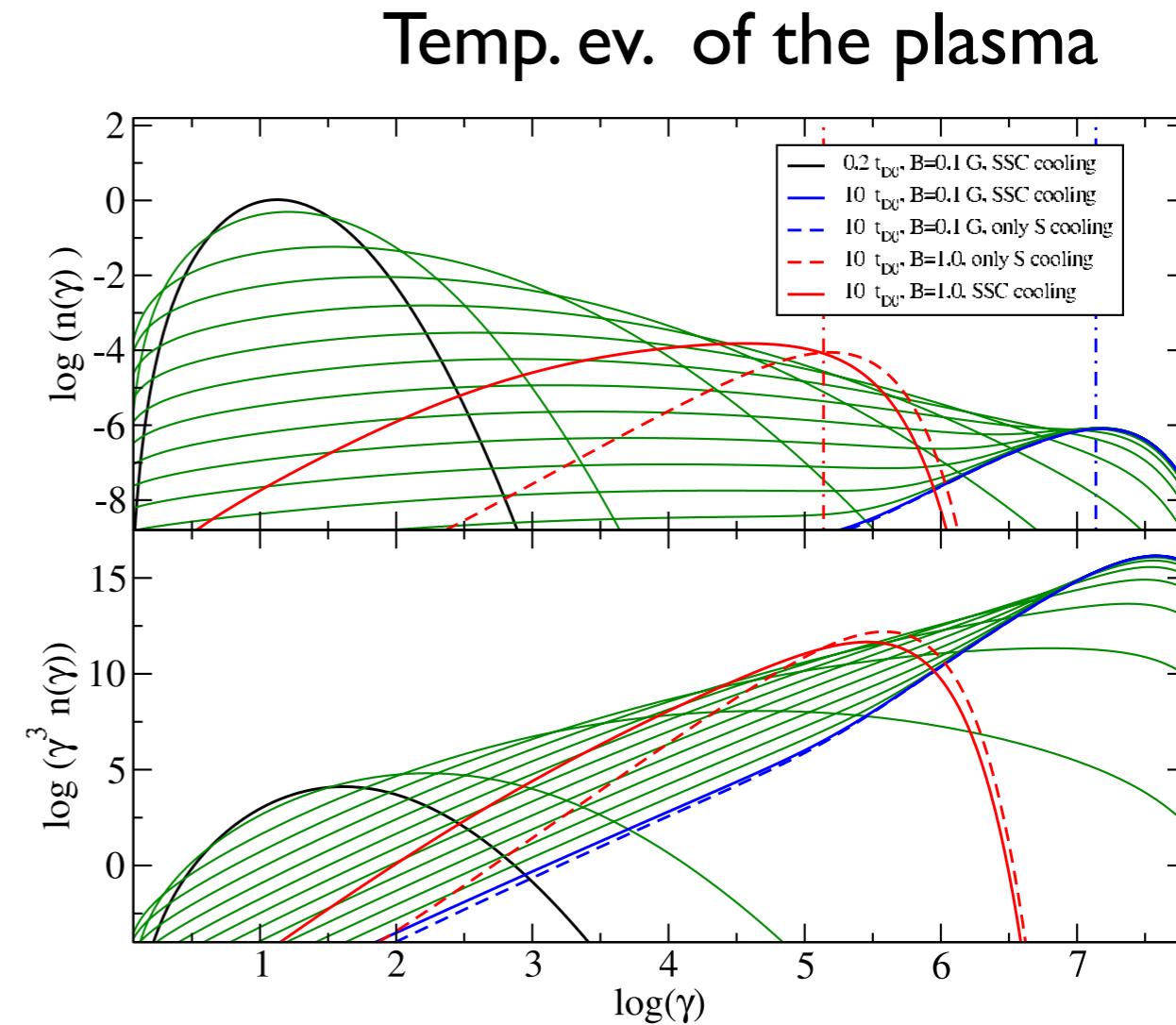
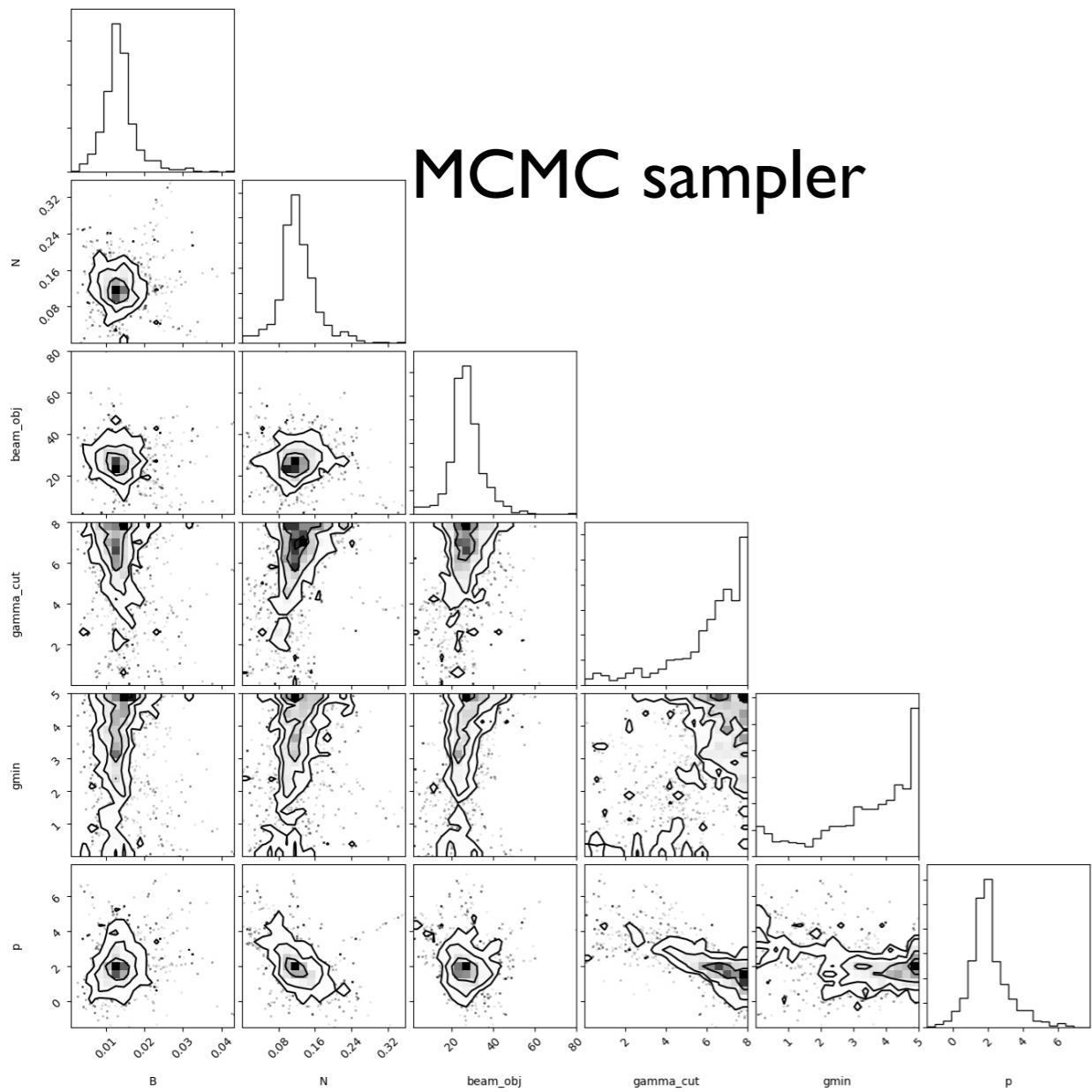
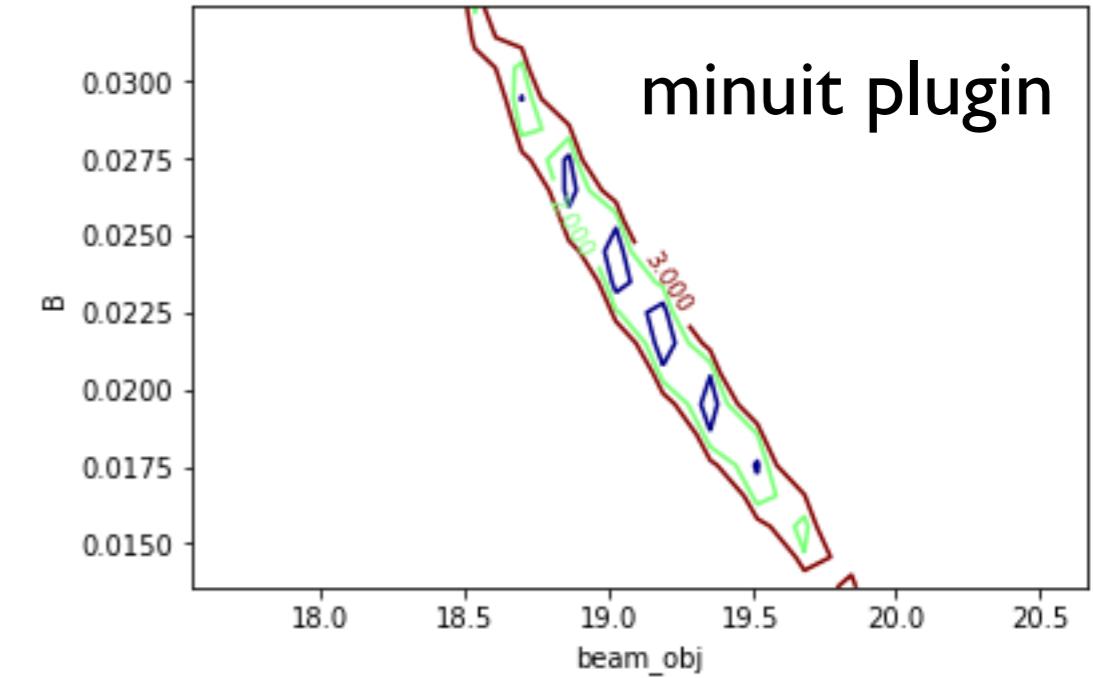
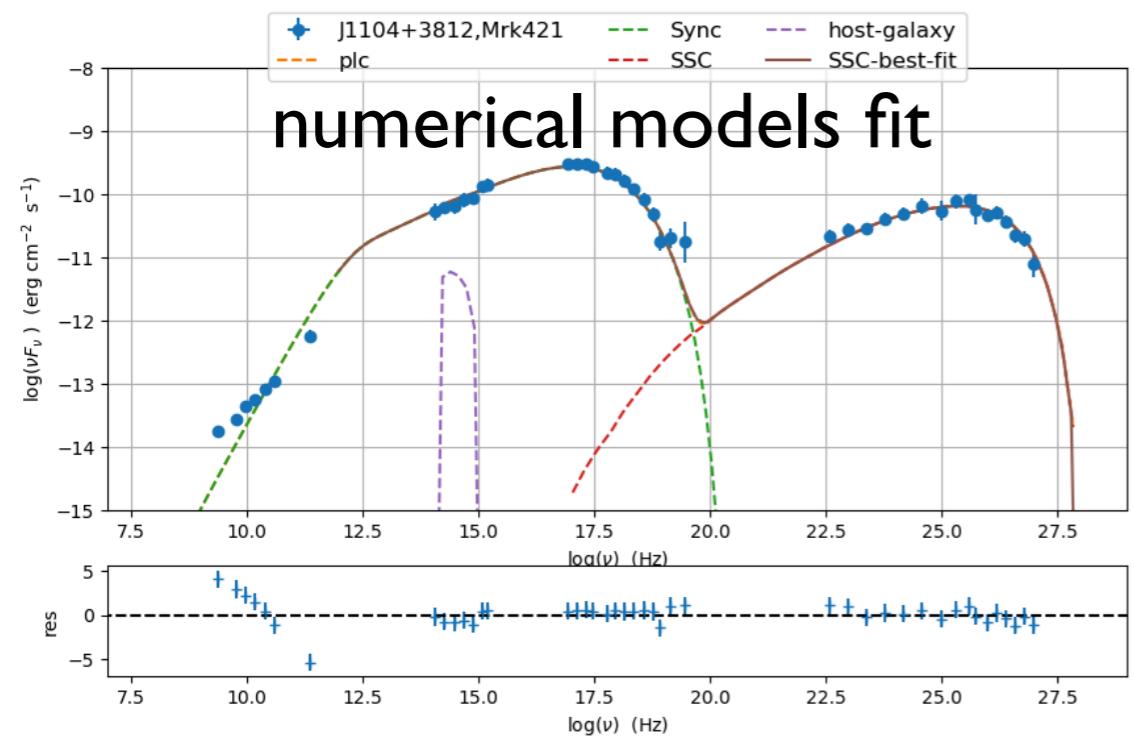
Jets SED modeler and fitting Tool

Author: [Andrea Tramacere](#)

JetSeT is an open source C/Python framework to reproduce radiative and accelerative processes acting in relativistic jets, allowing to fit the numerical models to observed data. The main features of this framework are:

- handling observed data: re-binning, definition of data sets, bindings to astropy tables and quantities definition of complex numerical radiative scenarios: Synchrotron Self-Compton (SSC), external Compton (EC) and EC against the CMB
- Constraining of the model in the pre-fitting stage, based on accurate and already published phenomenological trends. In particular, starting from phenomenological parameters, such as spectral indices, peak fluxes and frequencies, and spectral curvatures, that the code evaluates automatically, the pre-fitting algorithm is able to provide a good starting model, following the phenomenological trends that I have implemented. fitting of multiwavelength SEDs using both frequentist approach (iminuit) and bayesian MCMC sampling (emcee)
- Self-consistent temporal evolution of the plasma under the effect of radiative and accelerative processes, both first order and second order (stochastic acceleration) processes.

 v: latest ▾



backup slides

injection term

$$L_{inj} = \frac{4}{3}\pi R^3 \int \gamma_{inj} m_e c^2 Q(\gamma_{inj}, t) d\gamma_{inj} \quad (erg/s)$$

systematic term

$$S(\gamma, t) = -C(\gamma, t) + A(\gamma, t)$$

cooling term

$$C(\gamma) = |\dot{\gamma}_{\text{synch}}| + |\dot{\gamma}_{\text{IC}}|$$

syst. acc. term

$$A(\gamma) = A_{p0}\gamma, t_A = \frac{1}{A_0}$$

$$\frac{\partial n(\gamma, t)}{\partial t} = \frac{\partial}{\partial \gamma} \left\{ -[S(\gamma, t) + D_A(\gamma, t)]n(\gamma, t) + D_p(\gamma, t)\frac{\partial n(\gamma, t)}{\partial \gamma} \right\} - \frac{n(\gamma, t)}{T_{\text{esc}}(\gamma)} + Q(\gamma, t)$$

Turbulent magnetic field



momentum diffusion term

$$W(k) = \frac{\delta B(k_0^2)}{8\pi} \left(\frac{k}{k_0}\right)^{-q}$$

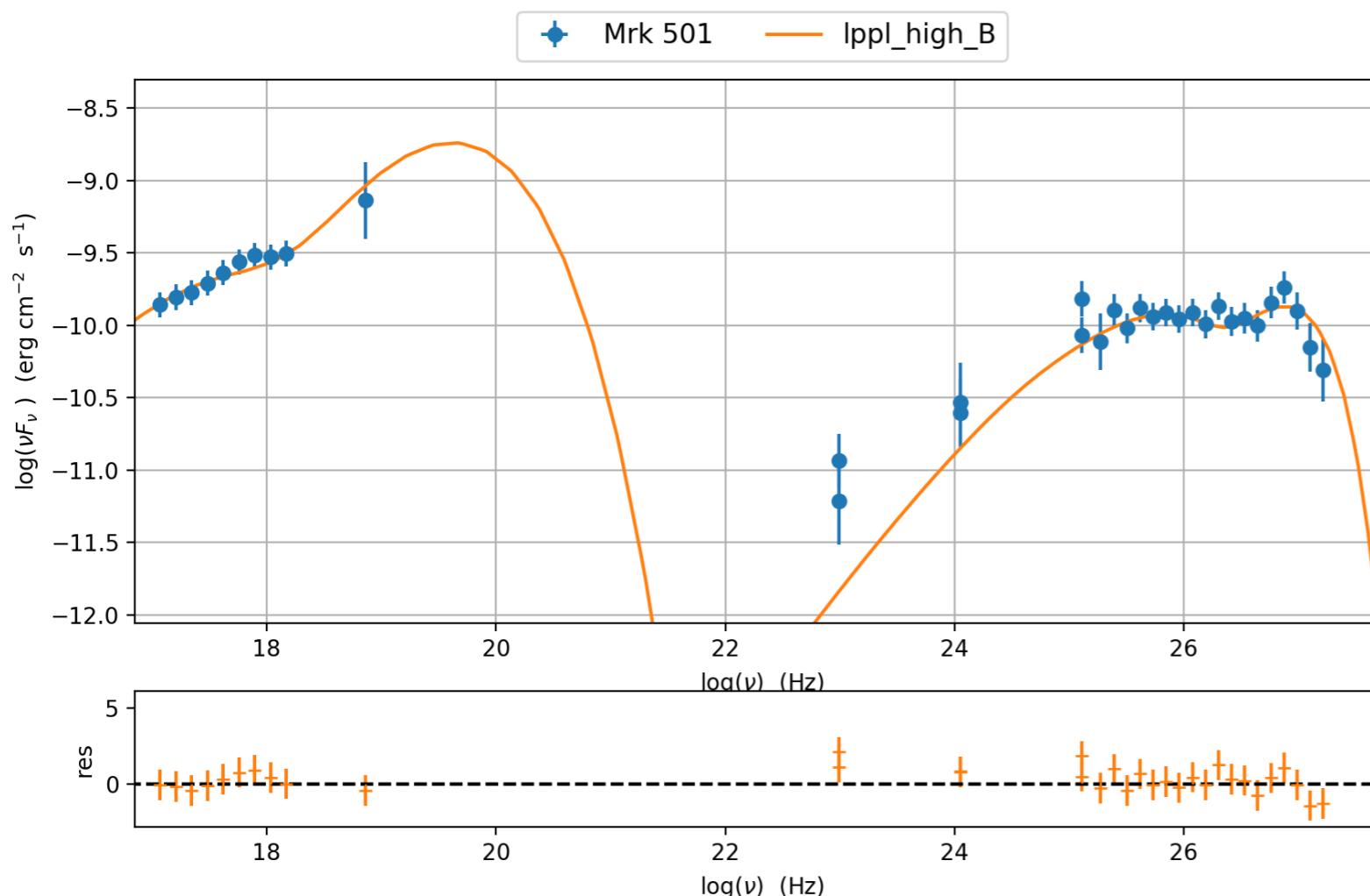
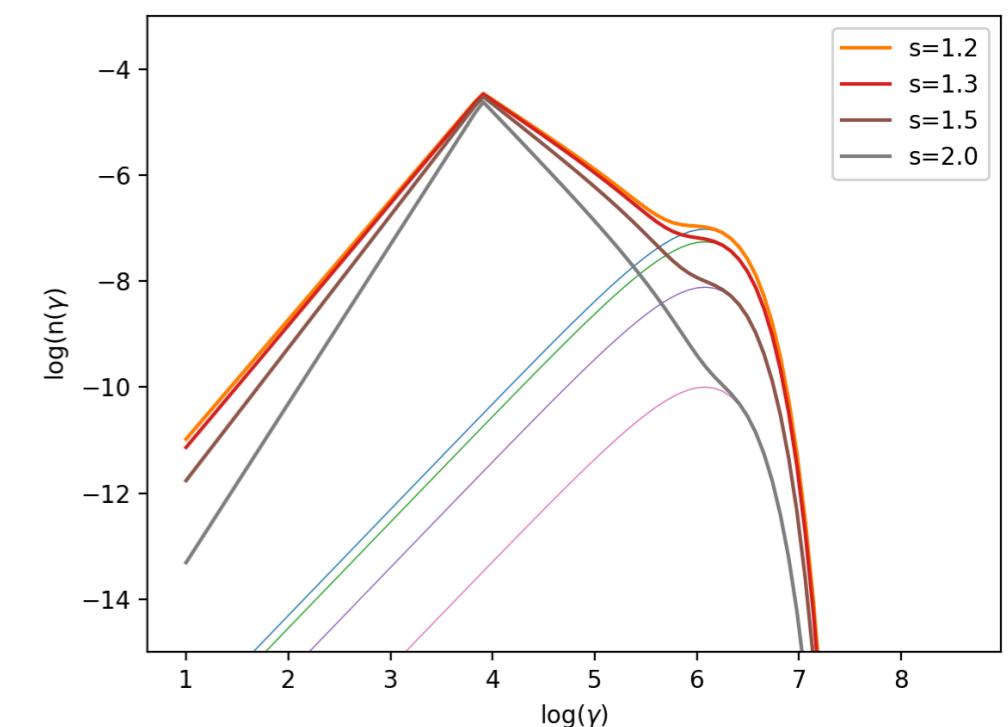
Mrk 501 2014 Flare

MAGIC paper (submitted)

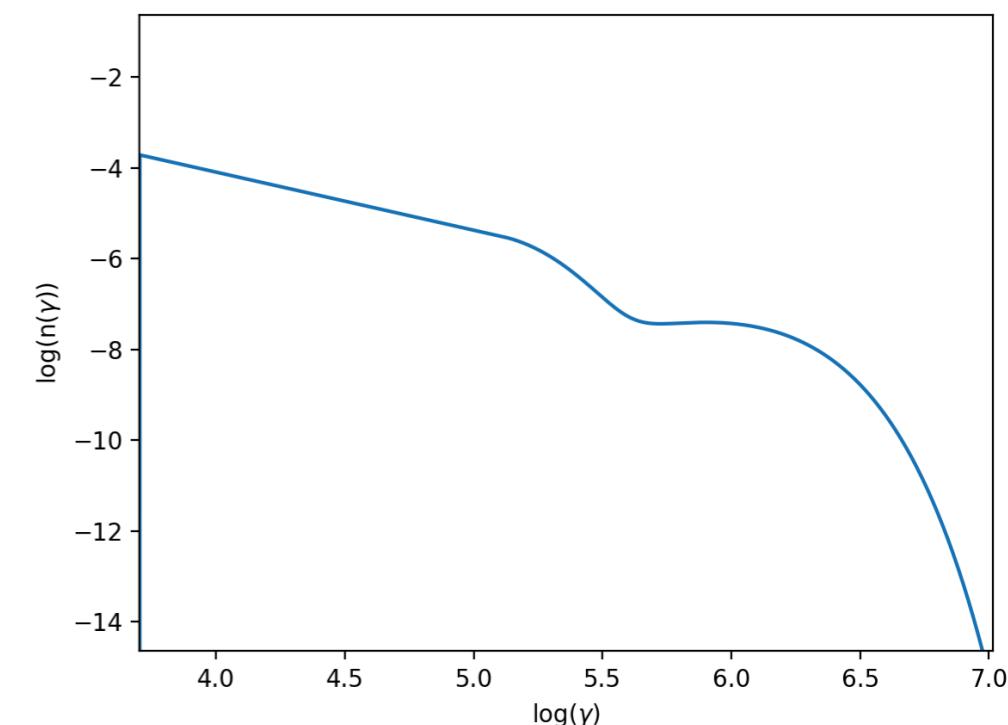
cont. single injection (Stawarz&Petrosian 2009)
not compatible with MW data

model parameters:

Name	Type	Units	value
B	magnetic_field	G	+3.000000e-01
N	electron_density	cm ⁻³	+2.360060e+00
R	region_size	cm	+1.551851e+01
alpha_pile_up	turn-over-energy		+1.000000e+00
beam_obj	beaming		+1.000000e+01
gamma0_log_parab	turn-over-energy	Lorentz-factor	+1.300000e+05
gamma_inj	turn-over-energy	Lorentz-factor	+5.000000e+03
gamma_pile_up	turn-over-energy	Lorentz-factor	+4.000000e+05
gmax	high-energy-cut-off	Lorentz-factor	+1.000000e+07
gmin	low-energy-cut-off	Lorentz-factor	+5.000000e+03
r	spectral_curvature		+6.100000e+00
ratio_pile_up	turn-over-energy		+7.000000e-18
s	LE_spectral_slope		+1.280000e+00
z_cosm	redshift		+3.364200e-02

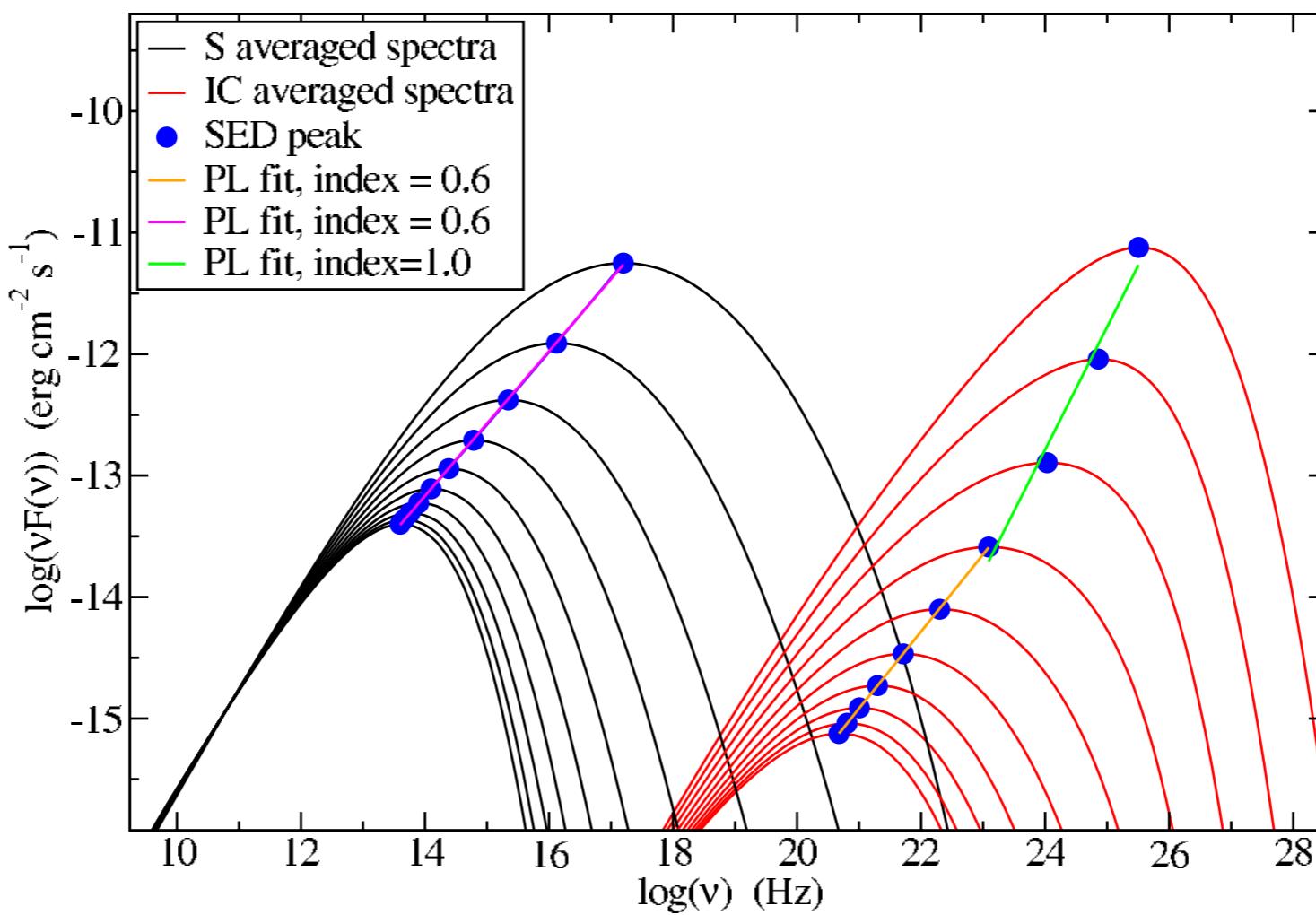


double cospatial injection
compatible with data

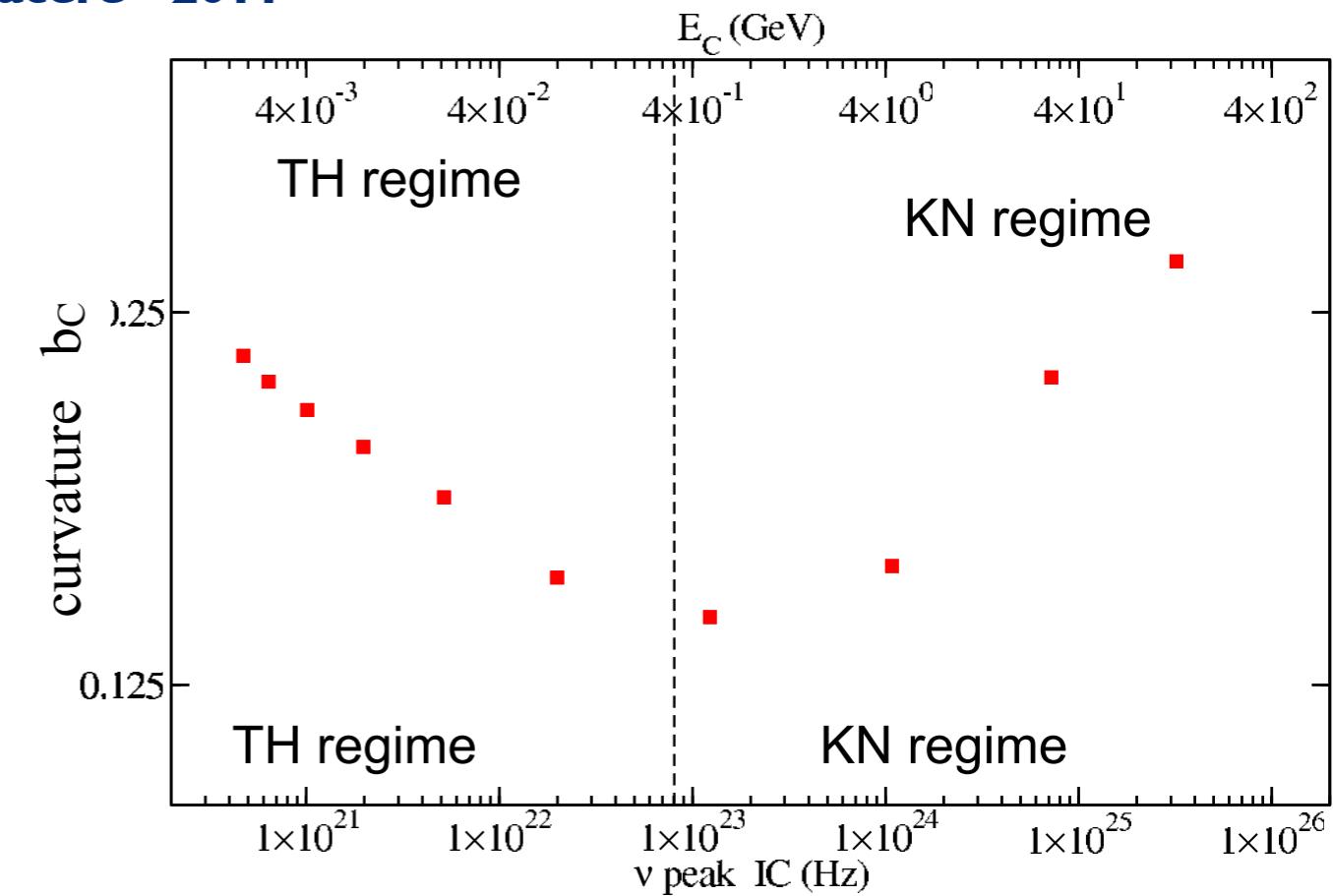
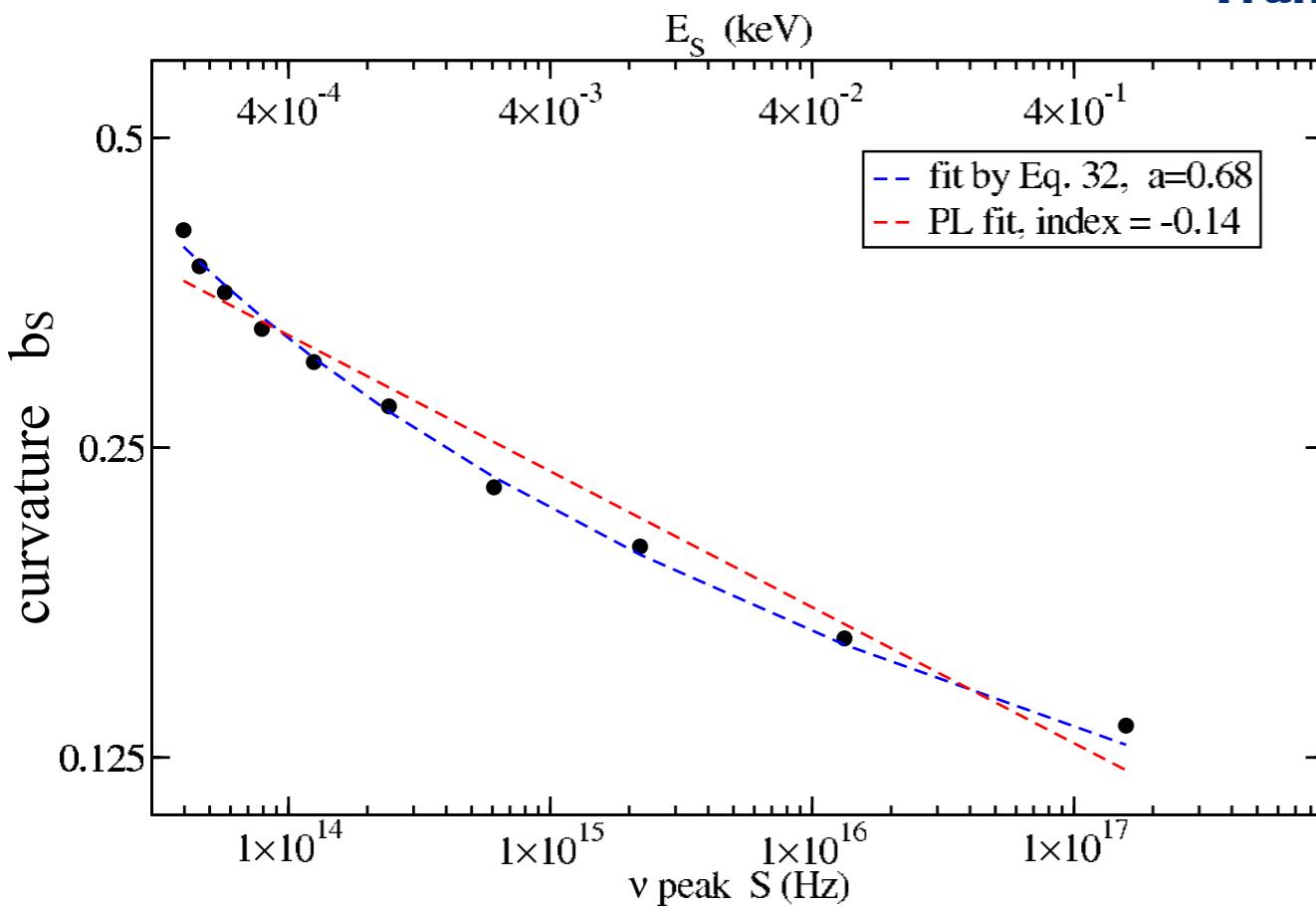


S vs IC

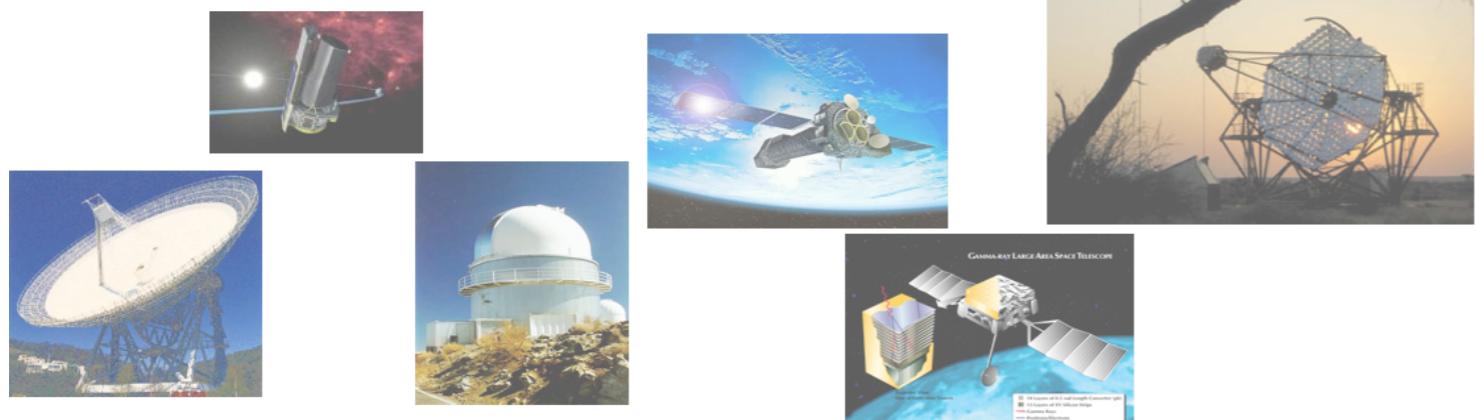
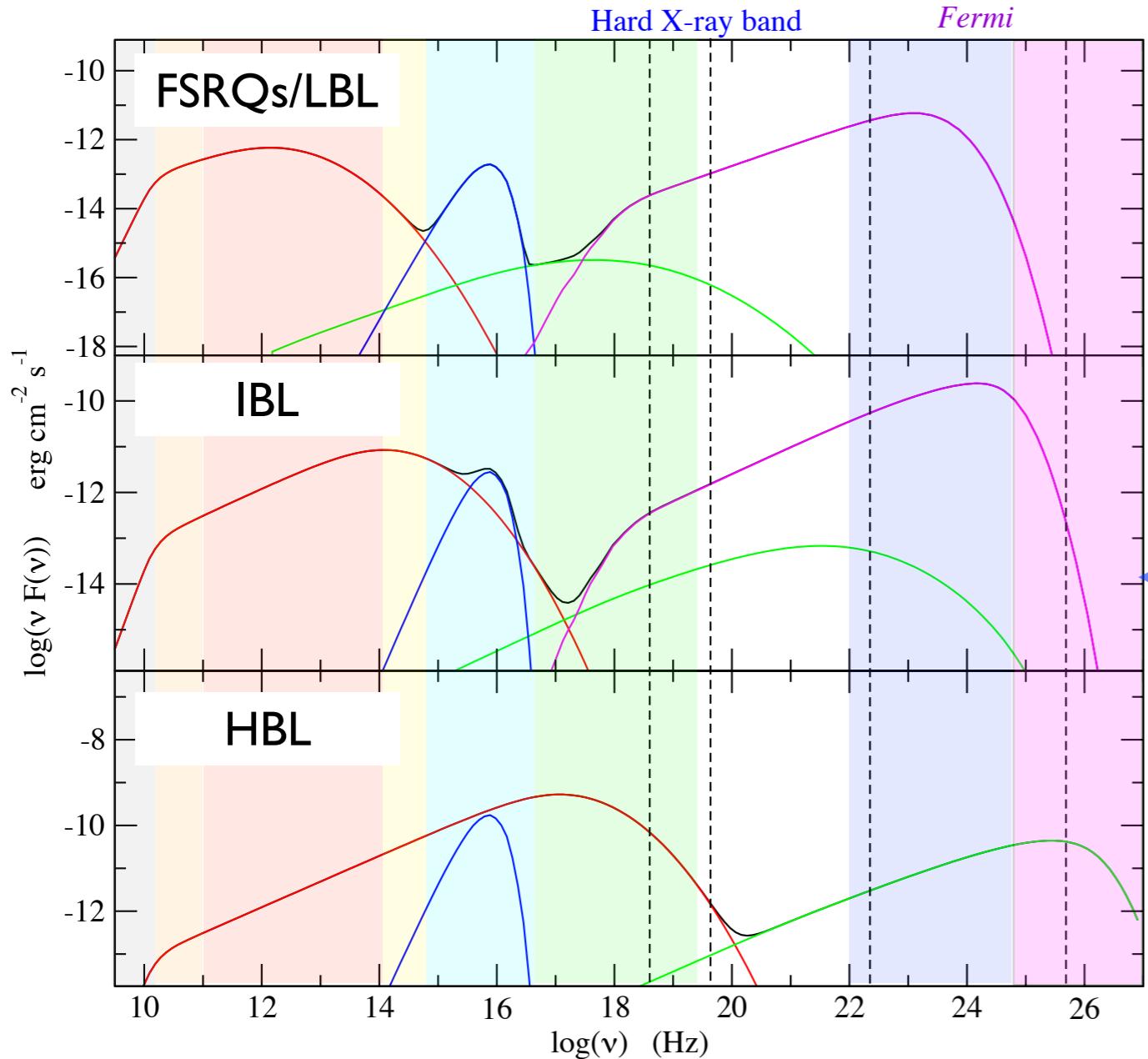
Tramacere+2011



Tramacere +2011



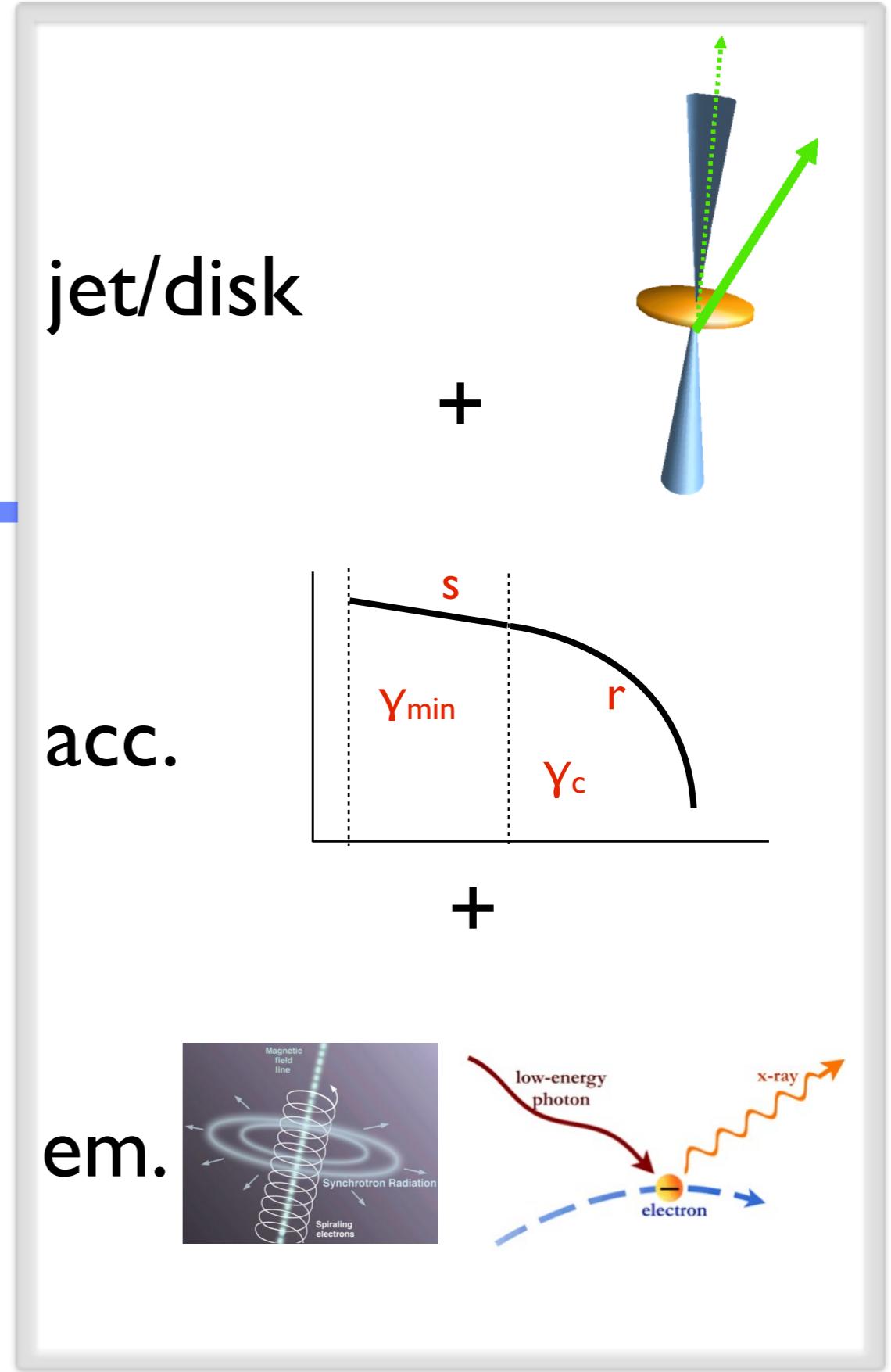
blazars in a nutshell



jet/disk

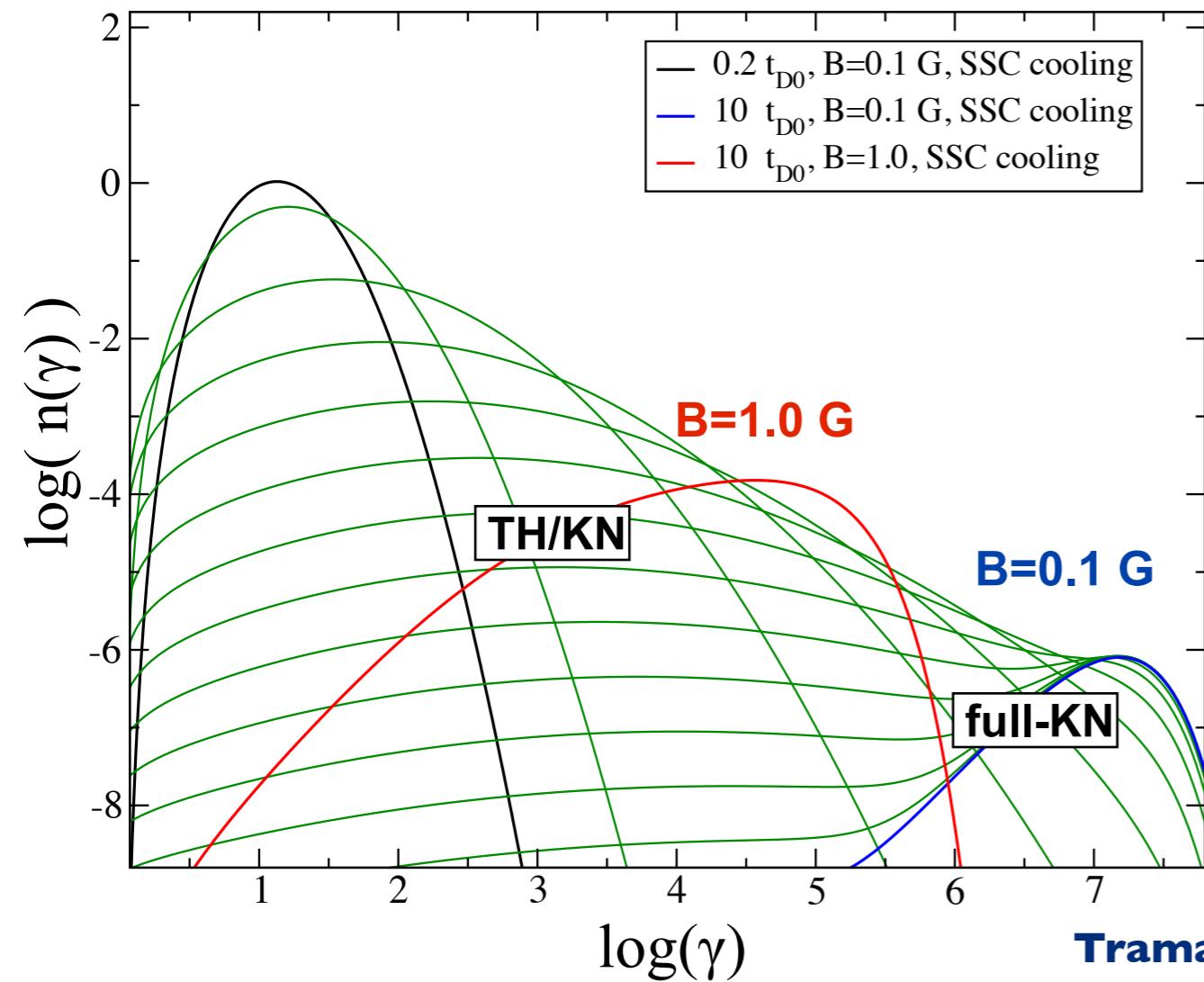
acc.

em.

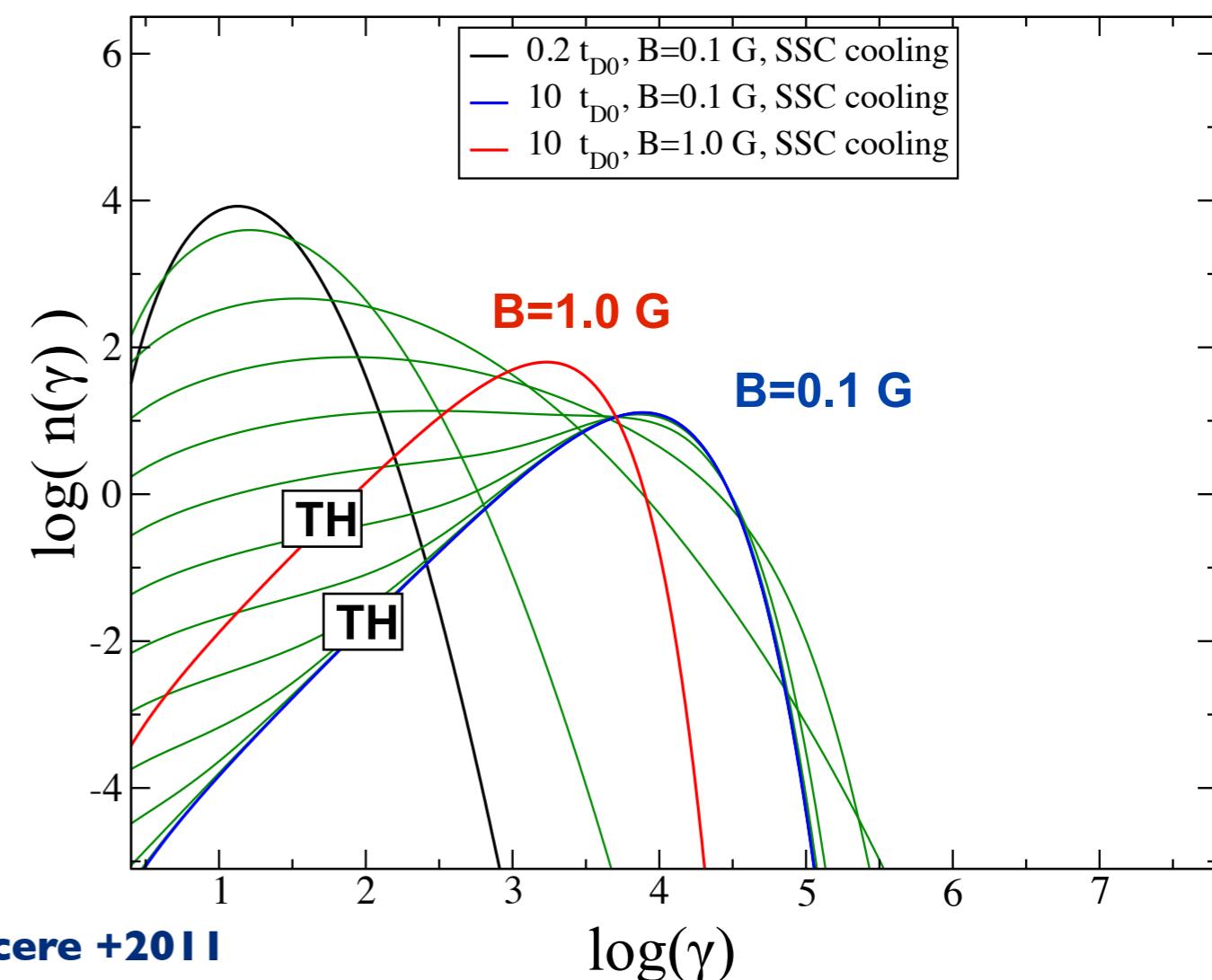


IC cooling and equilibrium

$R = 1 \times 10^{15} \text{ cm}$



$R = 5 \times 10^{13} \text{ cm}$

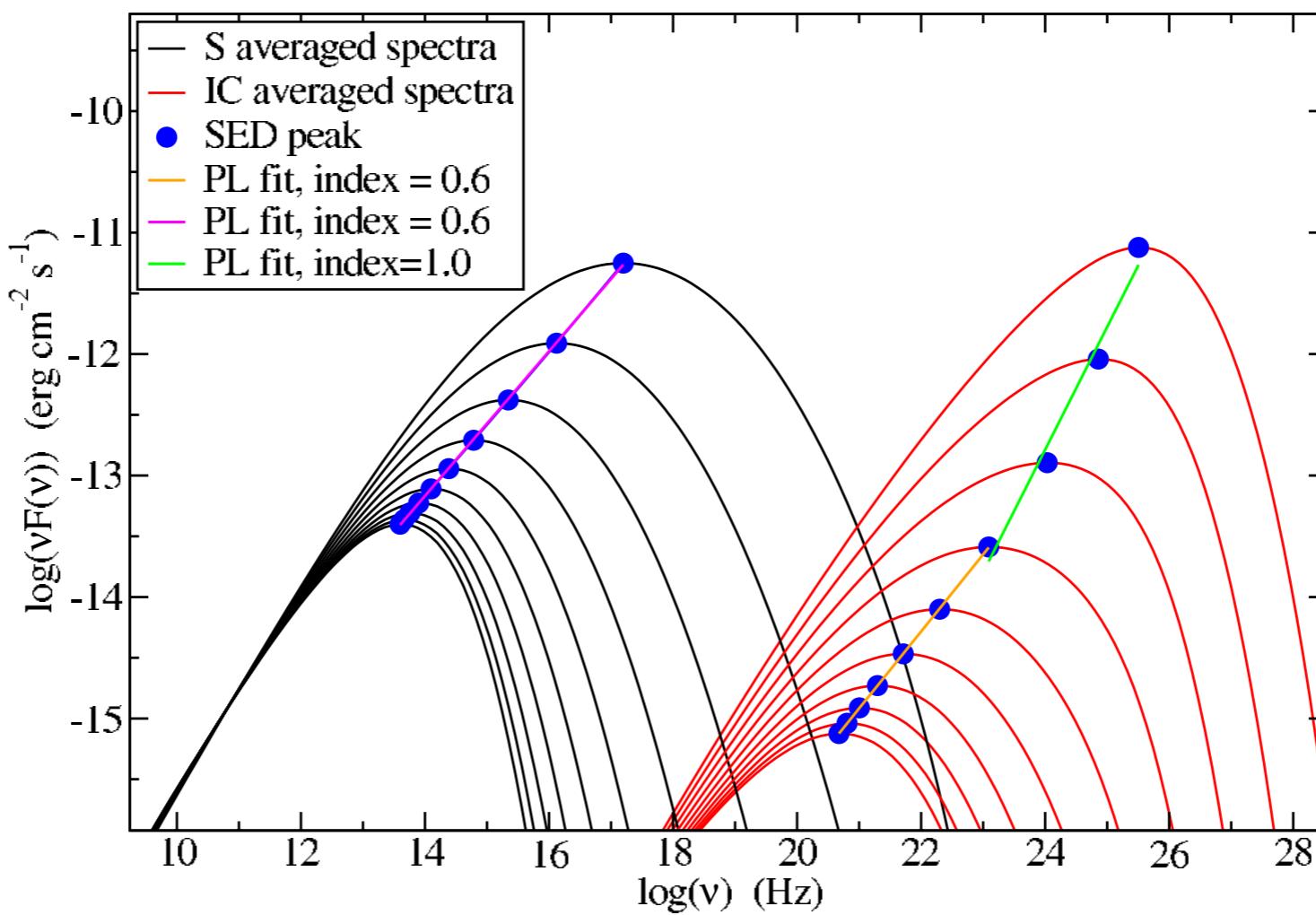


U_{ph} ($R = 1 \times 10^{13} \text{ cm}$) $\gg U_{ph}$ ($R = 1 \times 10^{15} \text{ cm}$)

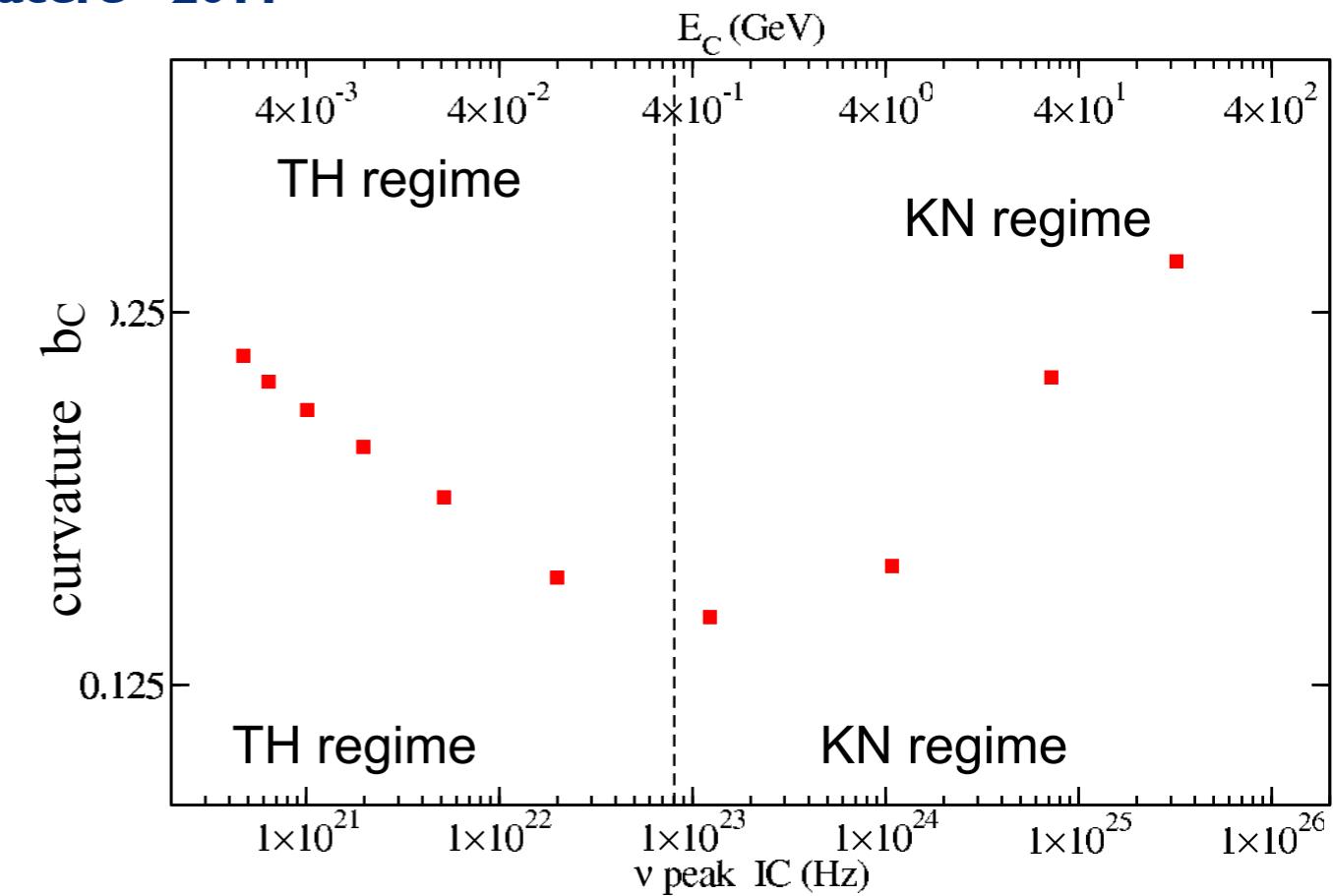
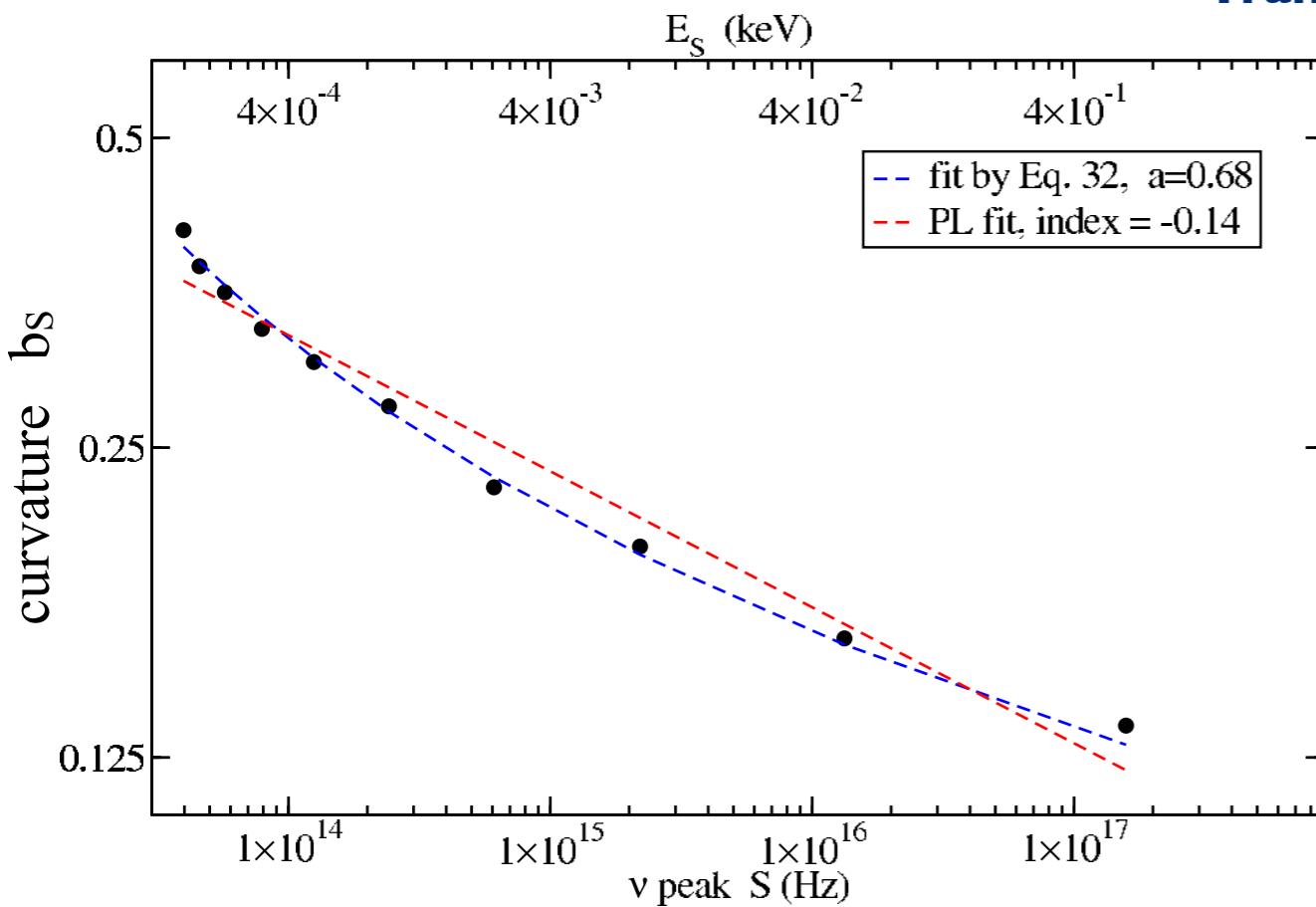
IC prevents higher energies in more compact accelerators (if all the parameters are the same) **Impact on rapid TeV variability!**

S vs IC

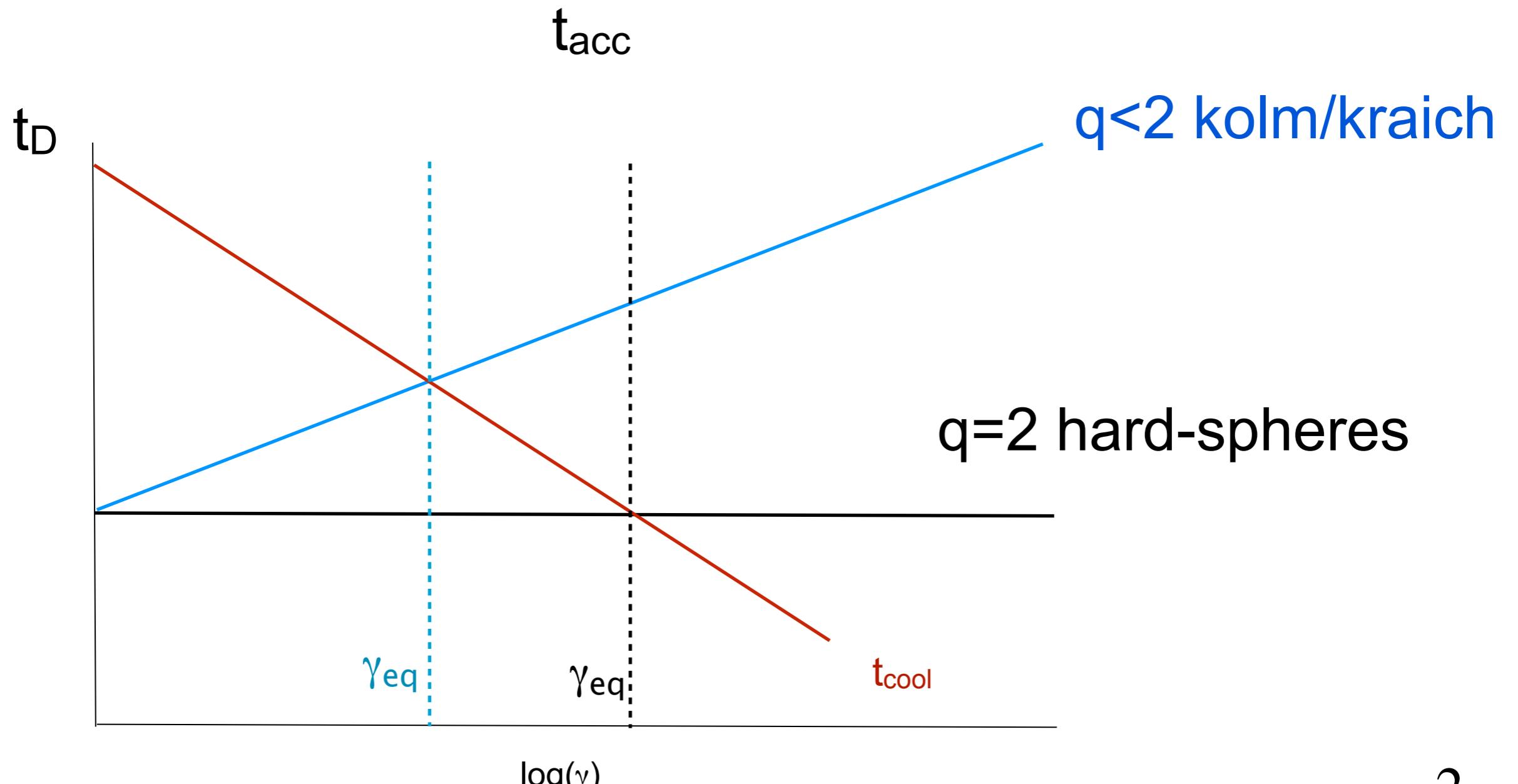
Tramacere+2011



Tramacere +2011



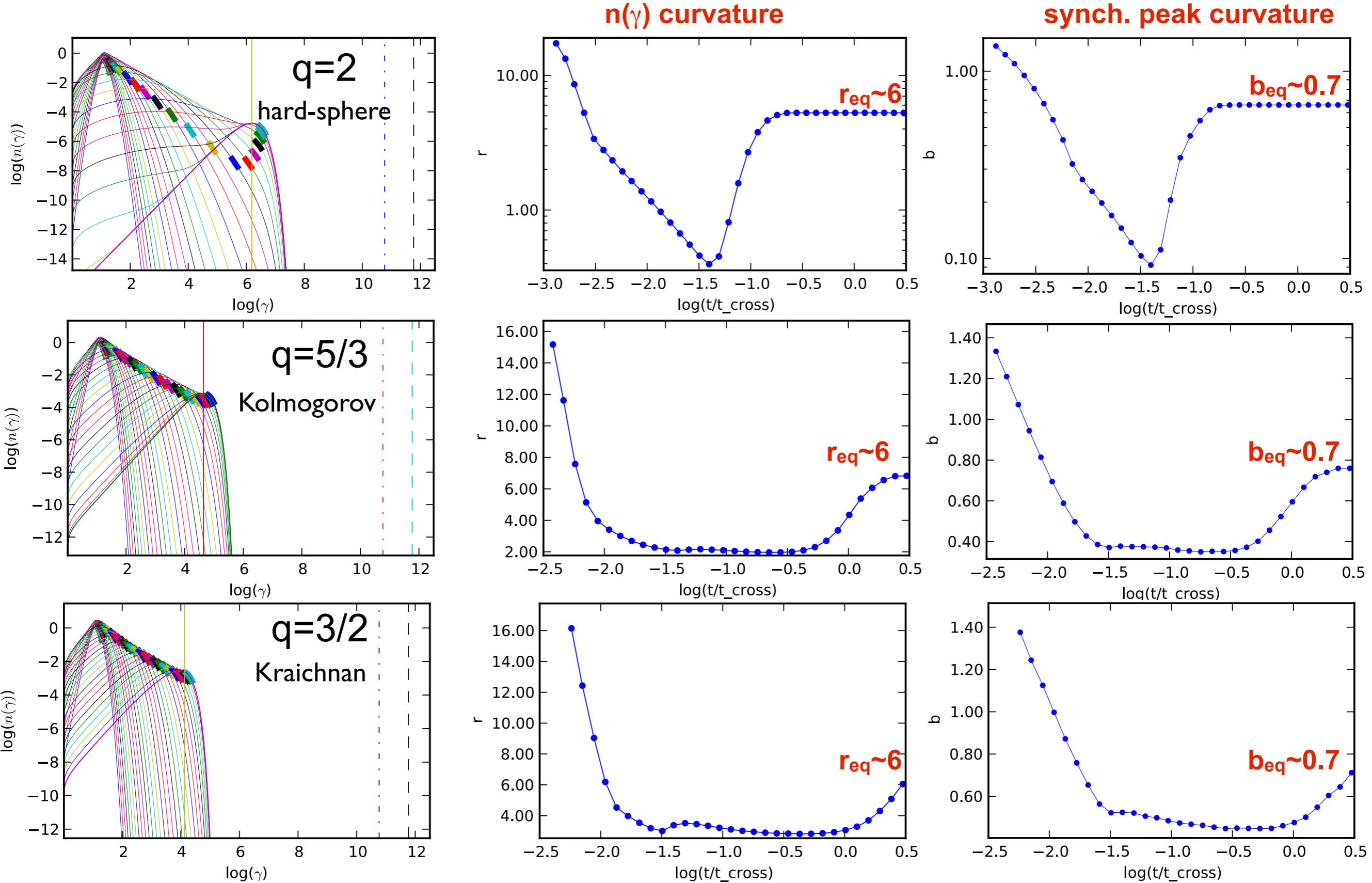
effect of the turbulence index q



$$t_D = \frac{1}{D_{p0}} \left(\frac{\gamma}{\gamma_0} \right)^{2-q}$$

effect of the turbulence index q

$B=1.0 \text{ G}$, $t_{D0}=10^3$, $R=5\times 10^{15} \text{ cm}$



log-parabola is not a “new” model...

KARDASHEV 1962

320

N. S. KARDASHEV

1962SvA.....6...317K

At first, for simplicity, we consider the effect of each process viewed separately on the energy spectrum, and then the simultaneous effect of two or more processes.

Spectra of Isolated Processes

1. Random and Systematic Acceleration.

The kinetic equation is

$$\frac{\partial N}{\partial t} = \alpha_1(t) \frac{\partial}{\partial E} \left(E^2 \frac{\partial N}{\partial E} \right) - \alpha_2(t) \frac{\partial}{\partial E} (EN).$$

Let the energy distribution be specified, at each instant of time t_0 , by the δ -function in the neighborhood of energy E_0 :

and

$$N(E, 0) = N_0 \delta(E - E_0)$$

$$\int_0^\infty N(E, 0) dE = N_0.$$

Then, utilizing the techniques developed, e.g., in [13], we may find that

$$N(E, t) = \frac{N_0}{\sqrt{\pi} E^2 \sqrt{a_1}} e^{-\left(\ln \frac{E_0}{E} + a_1 + a_2\right)^2 / 4a_1}, \quad (1)$$

where

$$a_1 = \int_{t_0}^t \alpha_1(t) dt, \quad a_2 = \int_{t_0}^t \alpha_2(t) dt.$$

increases c
The quanti
to expansi
the quanti
sistently p
creasing E
and conver
correspond

For th
 $= KE_0^{-\gamma}$ is
 $E_{\min} \leq E_0$
initial con

$$\int_{E_{\min}}^{E_{\max}} K$$

=

where

x

At E_{\max}

statistical approach

$$n(\gamma) = \frac{N_0}{\gamma \sigma_\gamma \sqrt{2\pi}} \exp \left[\frac{-(\ln(\gamma/\gamma_0) - n_s [\ln \bar{\varepsilon} - \frac{1}{2}(\sigma_\varepsilon/\bar{\varepsilon})^2])^2}{2n_s(\sigma_\varepsilon/\bar{\varepsilon})^2} \right].$$

$$\log(n(\gamma)) \propto \frac{(\log \gamma - \mu)^2}{2\sigma_\gamma^2} \propto r [\log(\gamma) - \mu]^2$$

diffusion equation approach

$$n(\gamma, t) = \frac{N_0}{\gamma \sqrt{4\pi D_{p0}t}} \exp \left\{ -\frac{[\ln(\gamma/\gamma_0) - (A_{p0} - D_{p0}t)]^2}{4D_{p0}t} \right\}$$

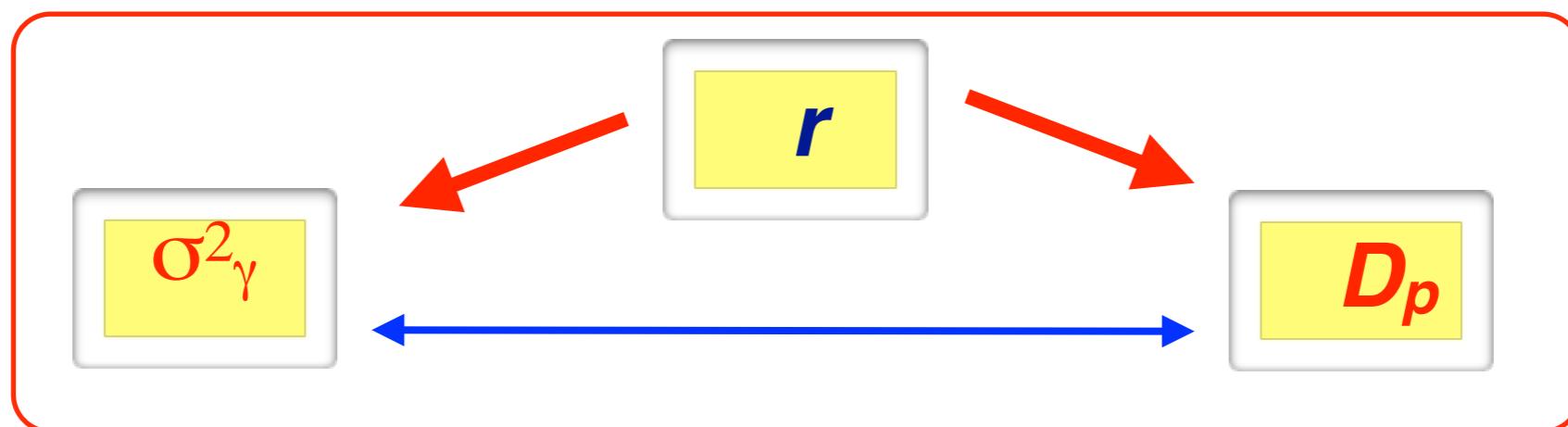
$$r \propto \frac{1}{D_{p0}t}$$



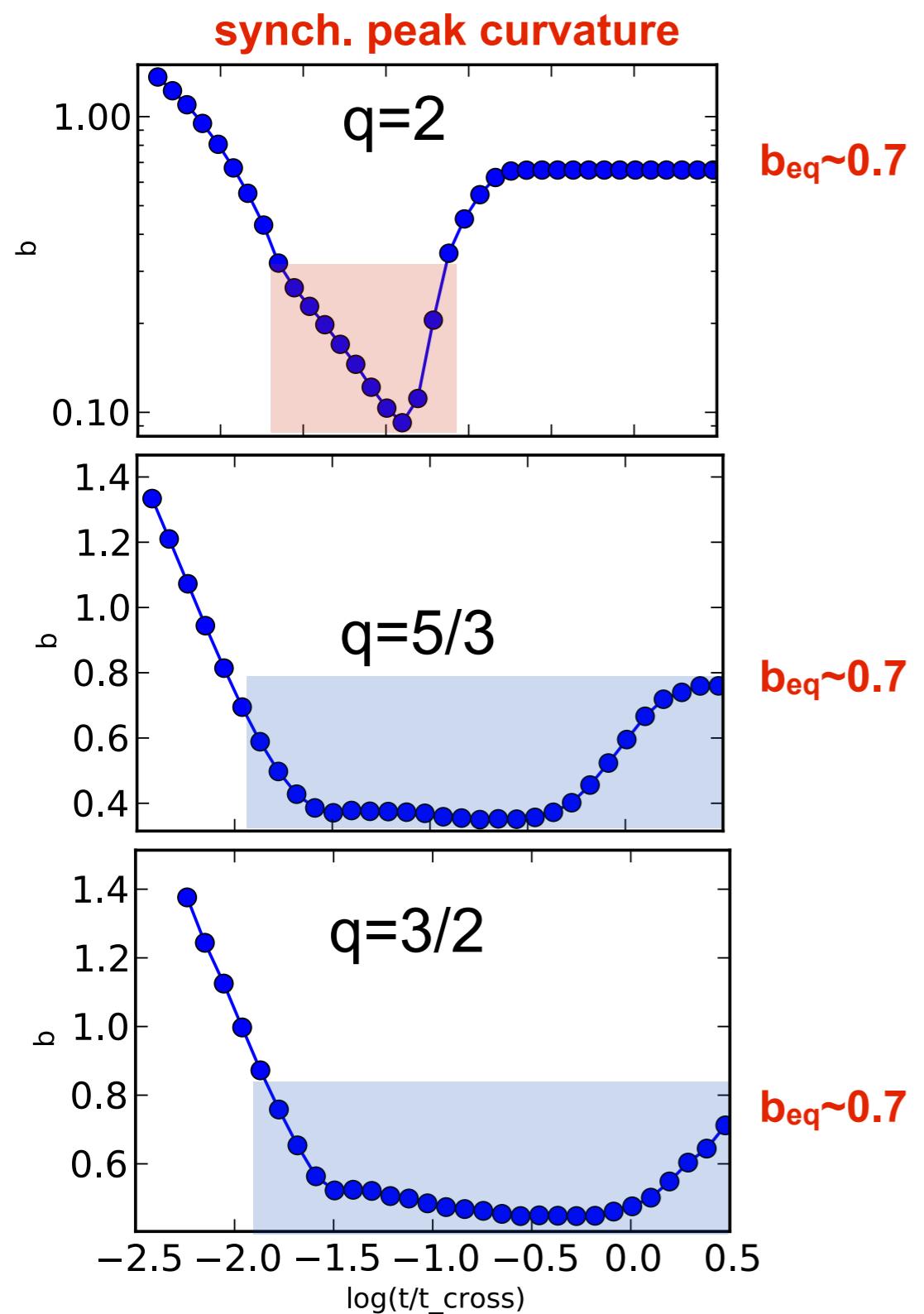
$$D_{p0} \propto \left(\frac{\sigma_\varepsilon}{\bar{\varepsilon}} \right)^2$$

The curvature r is inversely proportional to D_{p0} and σ_ε

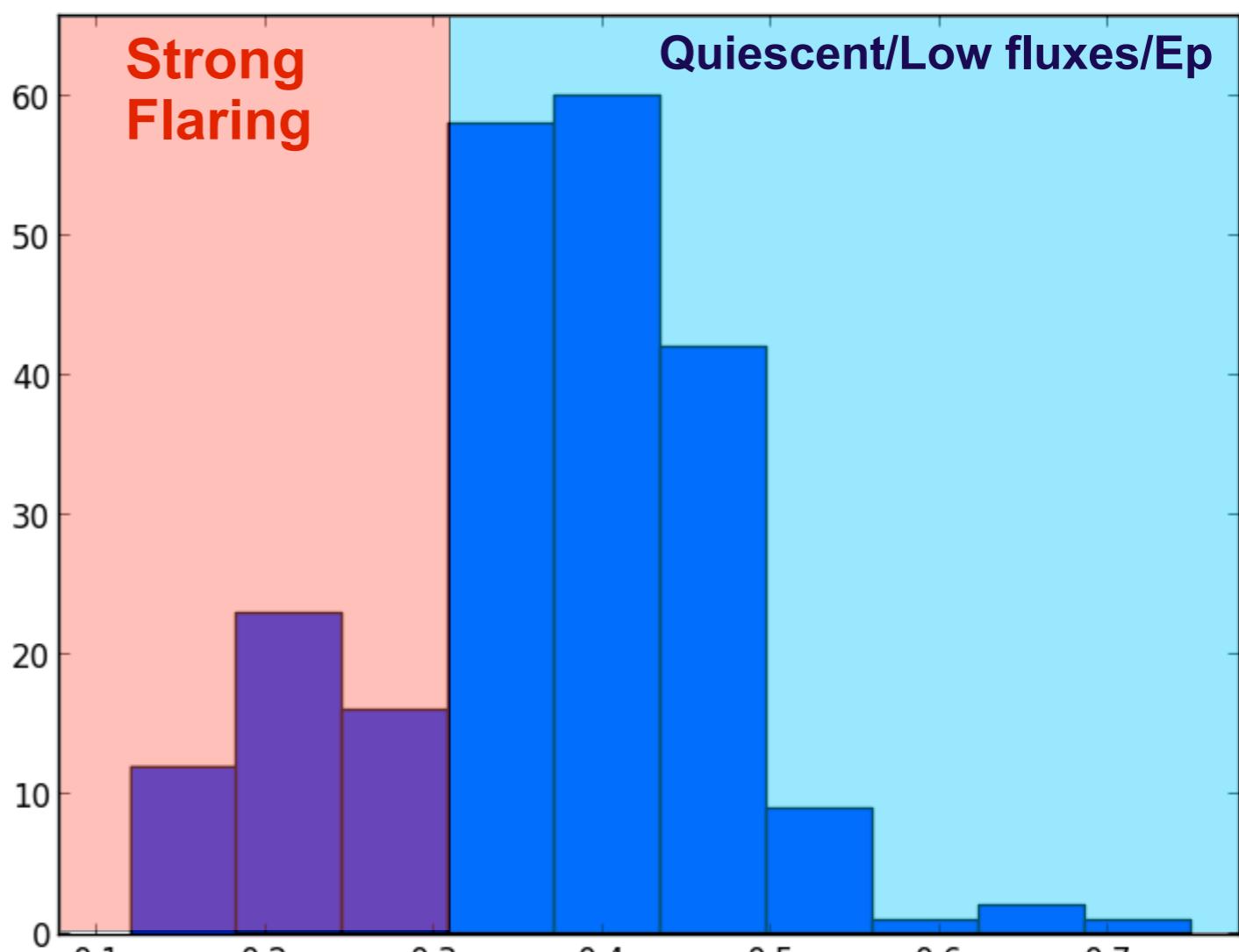
log-parabolic shape natural consequence of dispersion



b distributions and q



both flaring and quiescent seem to be far from equilibrium b eq. $\sim[0.7-1.0]$ (if full KN or S)



compatible with
q=2 far from
equilibrium
constraint on B

q=2 require more fine
tuning, especially on duration

compatible with q=5/3
constraint on B, and
duration, or TH/KN

self-consistent approach: acc+cooling

$$t_D = \frac{1}{D_{p0}} \left(\frac{\gamma}{\gamma_0} \right)^{2-q}$$

$$t_{DA} = \frac{1}{2D_{p0}} \left(\frac{\gamma}{\gamma_0} \right)^{2-q}$$

observed values

$$E_{p1}/E_{p2} \sim 5$$

$\Delta t \sim \text{few ks}$

values compatible with
Tammi & Duffy 2009

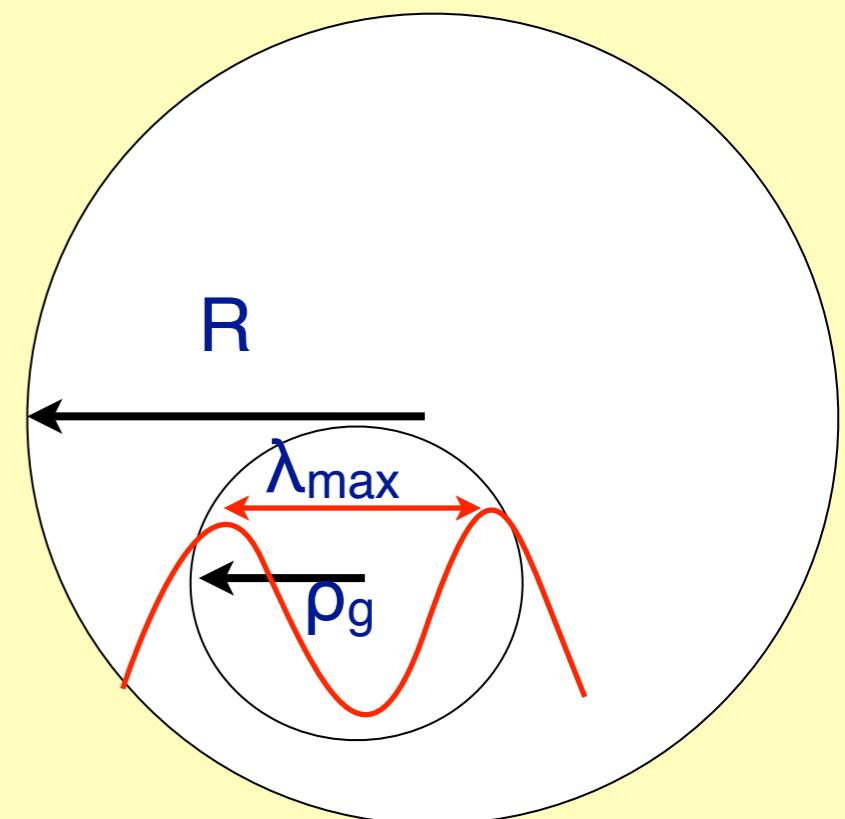
$$t_{DA} \sim < 5 \text{ ks}$$

$$t_D \sim < 10 \text{ ks}$$

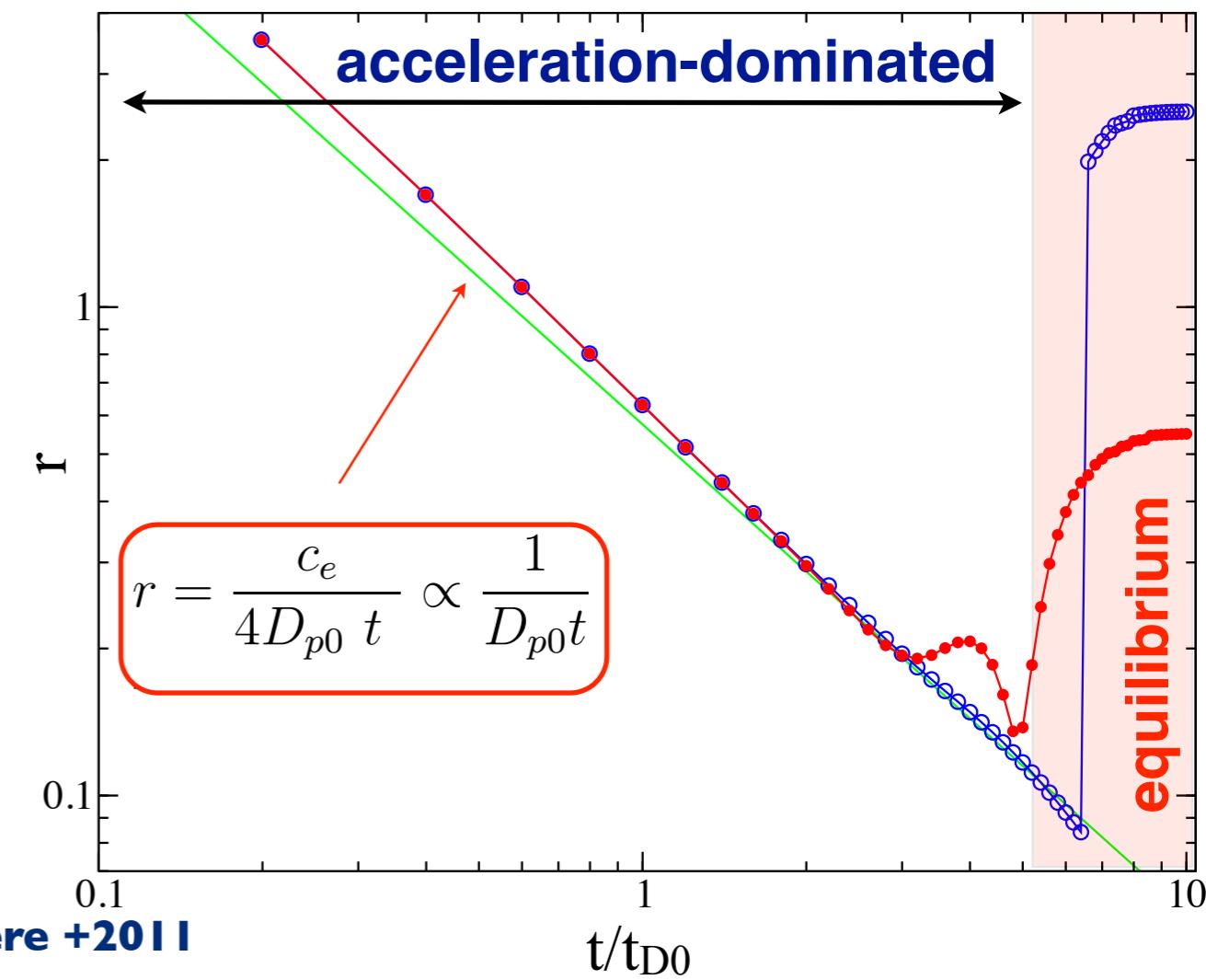
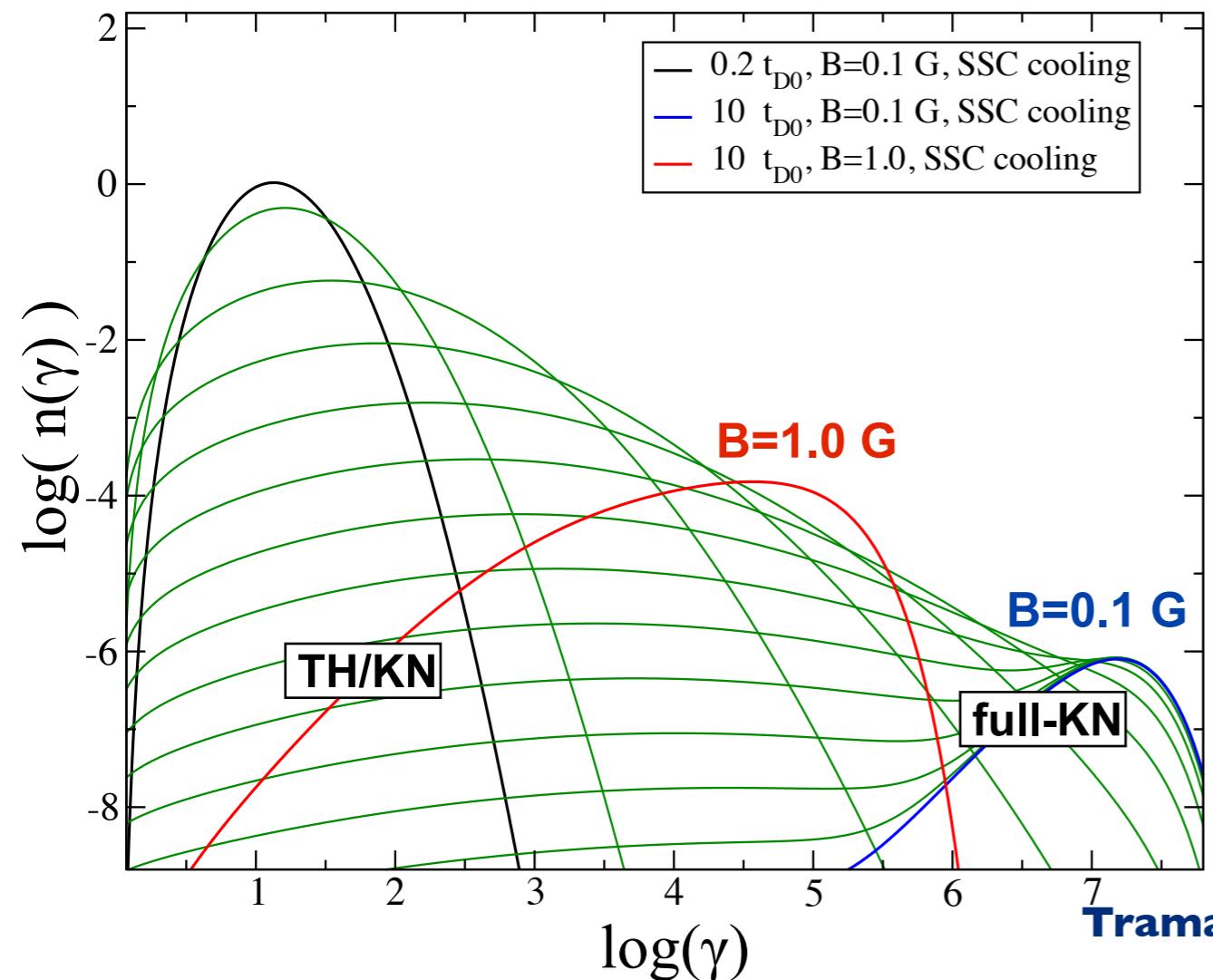
set-up of the accelerator

- $R \sim 10^{13}-10^{15} \text{ cm}$
- $\delta B/B \ll 1$, $B \sim [0.01-1.0] \text{ G}$
- $\beta_A \sim 0.1-0.5$
- $\lambda_{\max} < R \Rightarrow \sim 10^{[9-15]} \text{ cm}$
- $\rho_g < \lambda_{\max} \Rightarrow \gamma_{\max} \sim 10^{7.5}$

$$\rightarrow t_D \sim < 10^4 \text{ ks}$$



Flare: acc.-dominated-vs-equil., R= 10^{15} cm, q=2

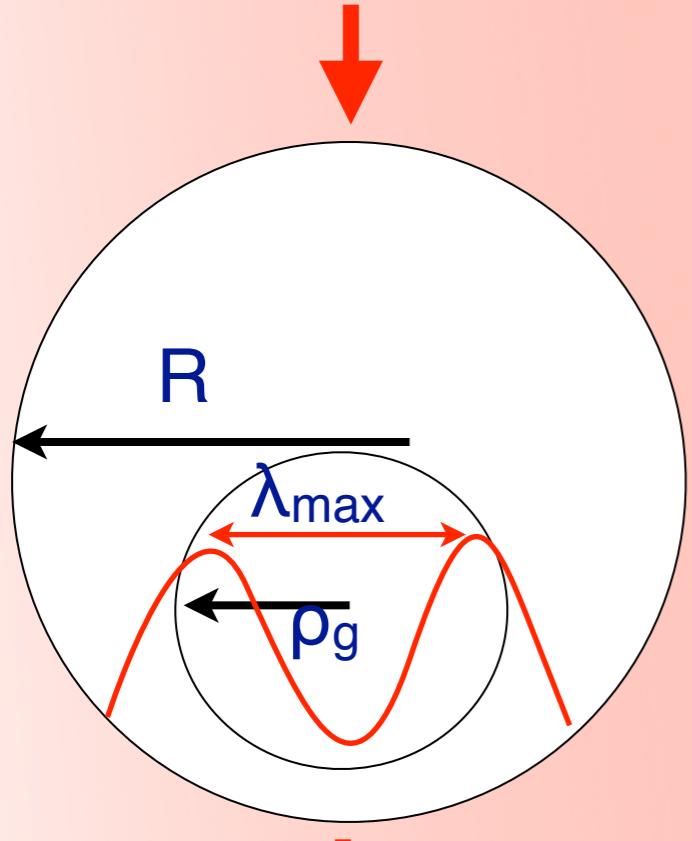


- mono energetic inj., $t_{\text{inj}} \ll t_{\text{acc}}$, $t_{\text{inj}} \ll t_{\text{sim}}$
- we measure r @peak as a function of the time
- two phase: **acceleration-dominated**, **equilibrium**
- equil. distribution:
 - **f=1 for q=2 and S, full TH, or full KN**
 - **equil. curv.: $r \sim 2.5$, ($r_{3p} \sim 6.0$) for TH or full KN**
 - **equil. curv.: $r \sim 0.6$, ($r_{3p} \sim 4.0$) for TH-KN**

$$n(\gamma) \propto \gamma^2 \exp \left[\frac{-1}{f(q, \dot{\gamma})} \left(\frac{\gamma}{\gamma_{eq}} \right)^{f(q, \dot{\gamma})} \right]$$

Jet

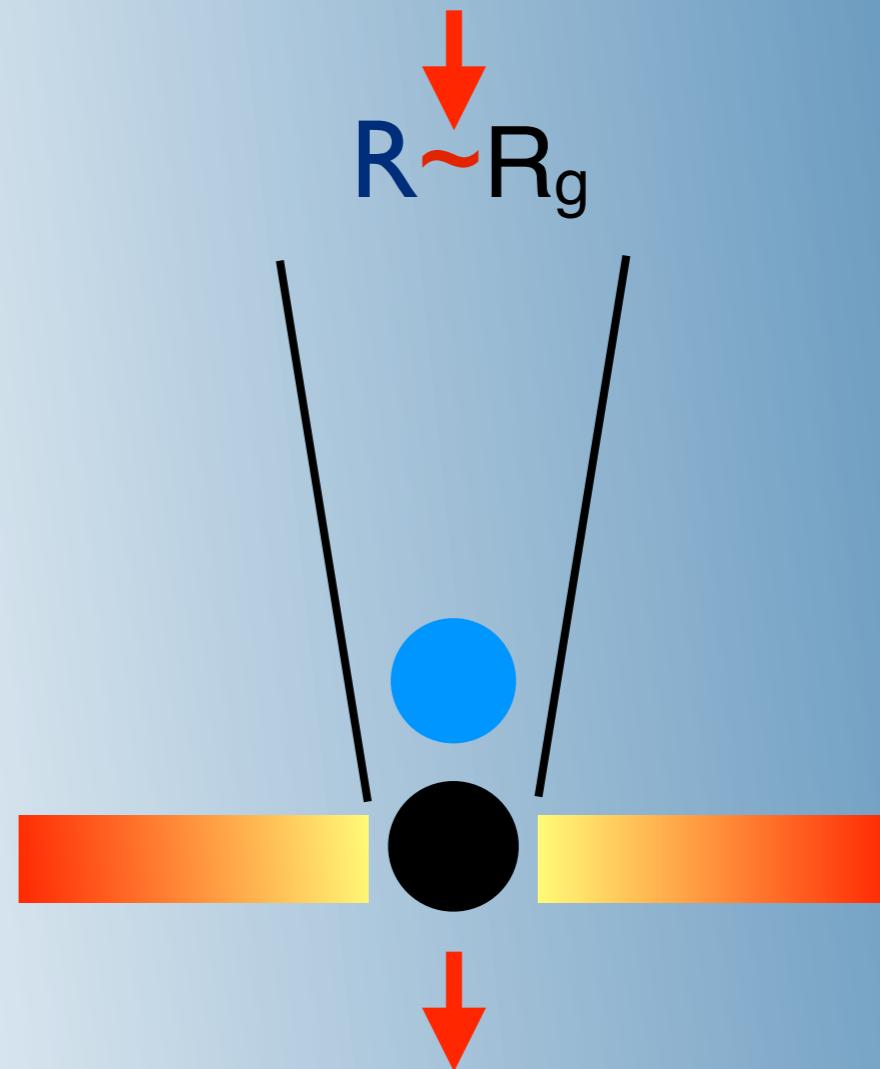
$$R \leq c \Delta t \delta / (1+z)$$



- γ - γ transparency
- B
- γ_{\max}

BH

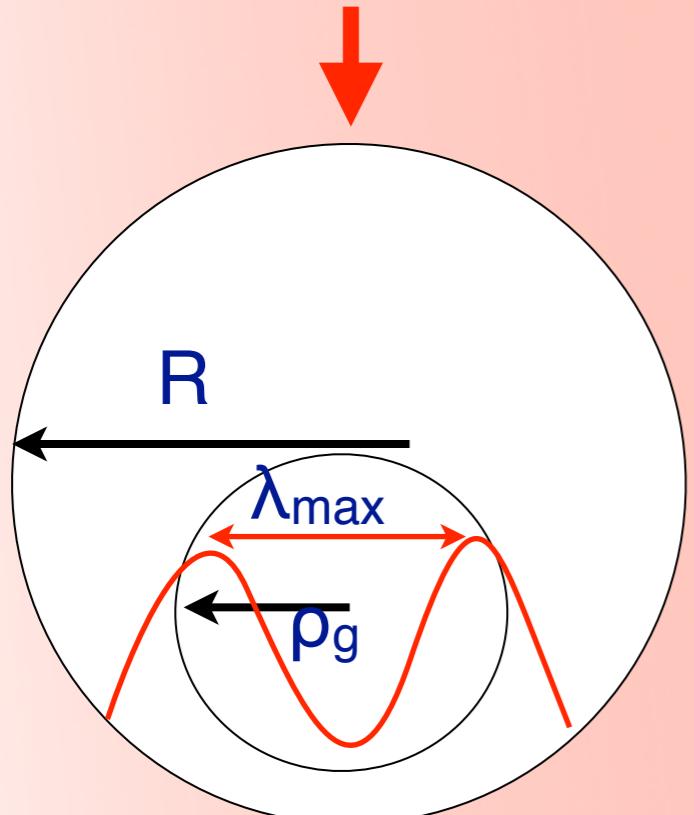
$$R \leq c \Delta t / (1+z)$$



- M_{BH}
- disk/jet feeding

Jet

$$R \leq c \Delta t \delta / (1+z)$$

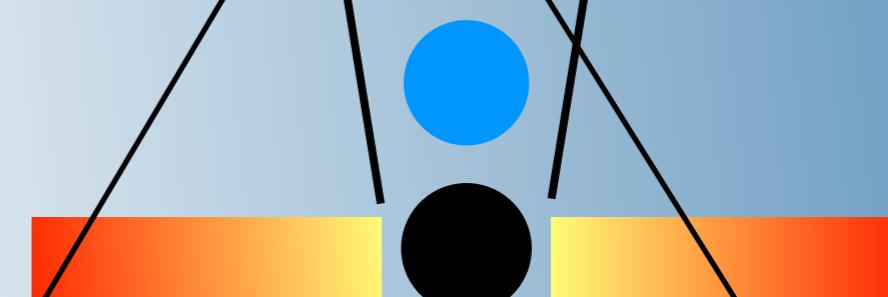


- γ - γ transparency
- B
- γ_{\max}

BH

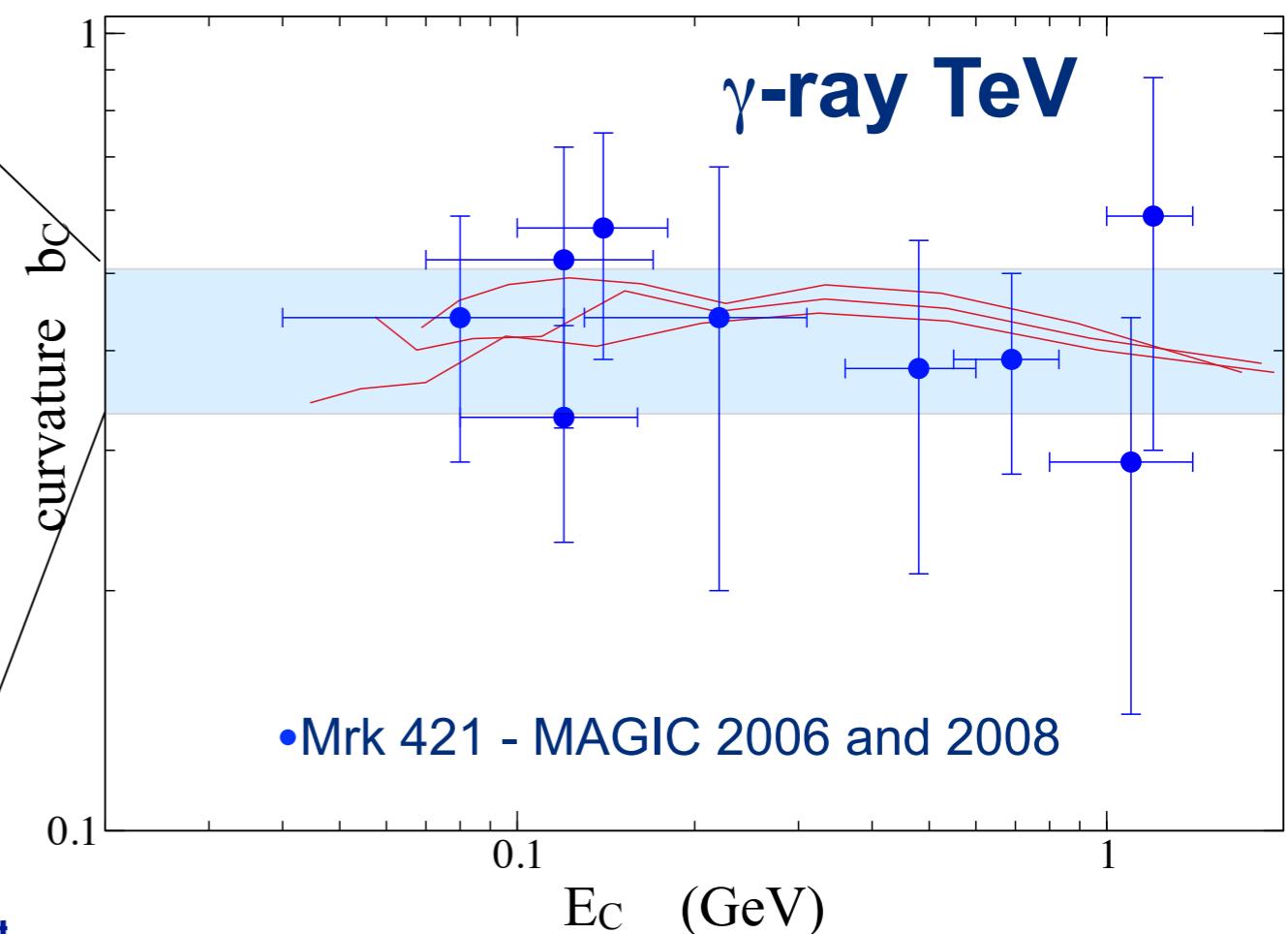
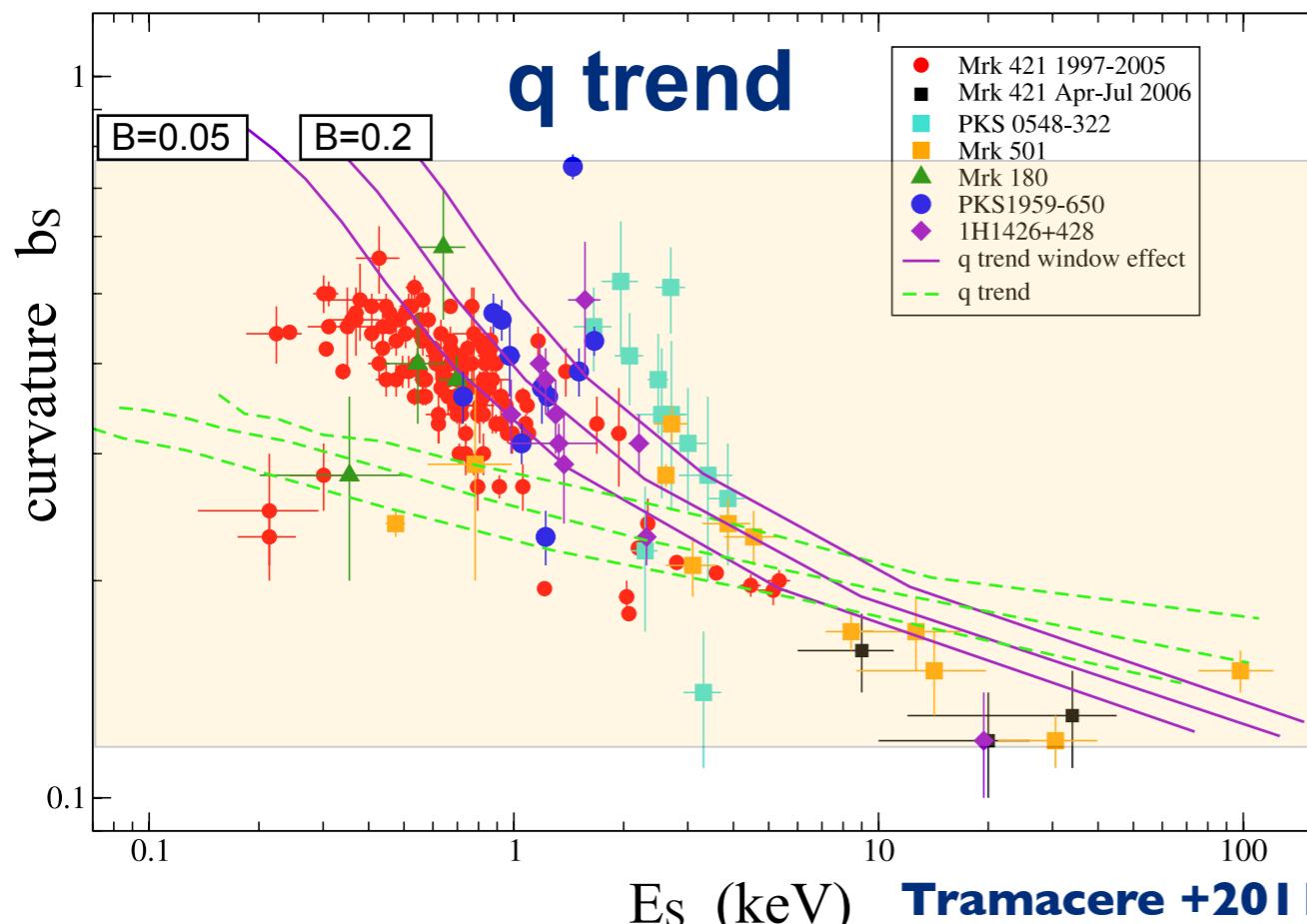
$$R \leq c \Delta t \delta / (1+z)$$

$$R \sim R_g$$



- M_{BH}
- disk/jet feeding

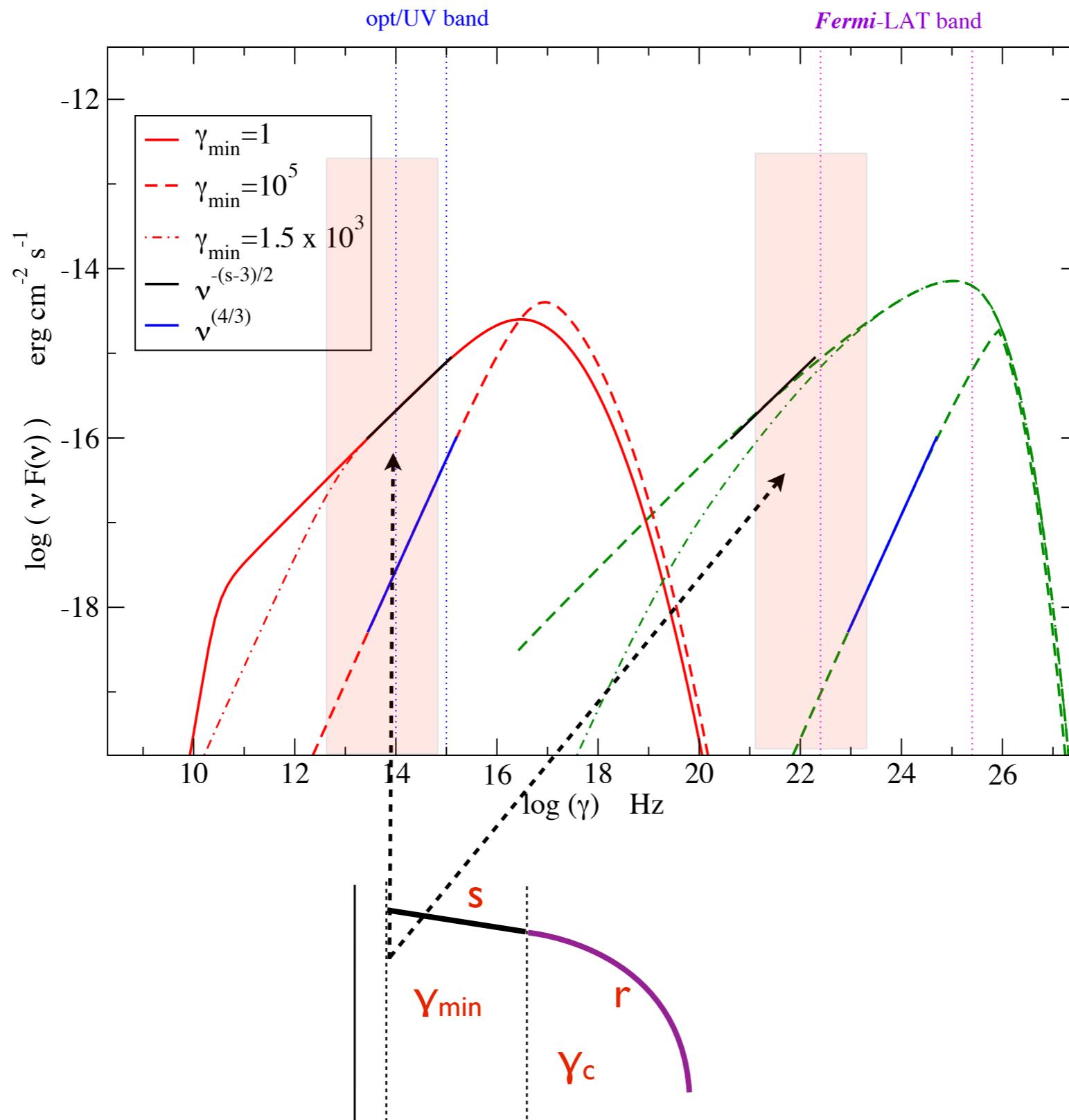
E_s - b_s X-ray trend and γ -ray predictions



- data span **13 years**, both flaring and quiescent states
- We are able to reproduce these long-term behaviours, by changing the value of only one parameter (q)
- curvature values imply distribution far from the equilibrium ($b \sim [0.7-1.0]$)
- More data needed at GeV/TeV, curvature seems to be cooling-dominated

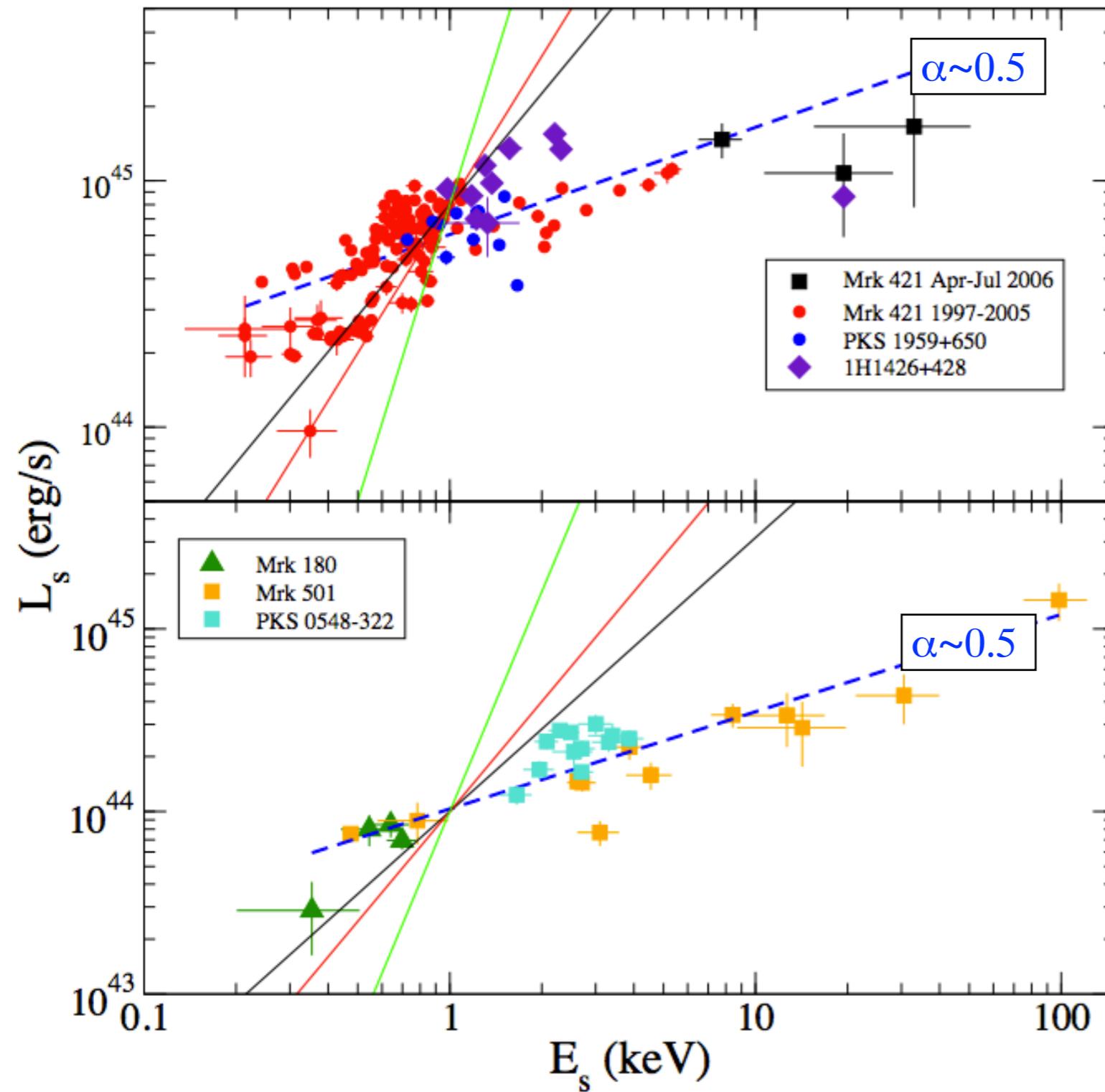
L_{inj} (E_s - b_s trend) (erg s $^{-1}$)	5×10^{39}
L_{inj} (E_s - L_s trend) (erg s $^{-1}$)	$5 \times 10^{38}, 5 \times 10^{39}$
q	[3/2, 2]
t_A	(s)
$t_{D_0} = 1/D_{P0}$	(s)
T_{inj}	(s)
T_{esc}	(R/c)

HBLs case



acceleration signature in the Es-vs-Ls trend

long-trend main drivers

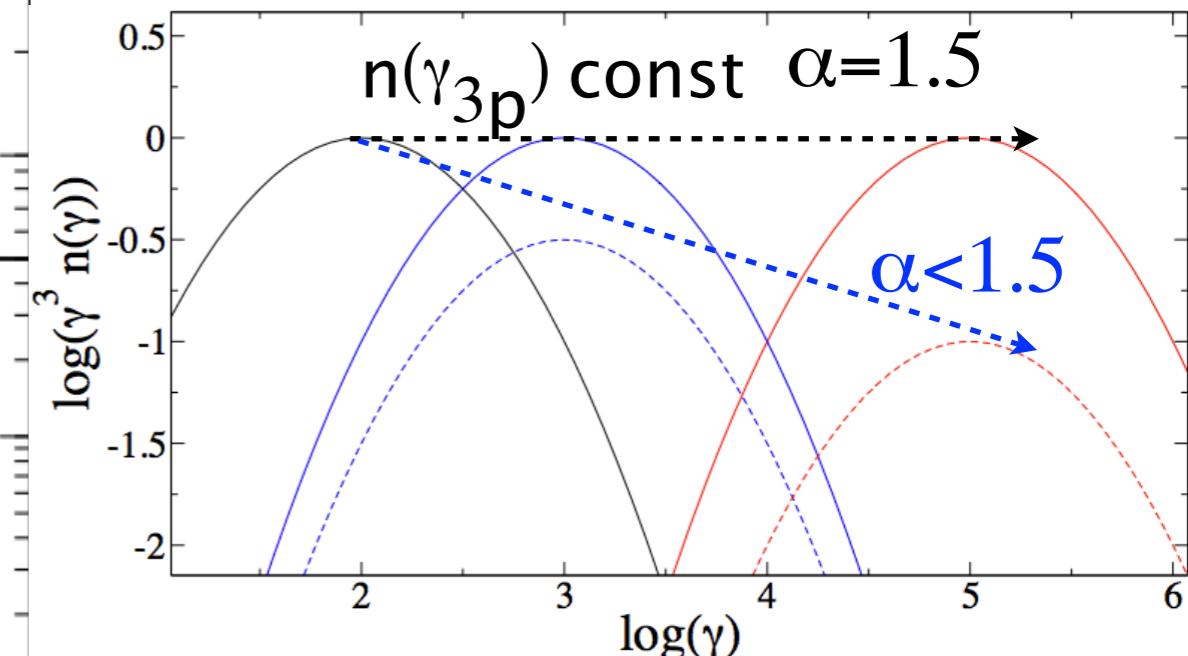


Tramacere+2009

$$S_s(E_s) \propto n(\gamma_{3p}) \gamma_{3p}^3 B^2 \delta^4$$

$$E_s \propto \gamma_{3p}^2 B \delta.$$

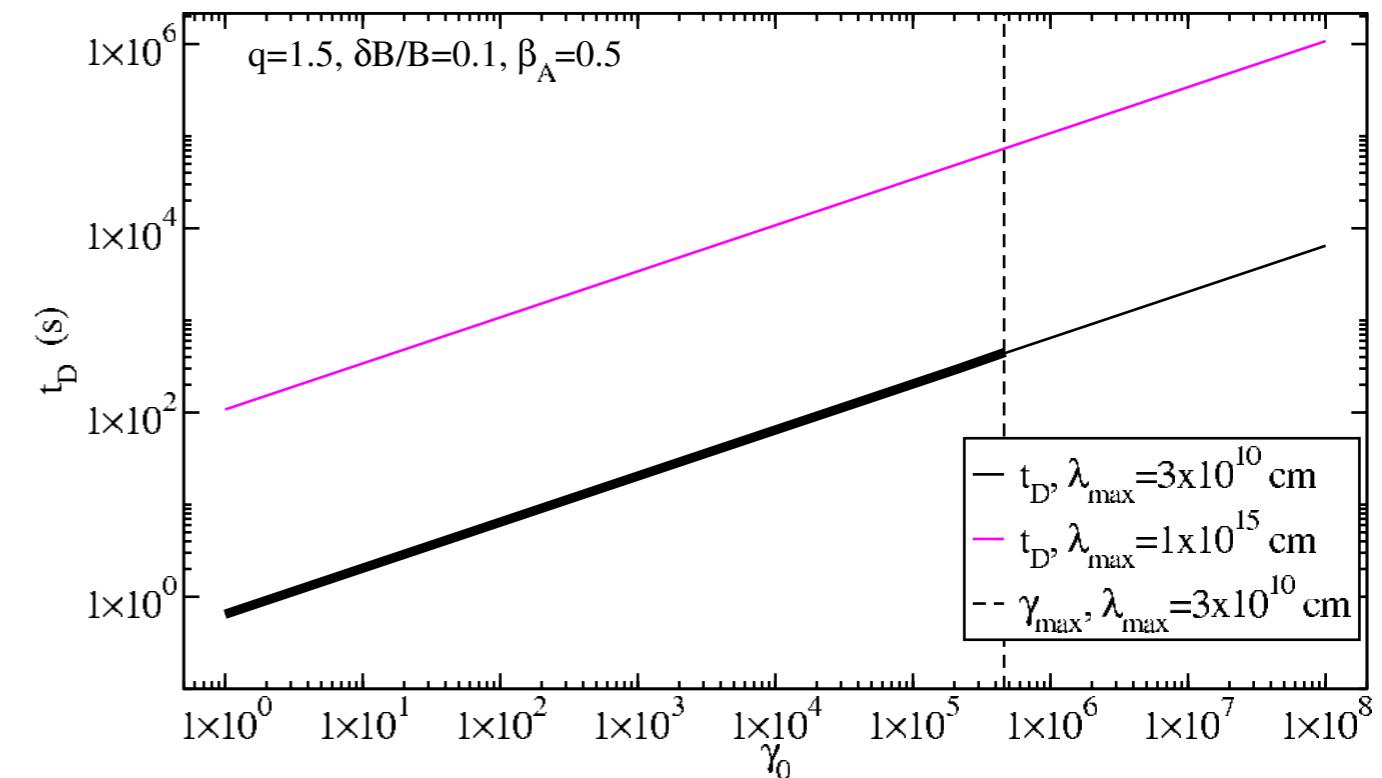
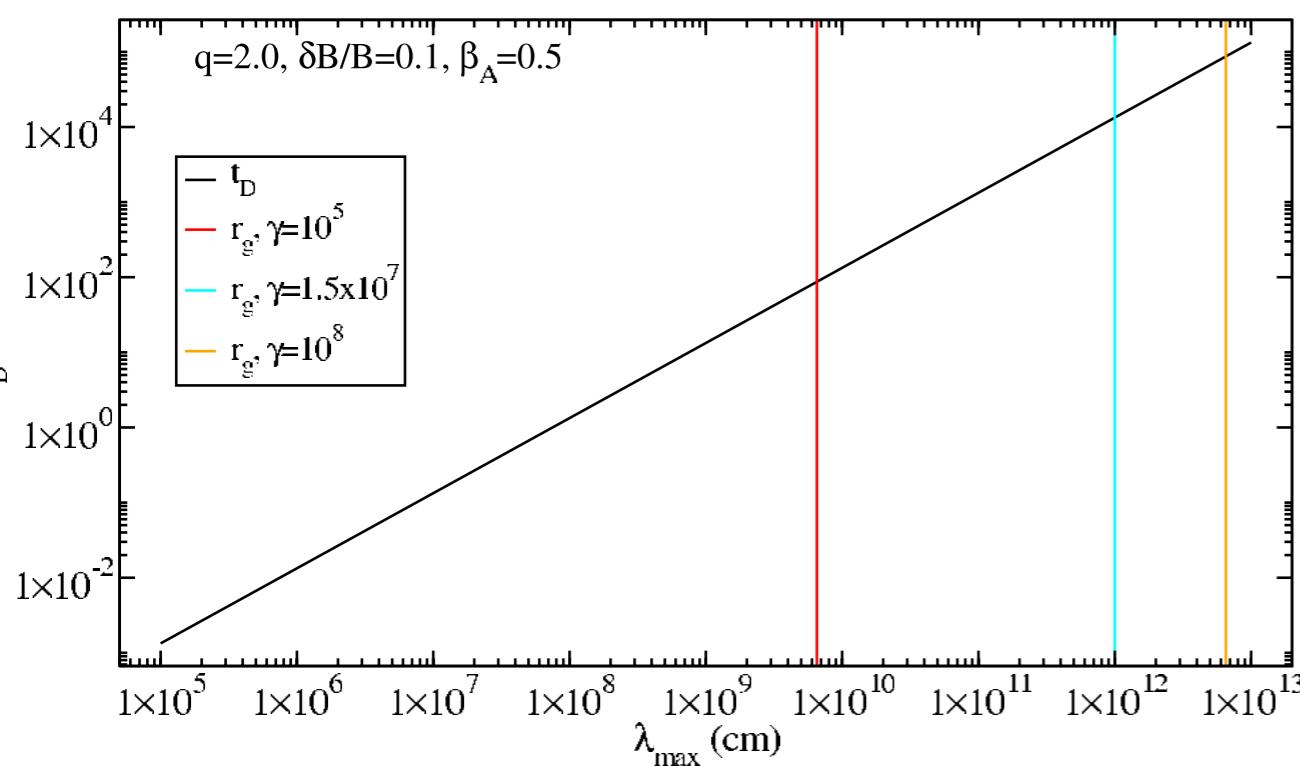
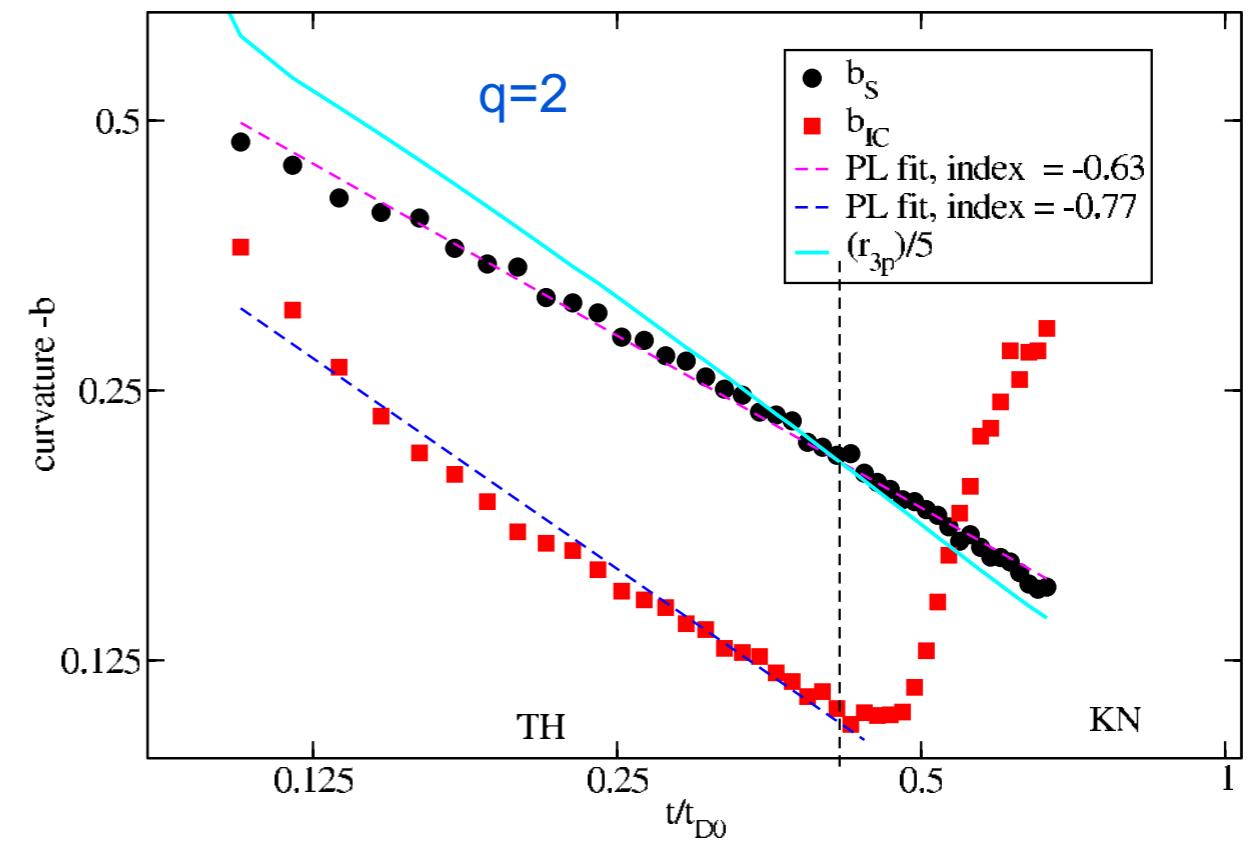
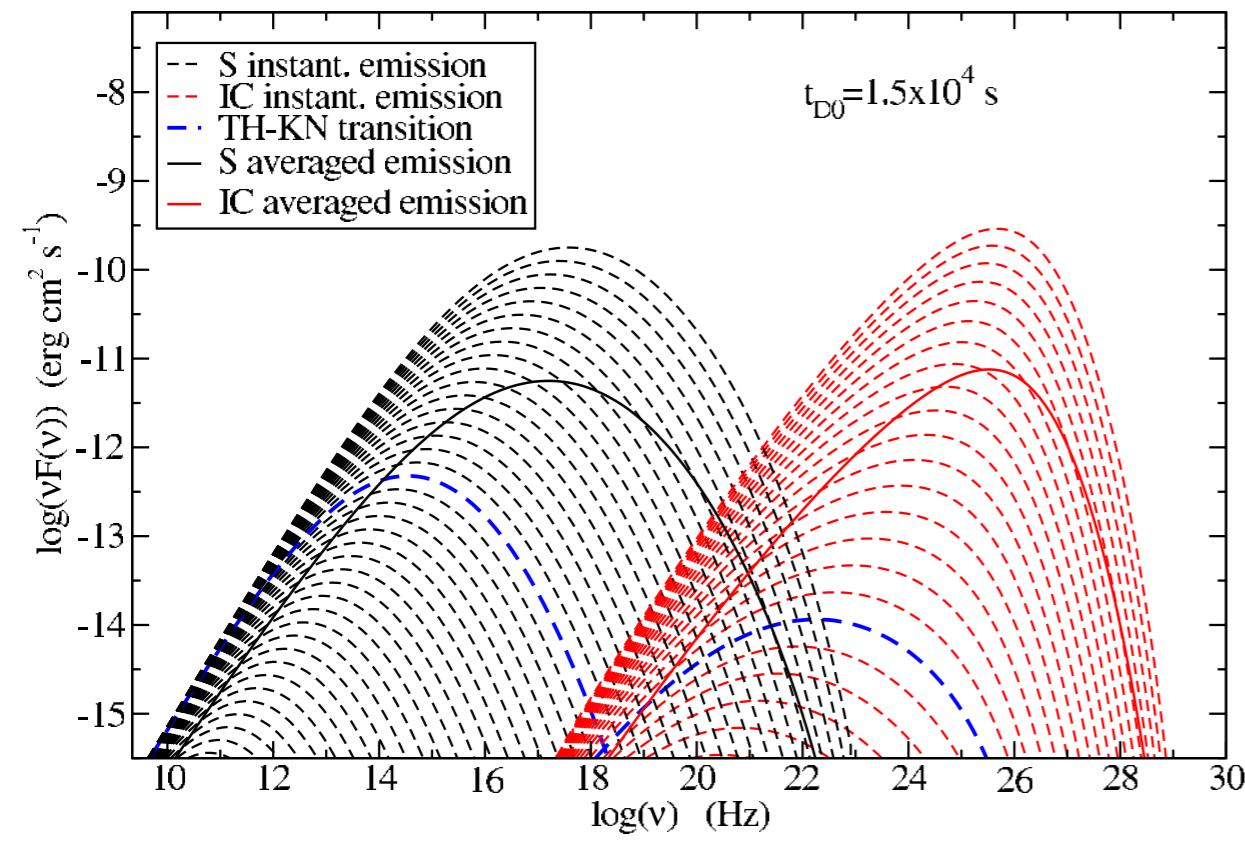
$$S_s \propto (E_s)^\alpha$$

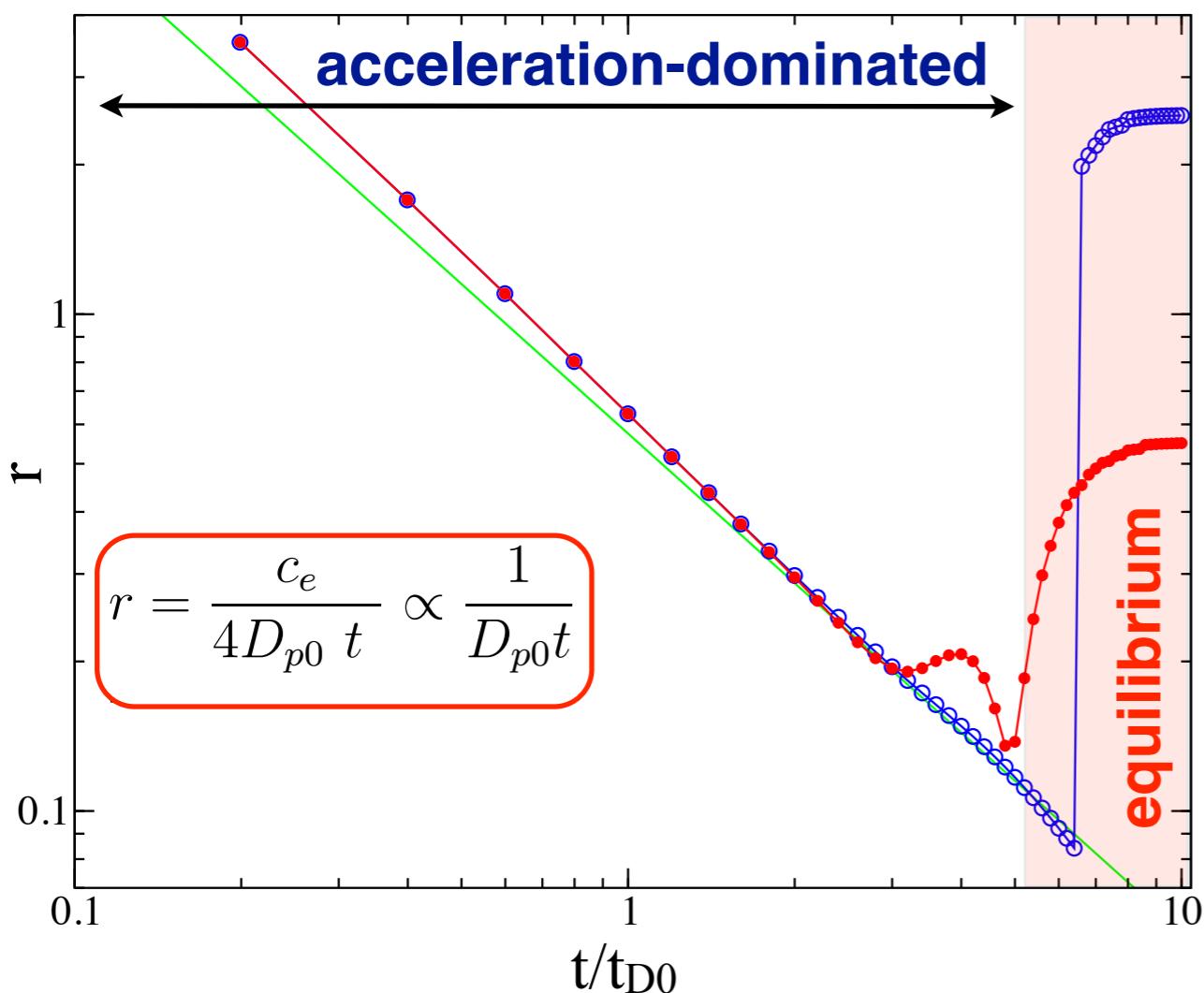


• $\gamma_{3p} \uparrow$ and $n(\gamma_{3p}) \downarrow \Rightarrow \alpha < 1.5$
acceleration+energy conservation

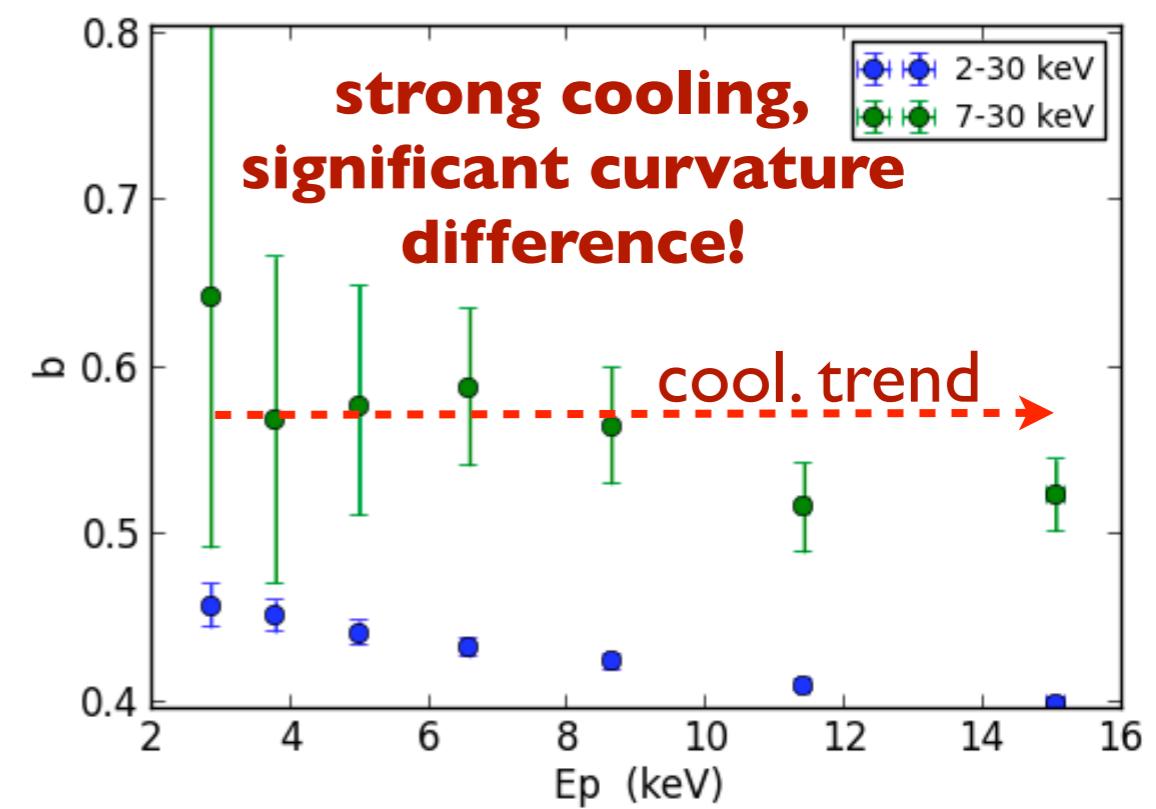
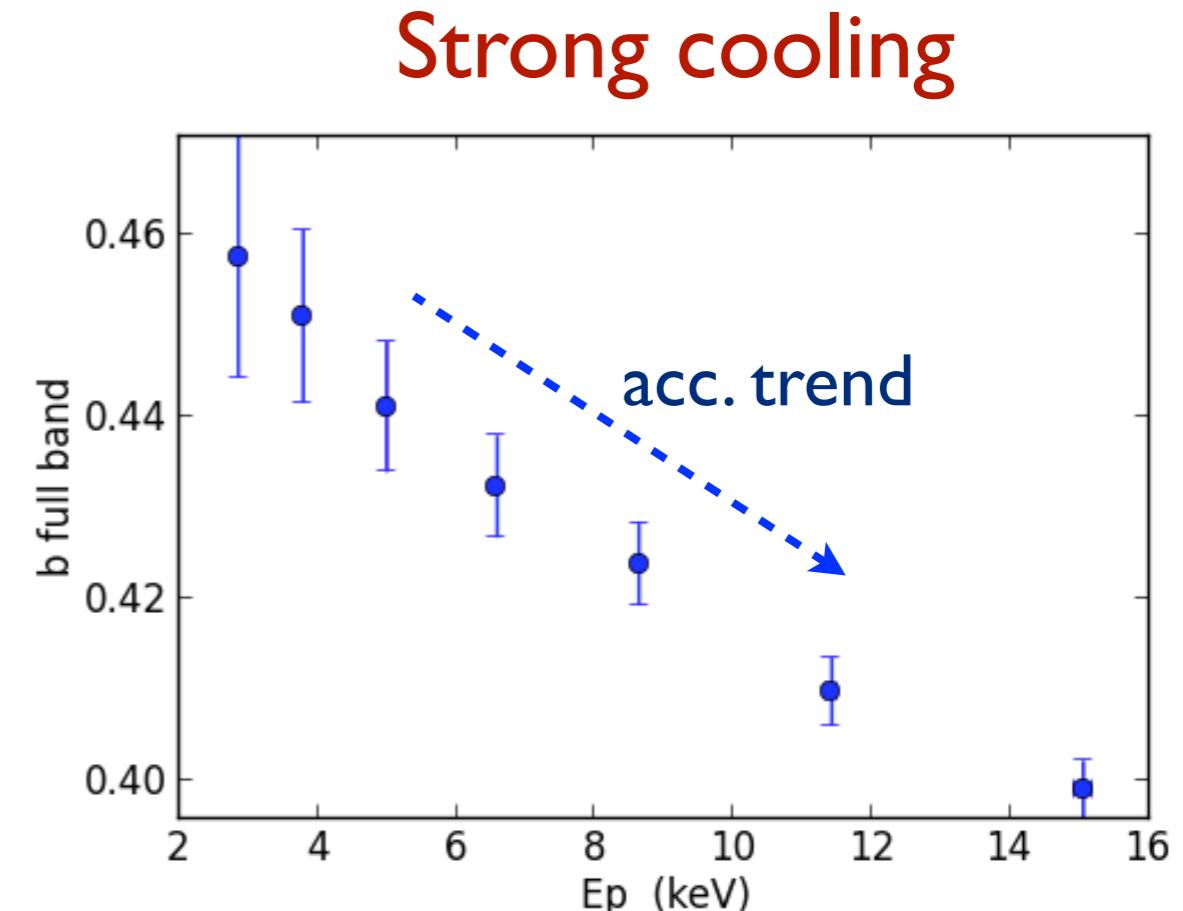
• $B \rightarrow \alpha = 2.0$, incompatible as
 • $\delta \rightarrow \alpha = 4$ long-trend main driver

SEDS evolution



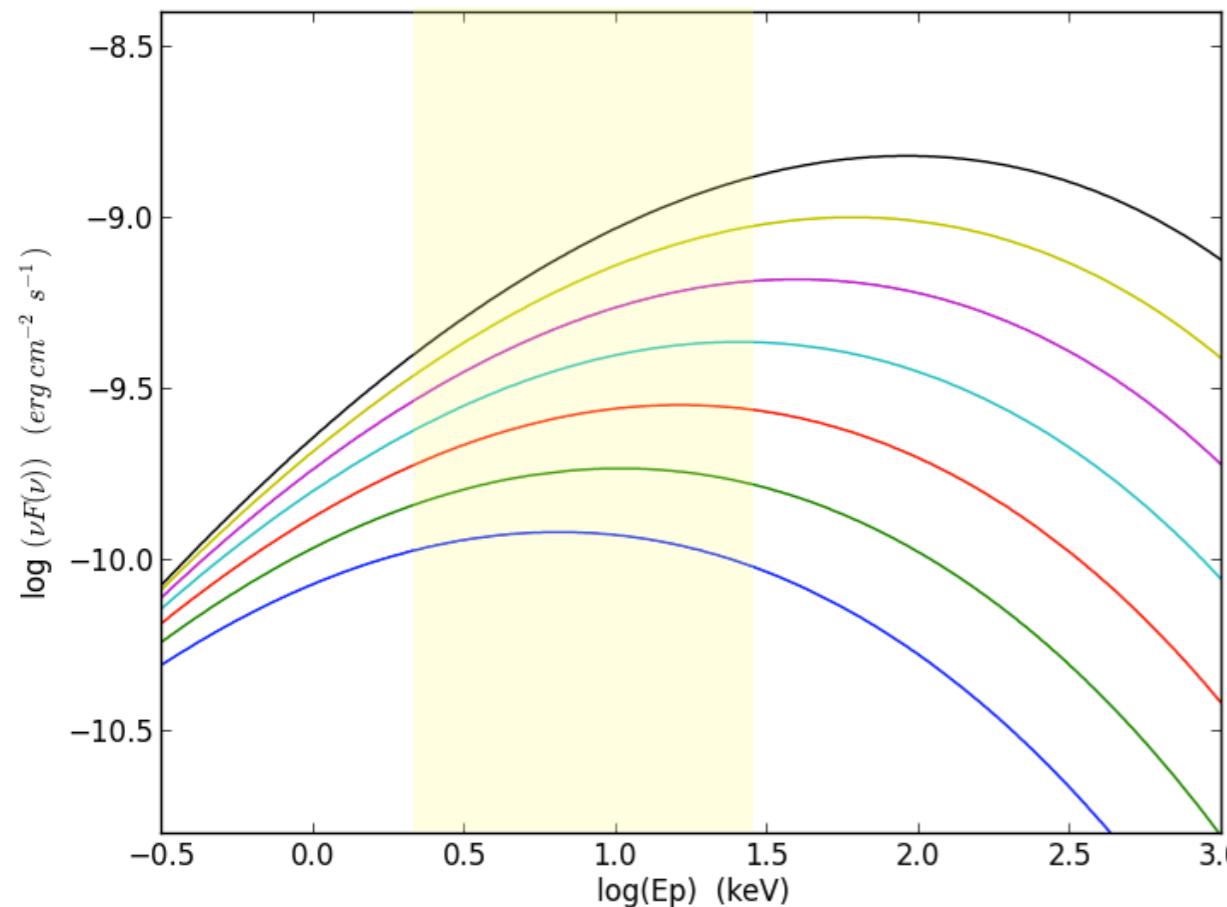


- Full bands curvature related to EED broadness, acceleration signature
- High energy band, dominated by cooling, moving towards the equilibrium

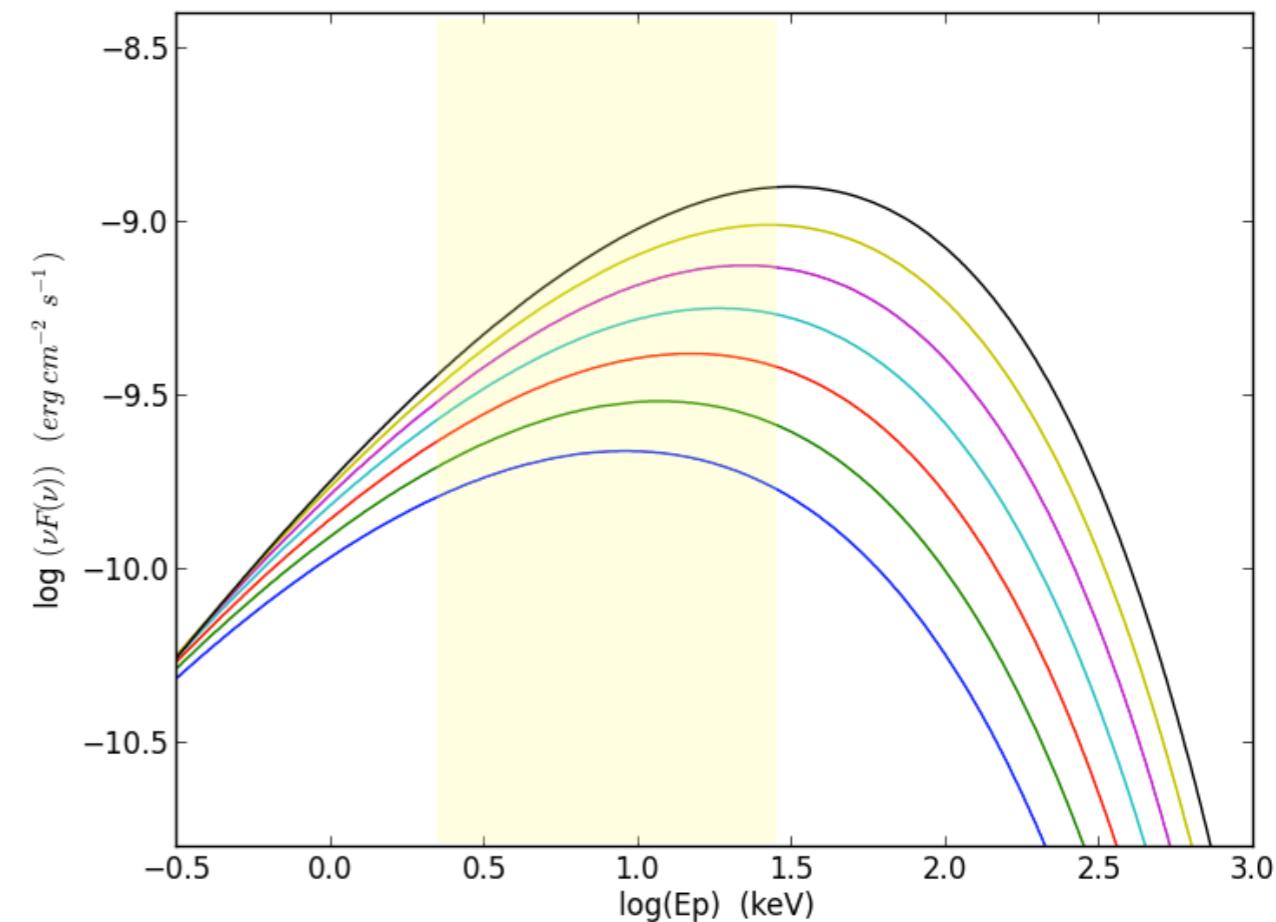


Moving Ep above 30 keV

Low cooling



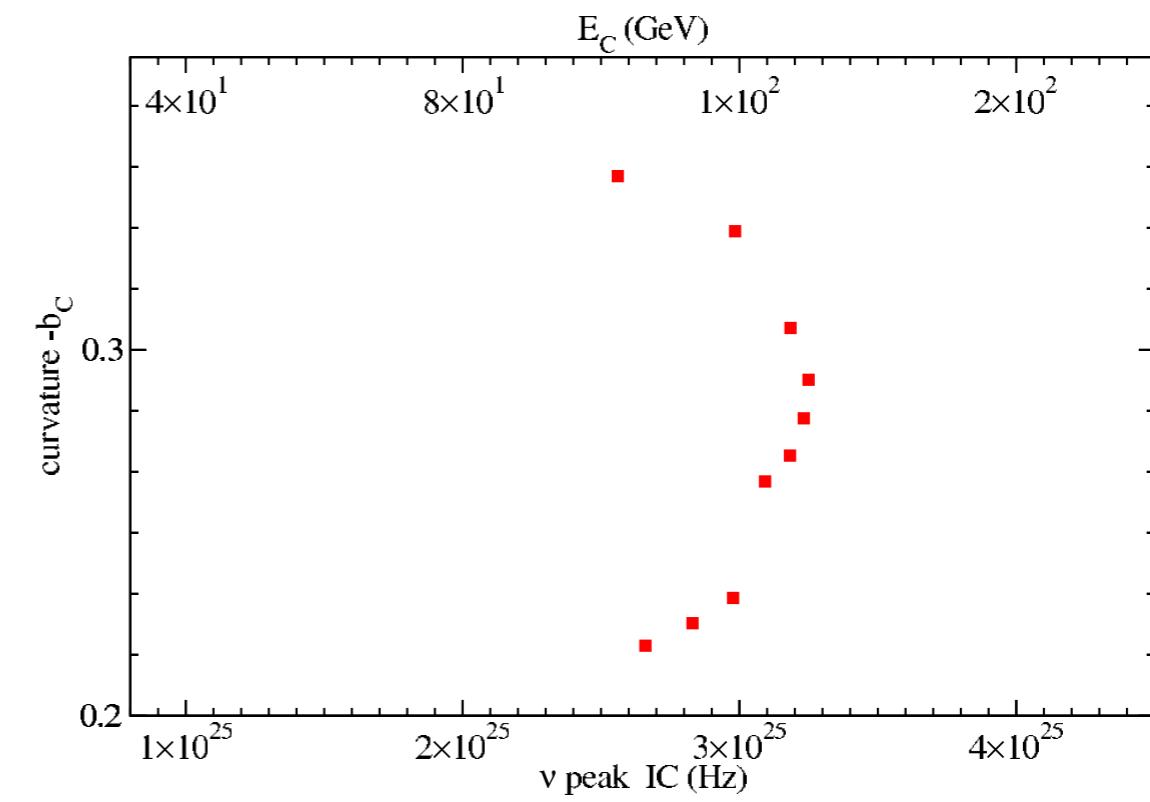
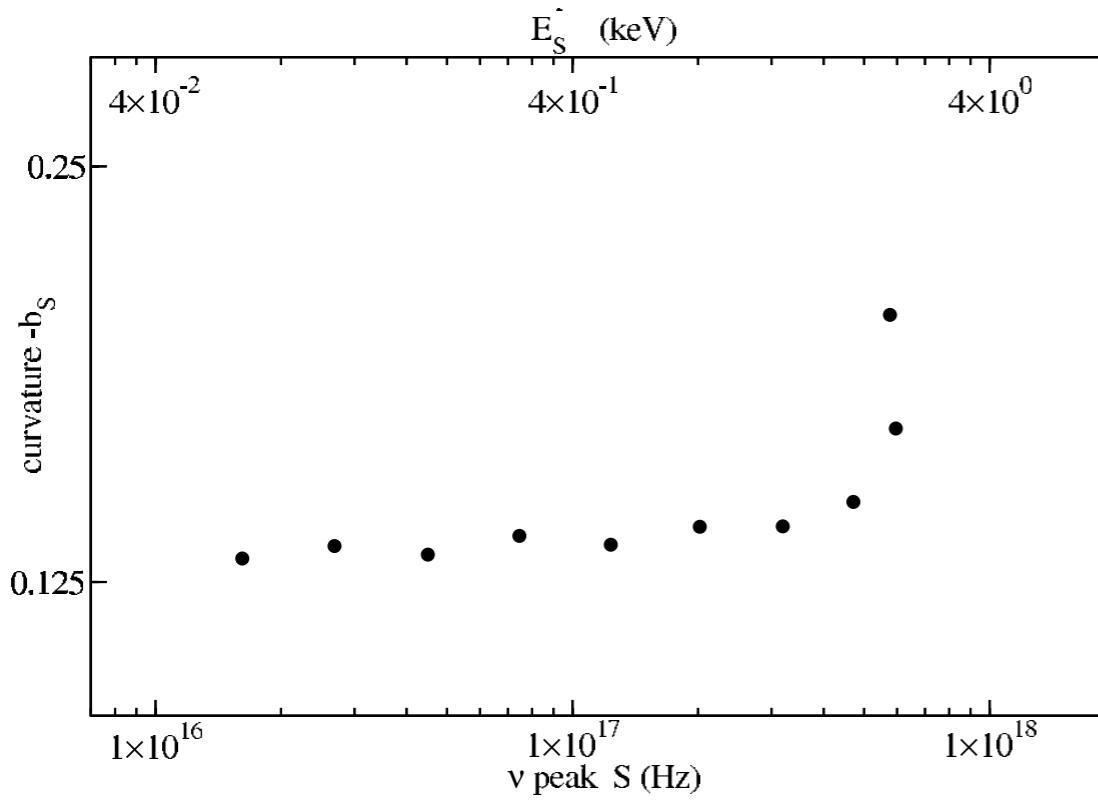
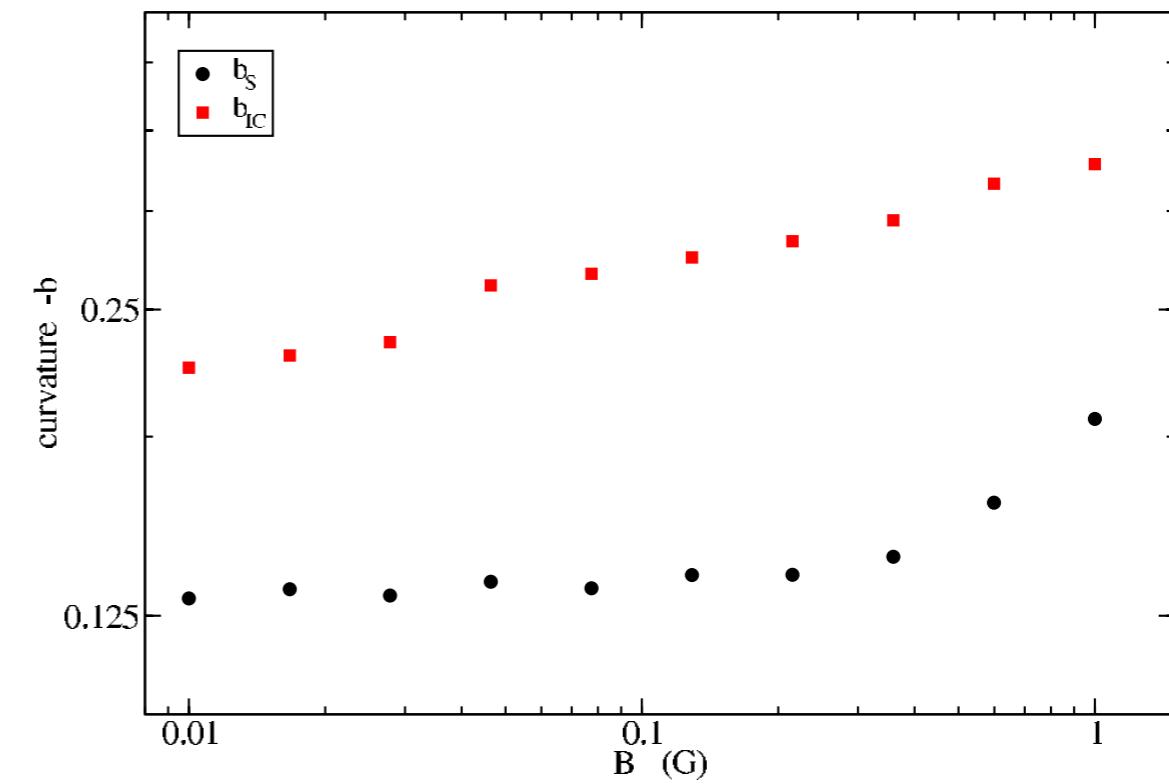
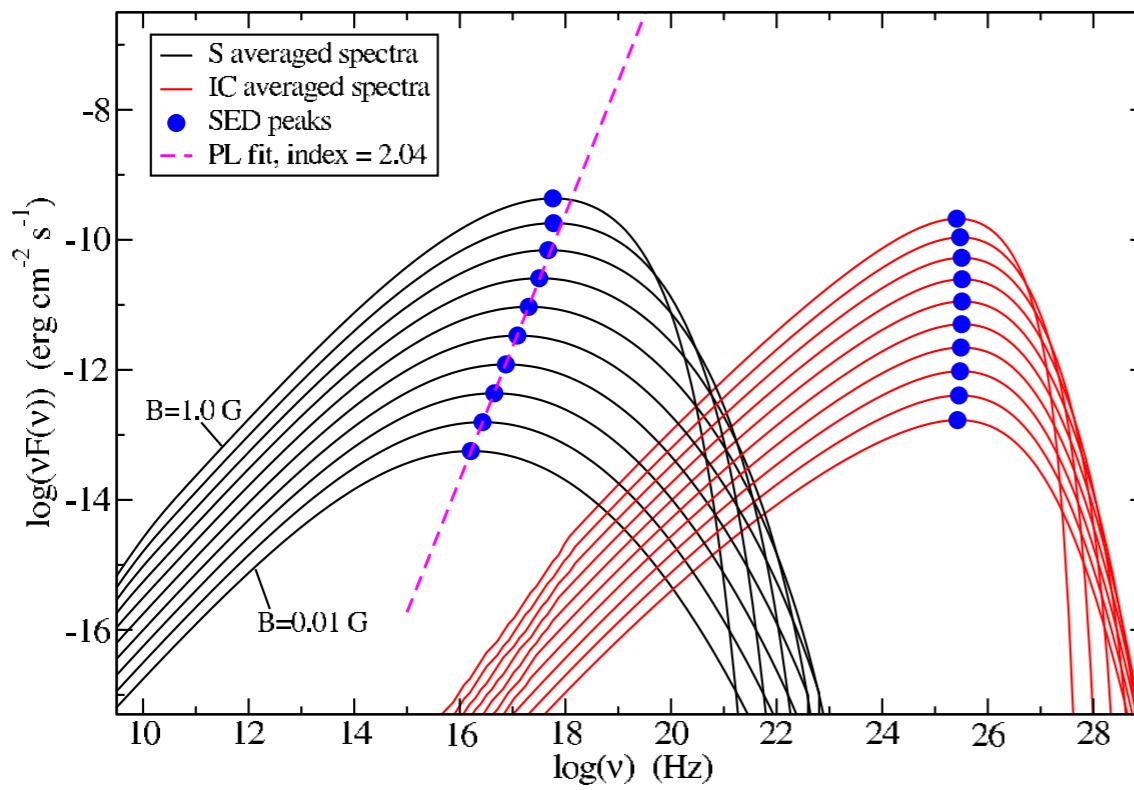
Strong cooling



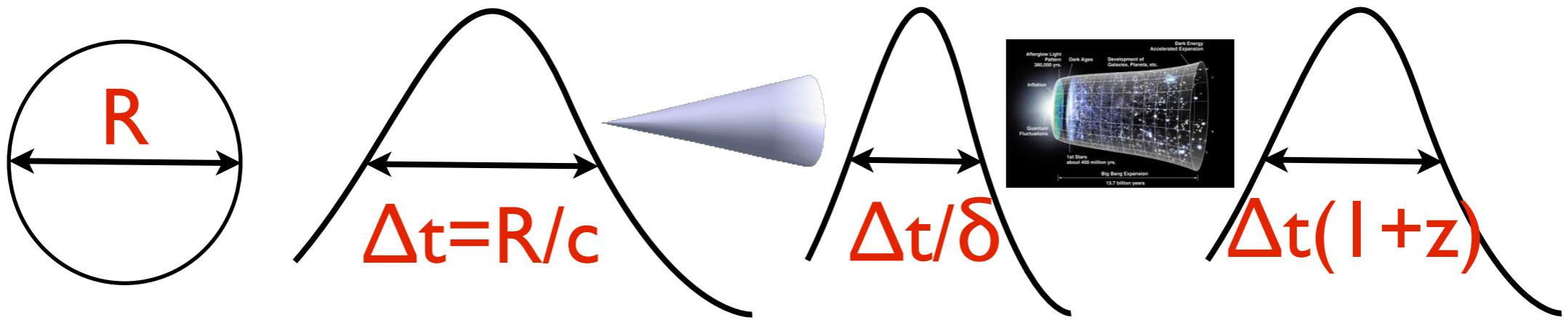
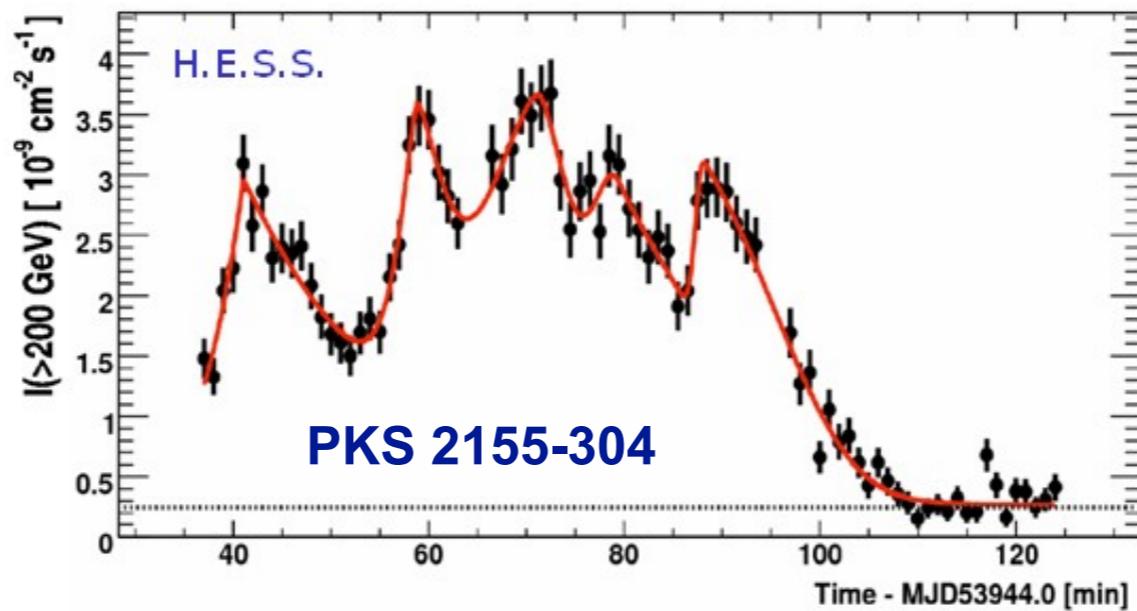
B	0.2/1.0	G
R	3×10^{15}	cm
L_{inj}	5×10^{39}	erg/s
q	2	
t_A	1.2×10^3	s
t_D	2.2×10^4	s

- SEDs are rescaled in order that the **brightest** state matches the flux of $10^{-9} \text{ erg cm}^{-2} \text{ s}^{-1}$ [2-10] keV
- during the flares, the fluxes range in $\sim 1 \times 10^{-10} - 10^{-9} \text{ erg cm}^{-2} \text{ s}^{-1}$
- **I ks integration time**

Effect o B on SEDs



Rapid Variability

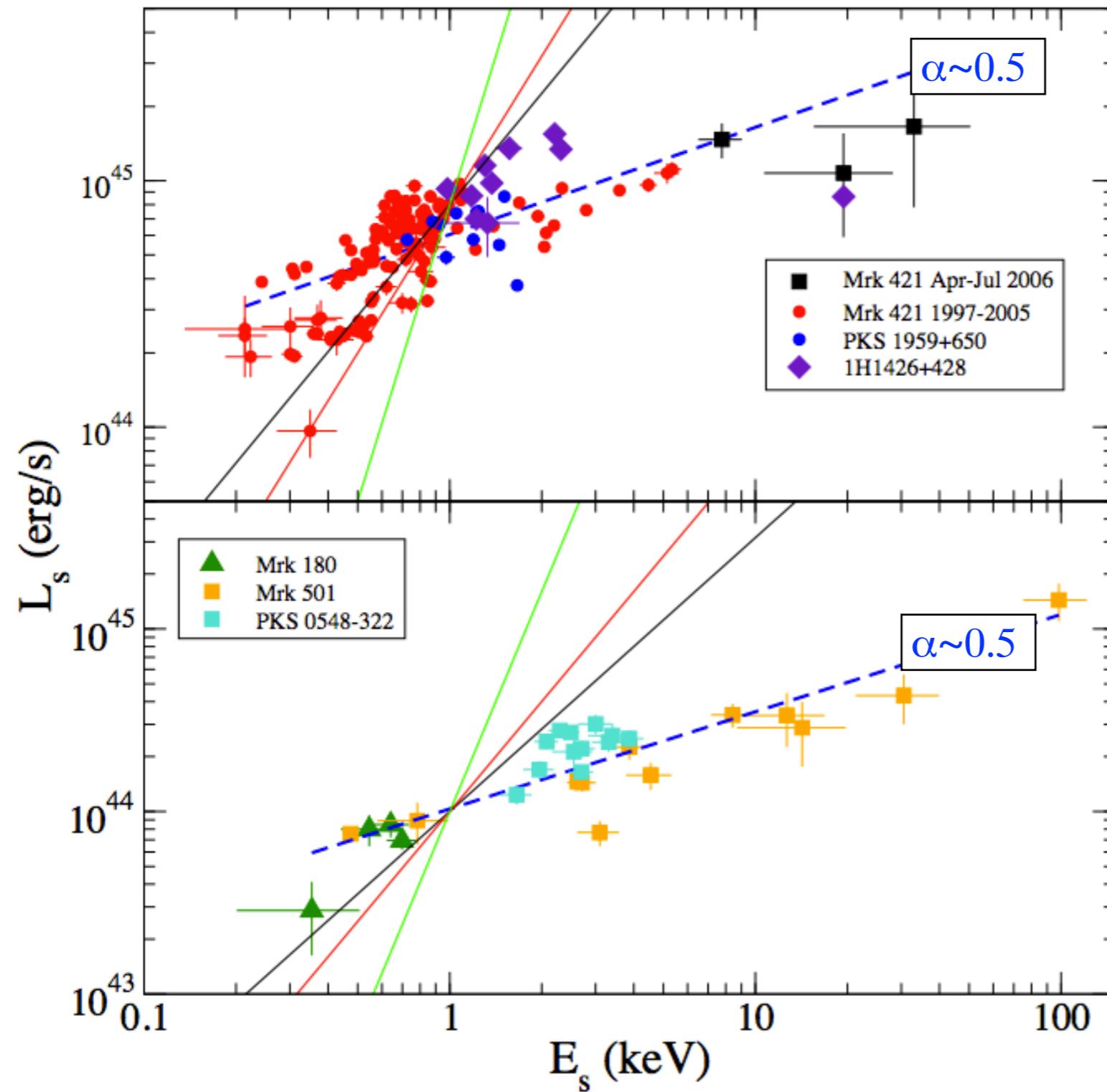


$$R \leq c \Delta t \delta / (1+z)$$

acceleration signature in the Es-vs-Ls trend

Tramacere A., et al. 2009A&A...501

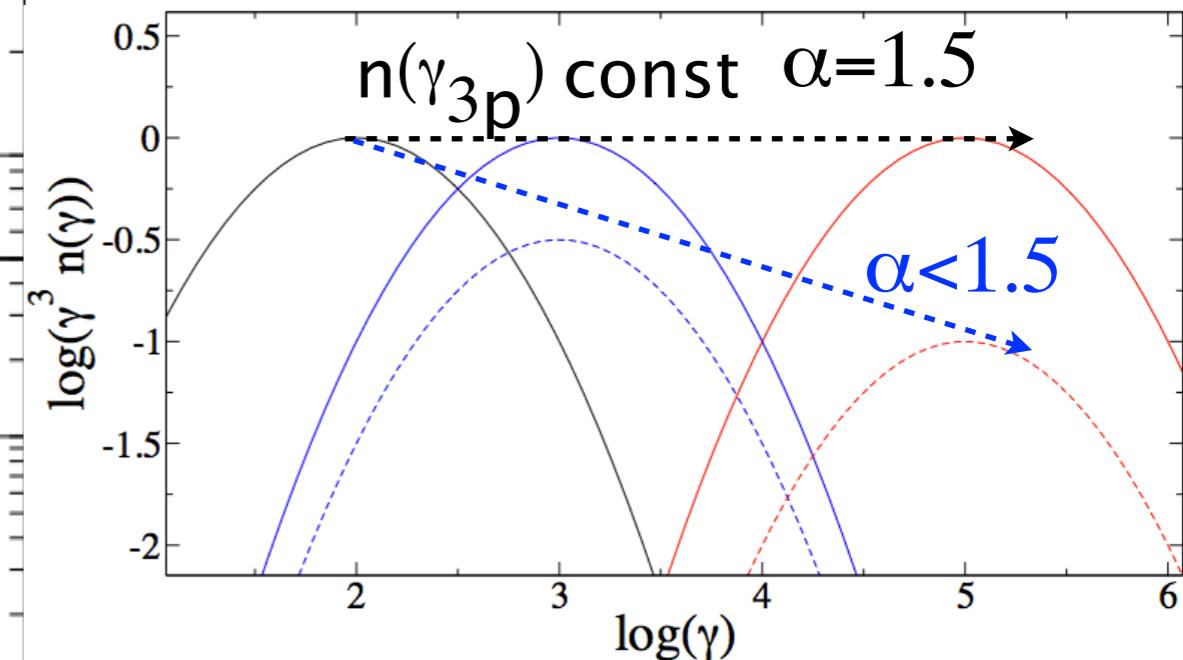
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$$S_s(E_s) \propto n(\gamma_{3p}) \gamma_{3p}^3 B^2 \delta^4$$

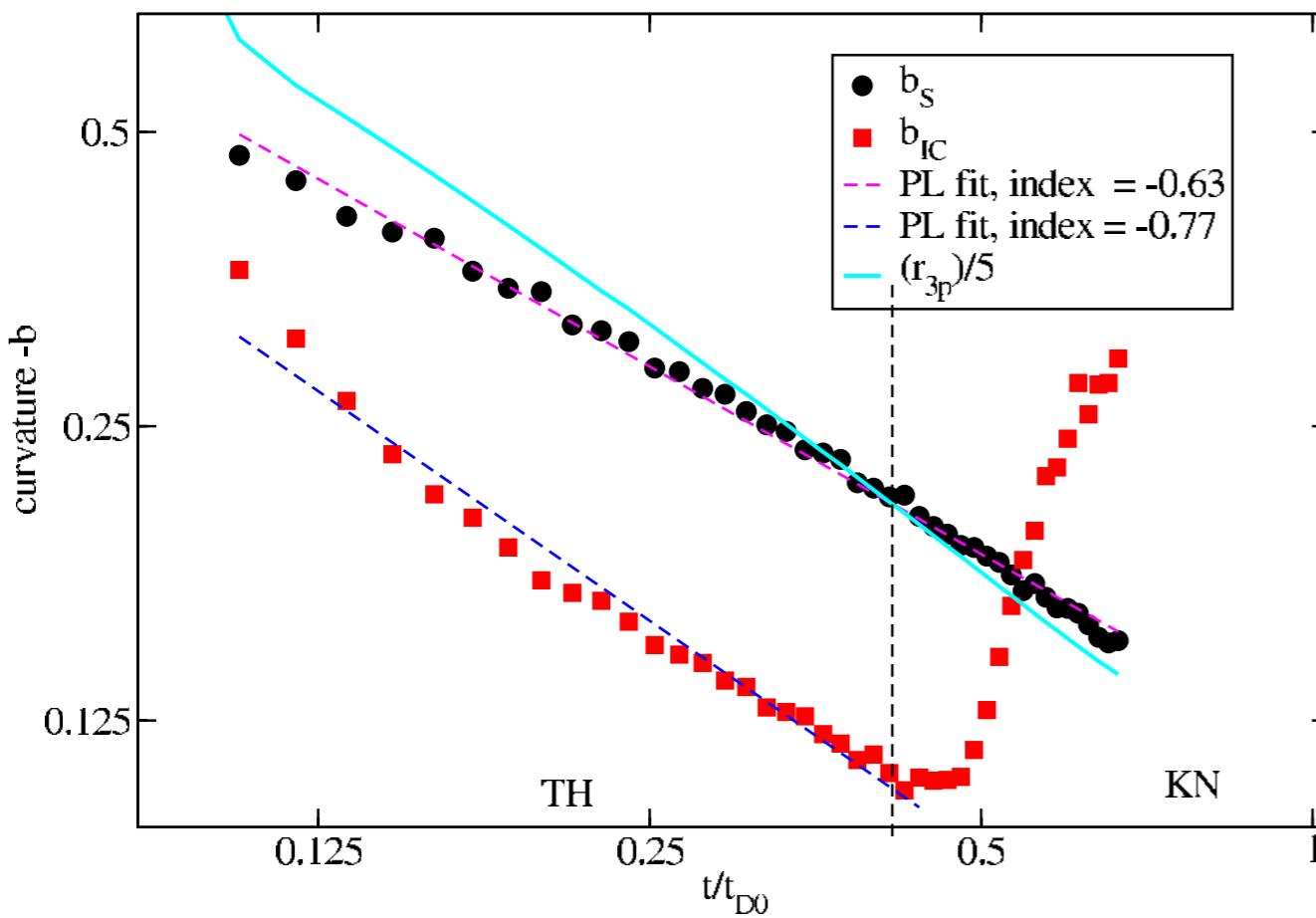
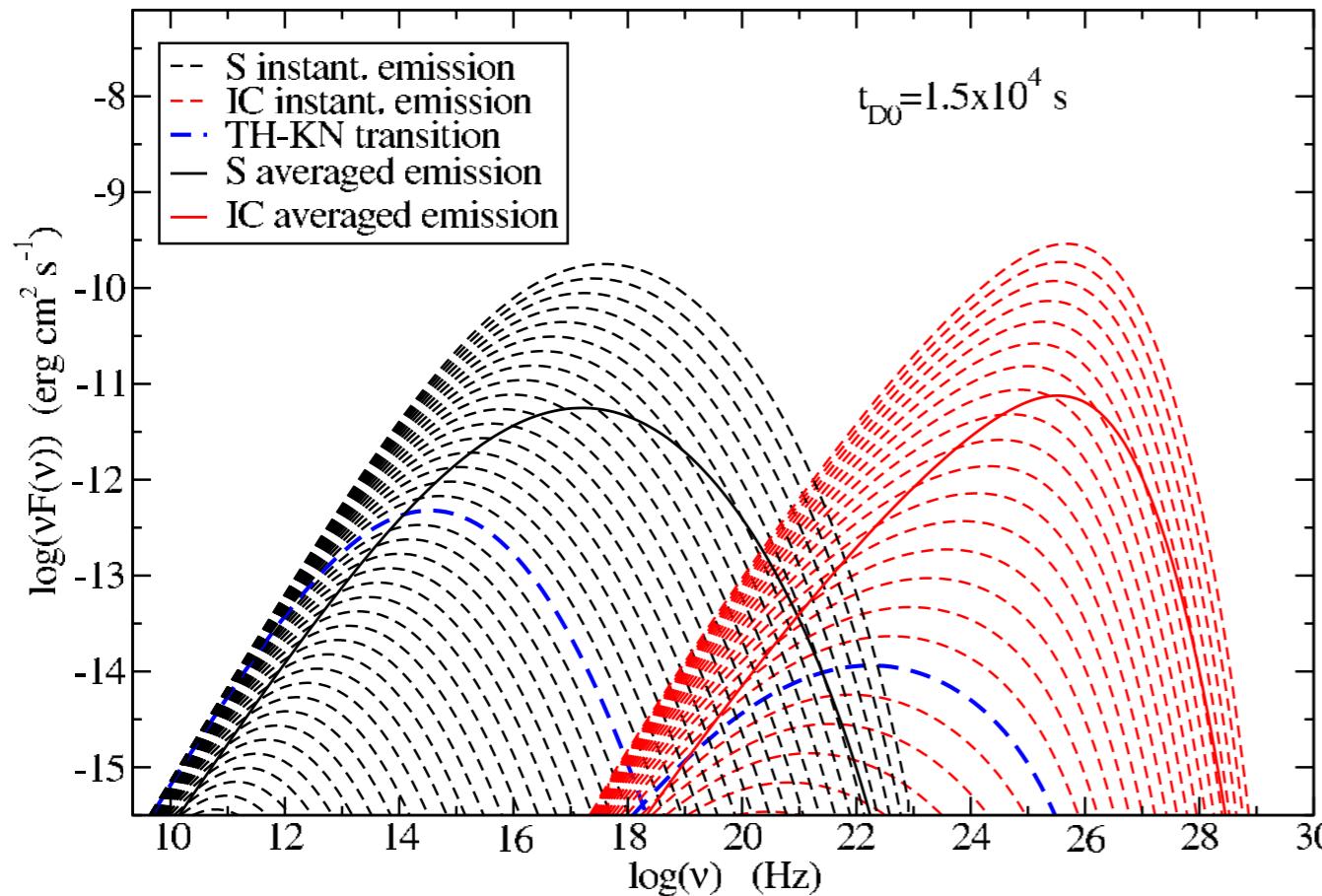
$$E_s \propto \gamma_{3p}^2 B \delta.$$

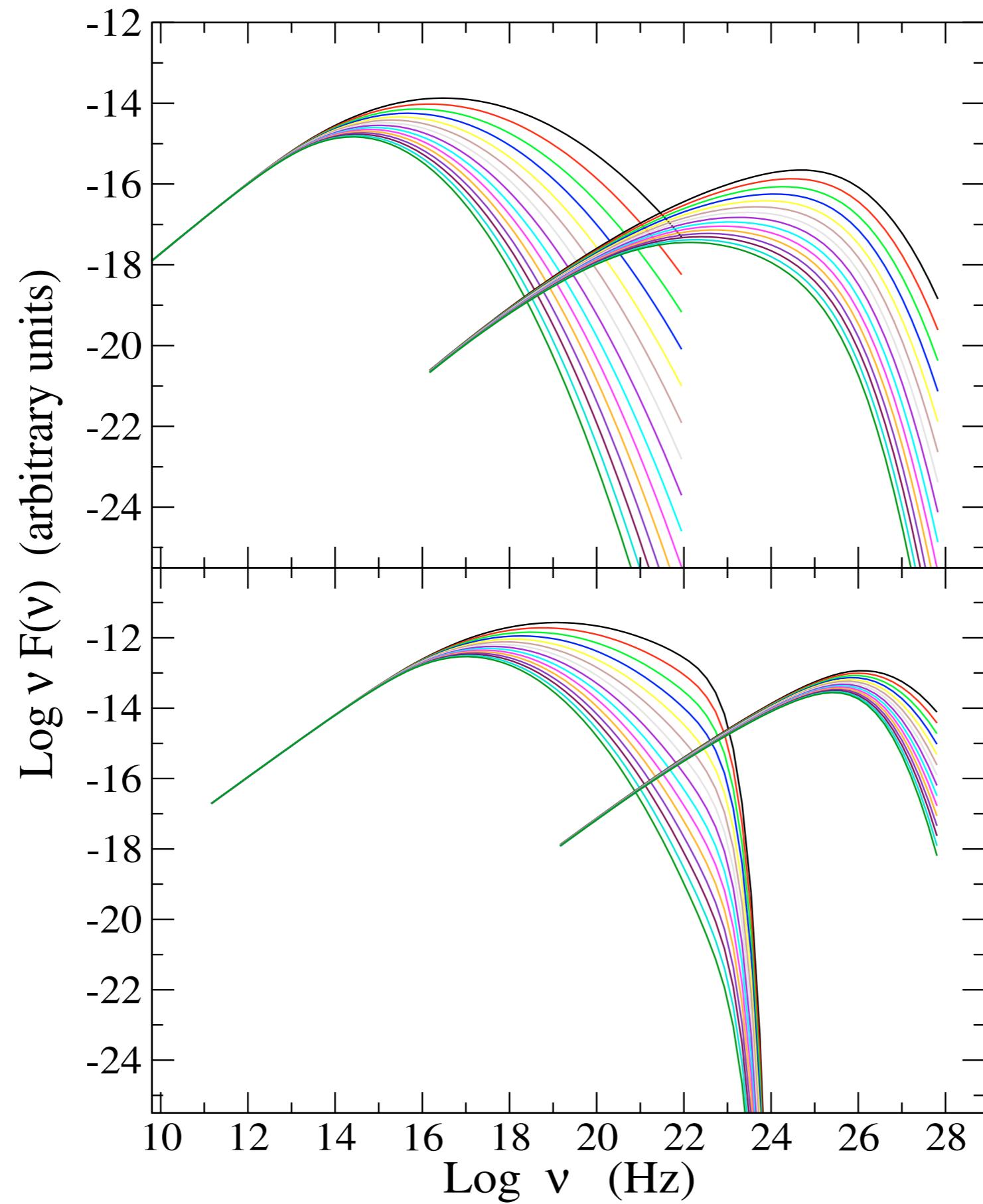
$$S_s \propto (E_s)^\alpha$$



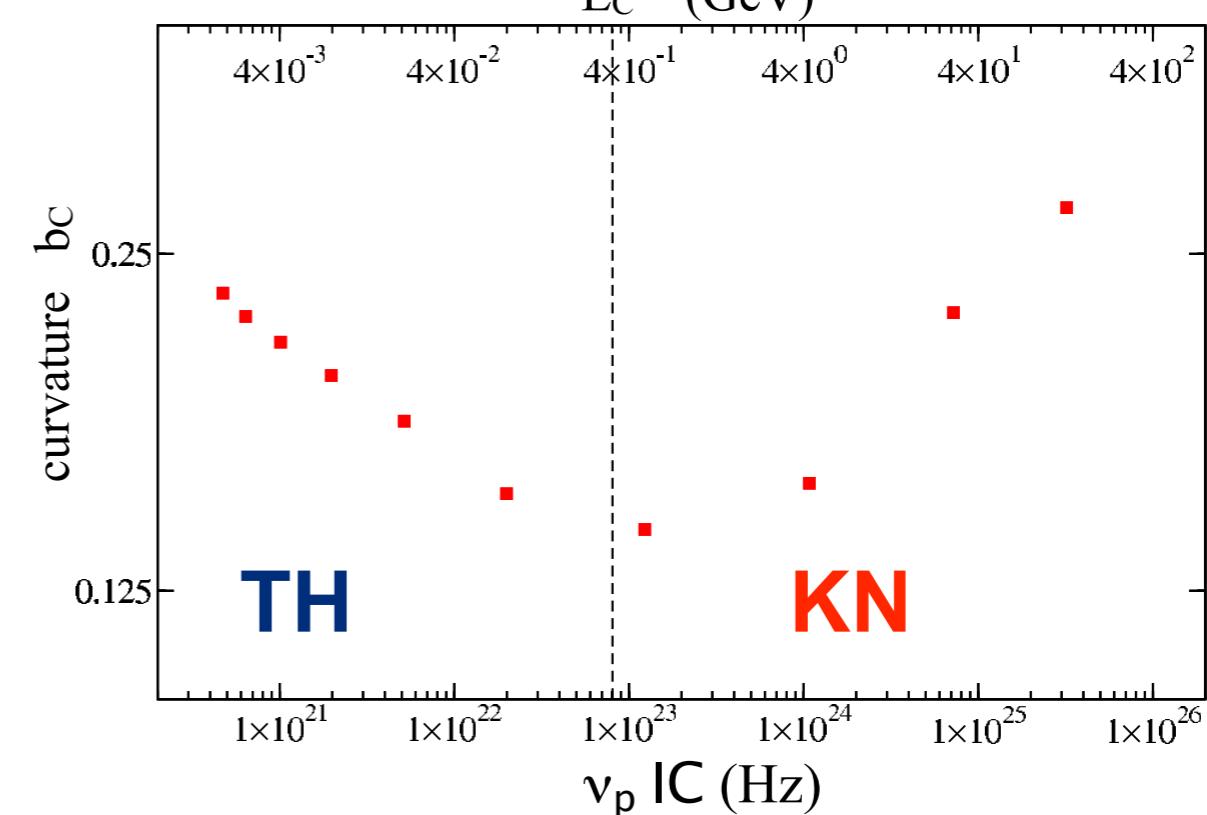
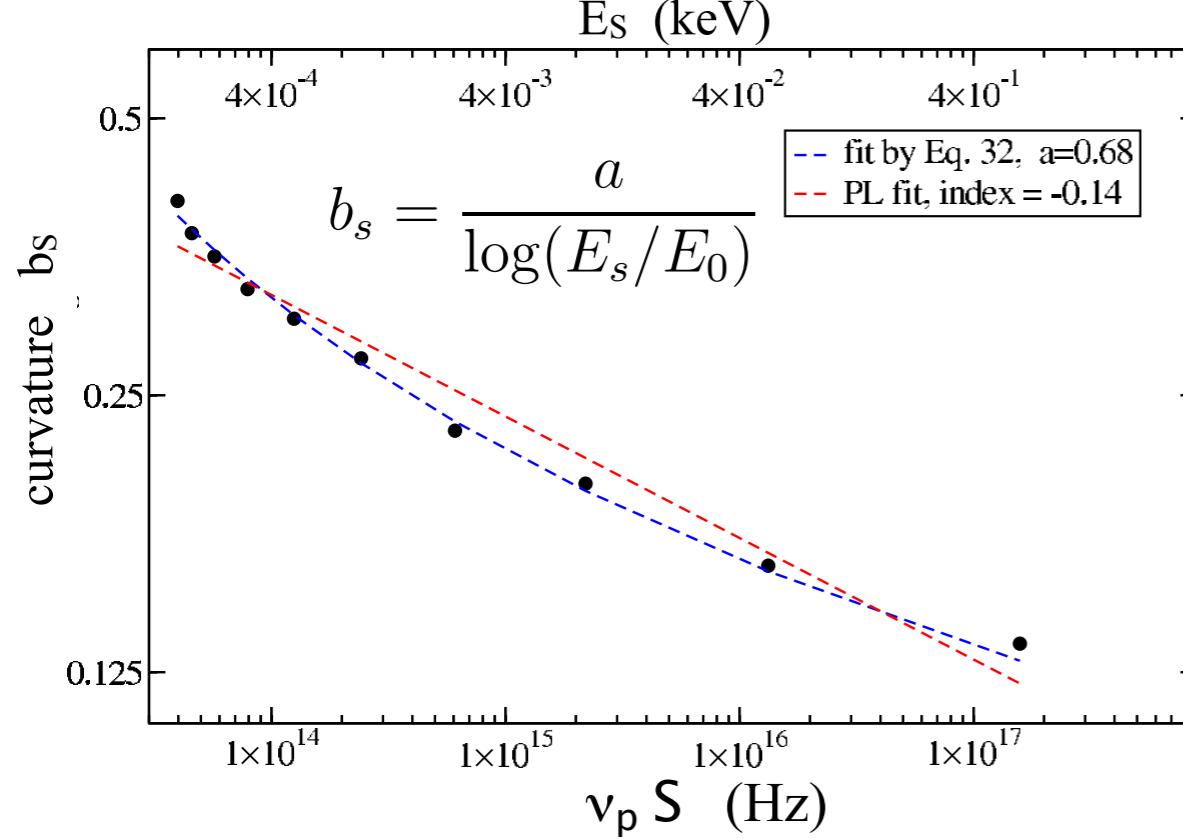
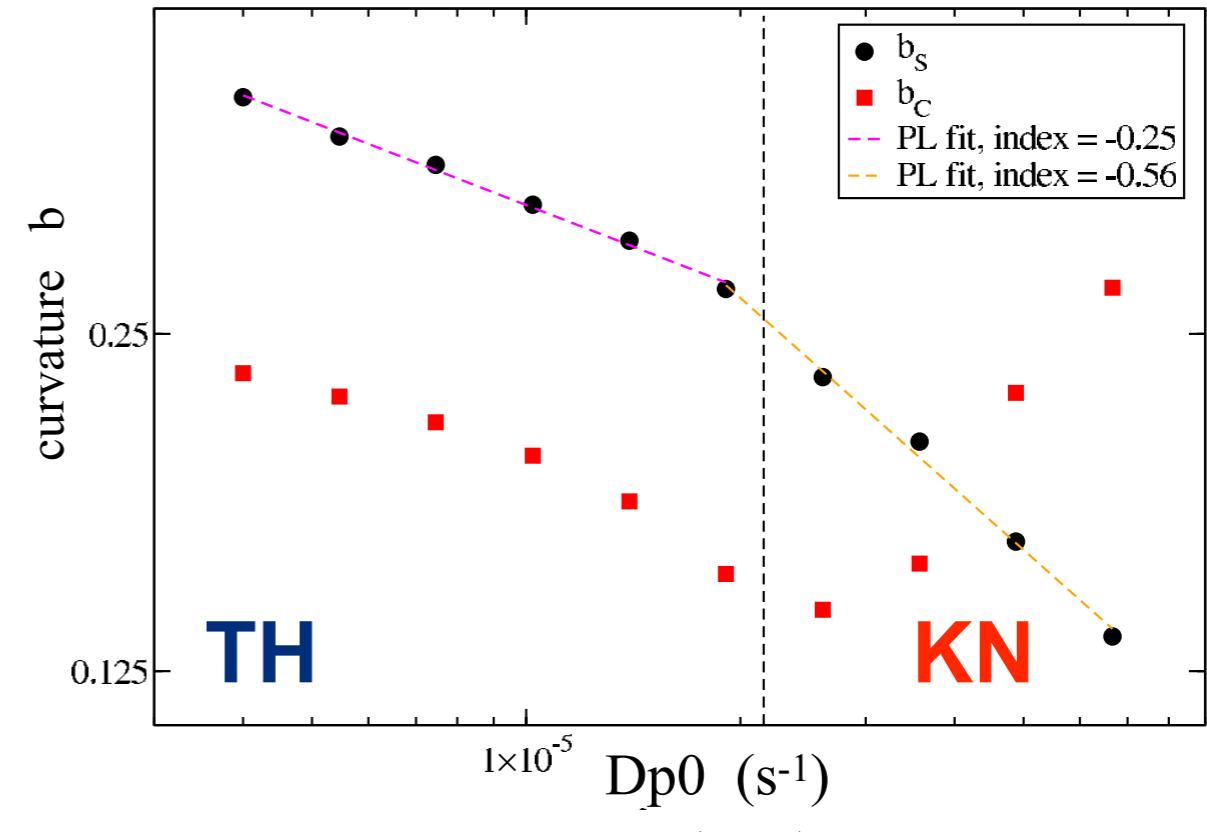
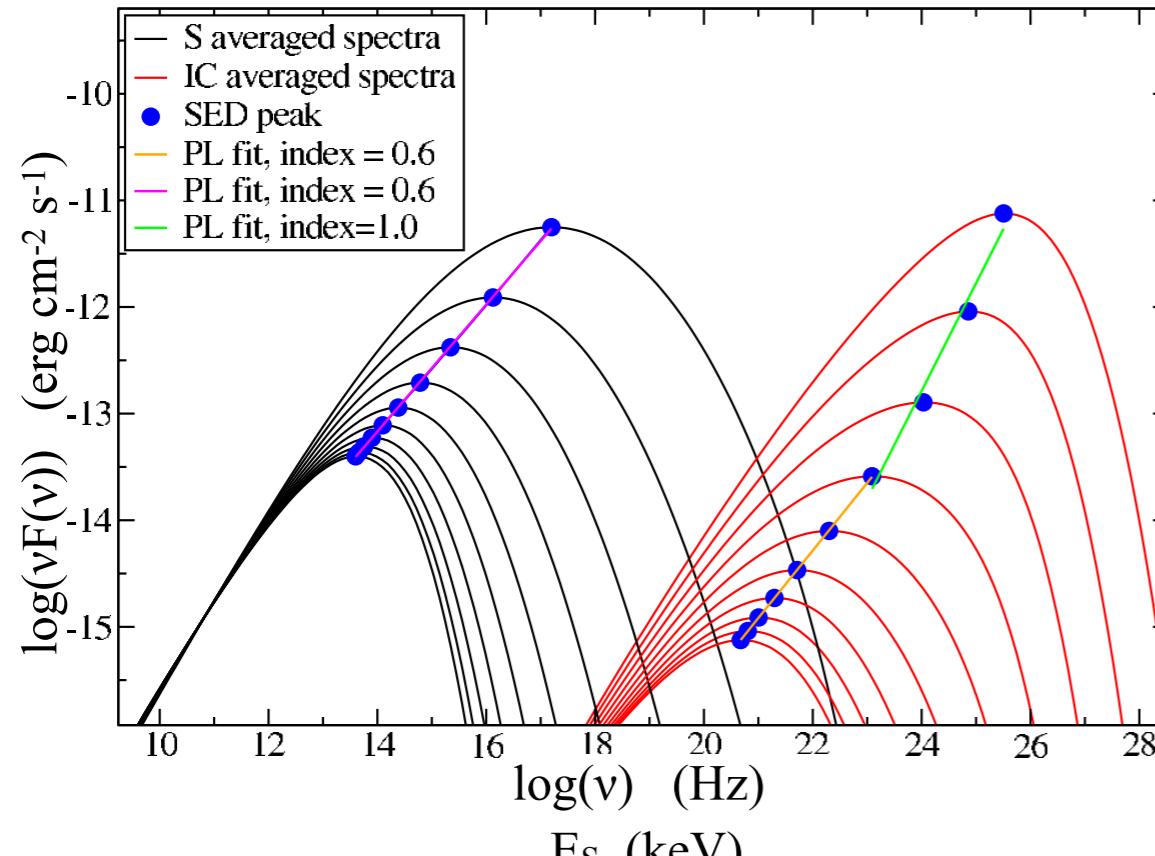
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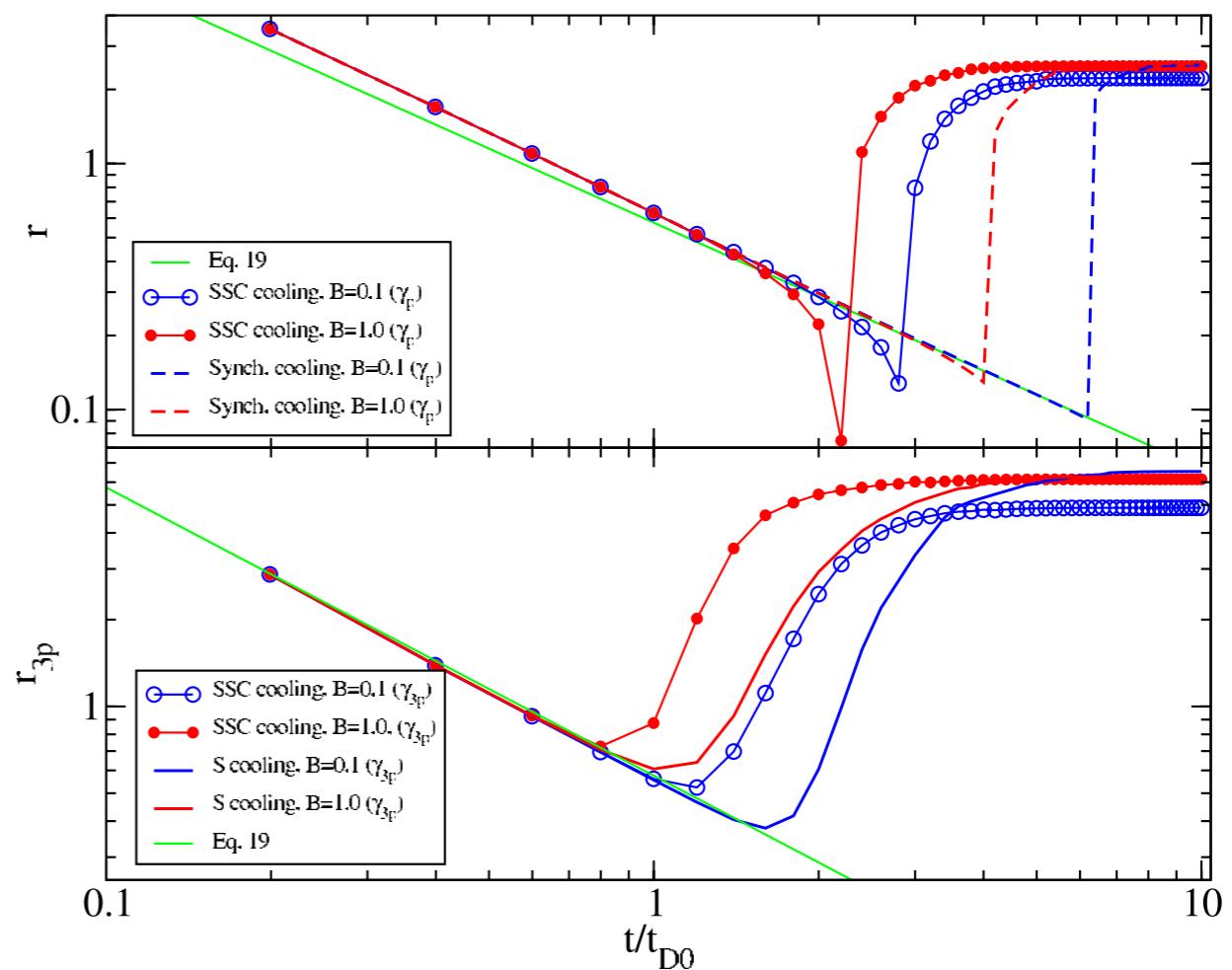
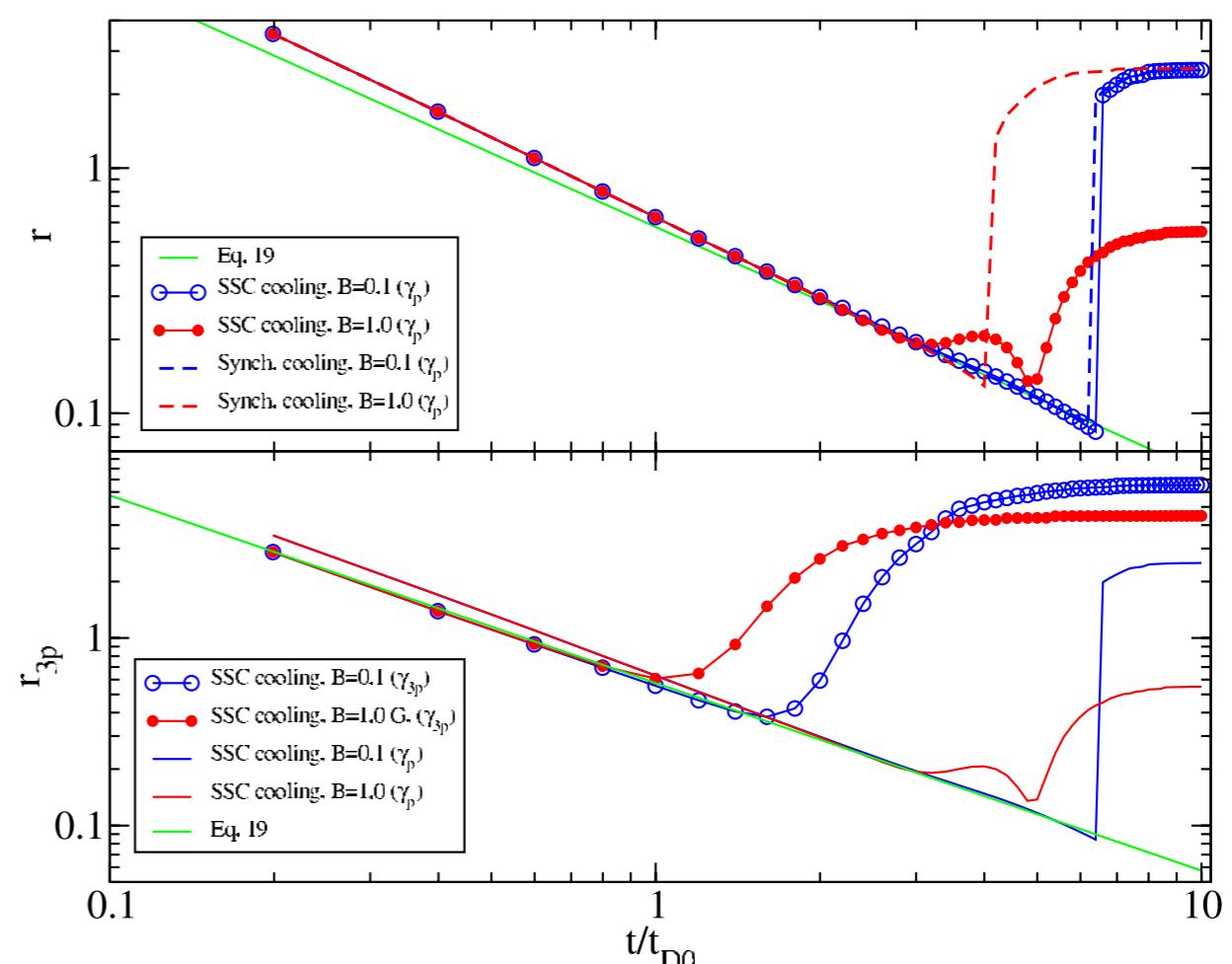
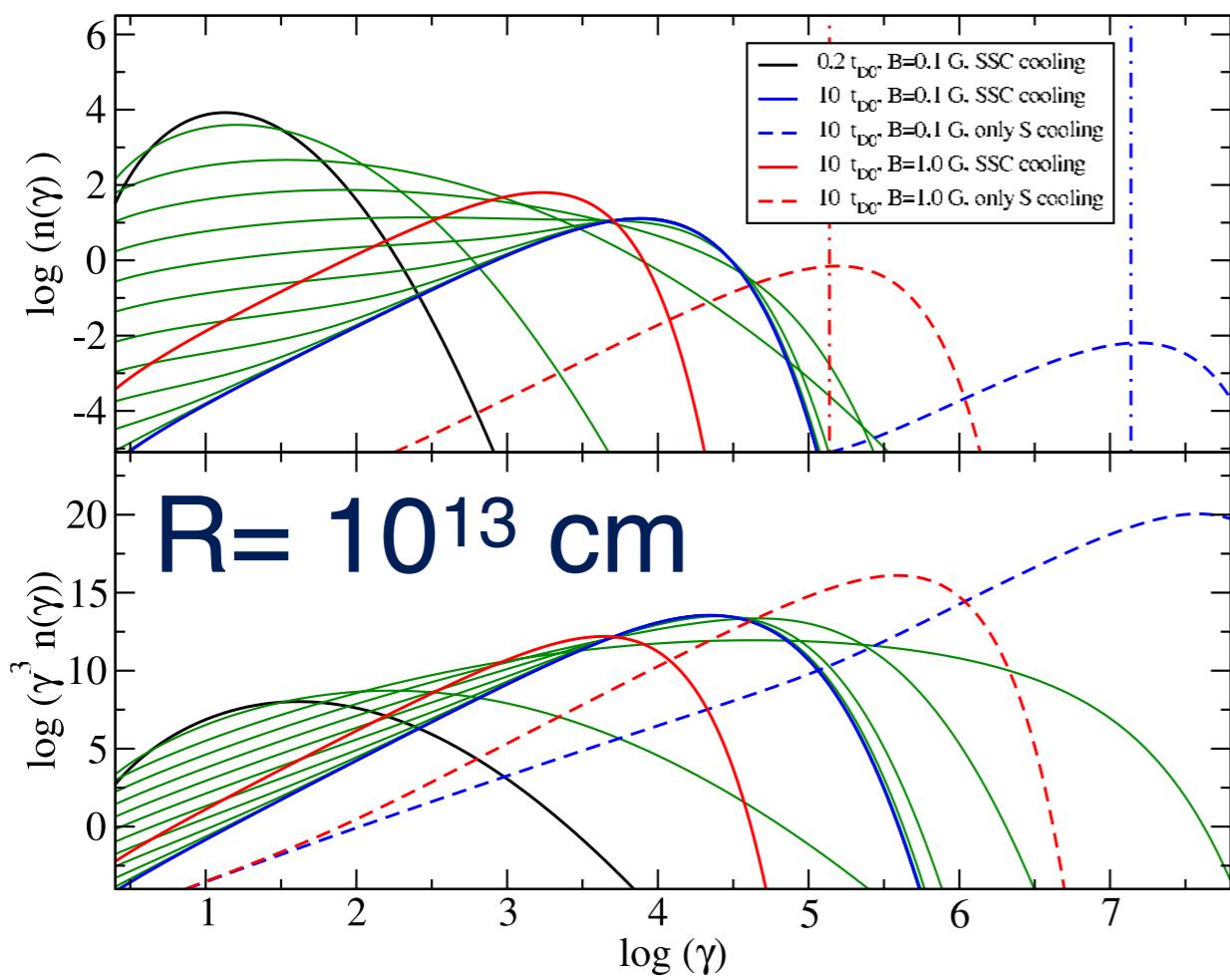
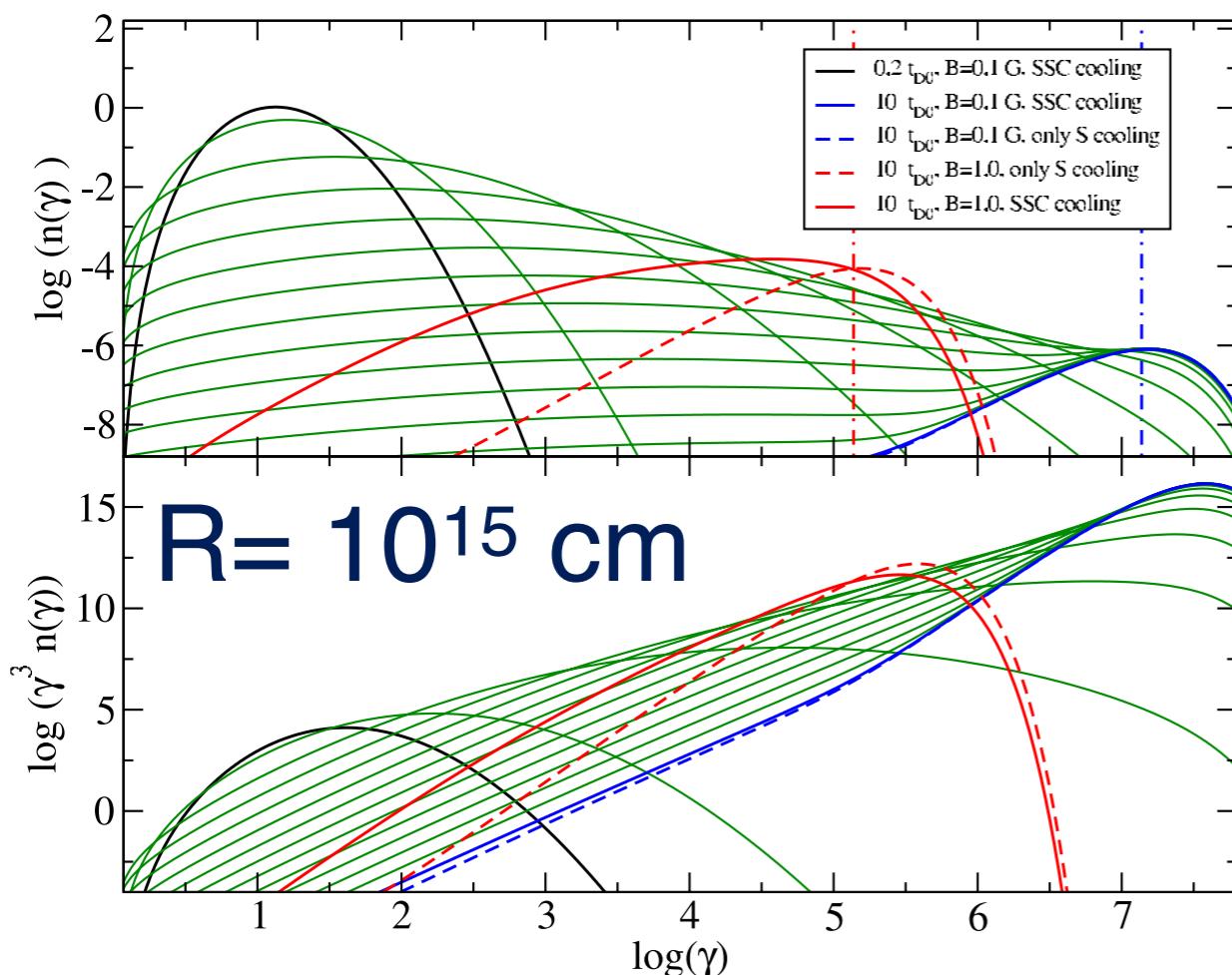
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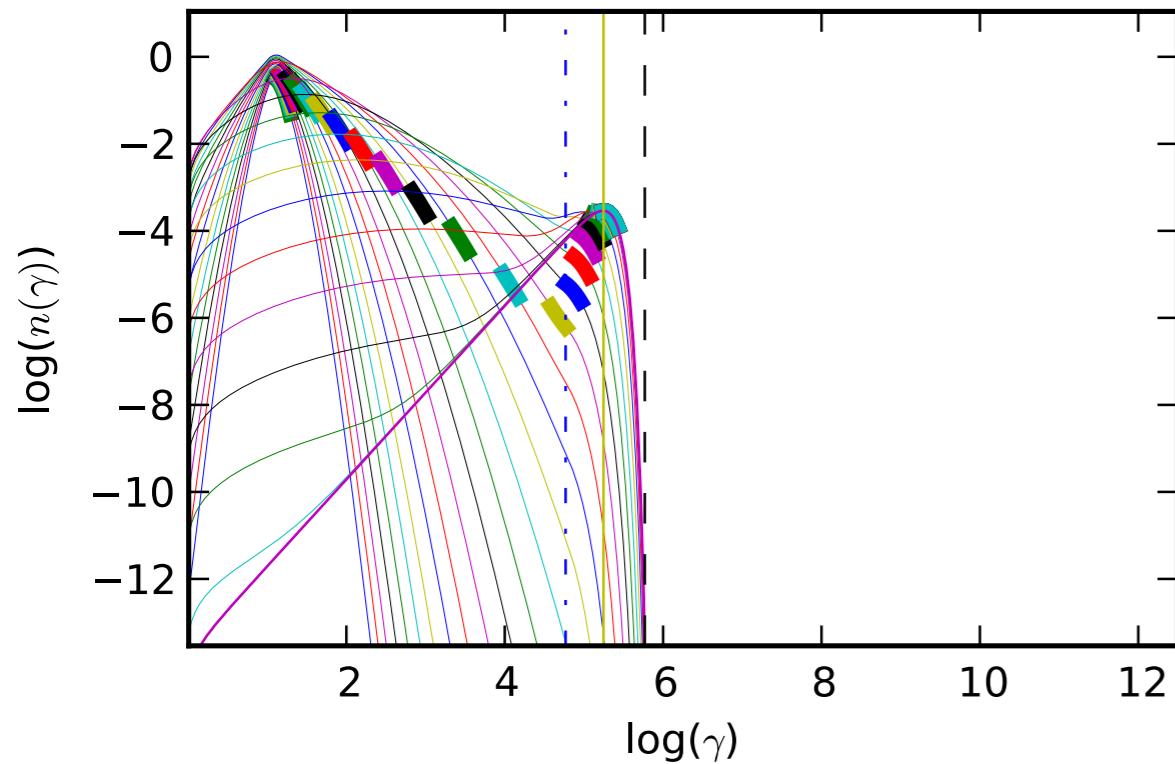
D_p -driven trends $t_D = [1.5 \times 10^4 - 1.5 \times 10^5]$, $L_{\text{inj}} = \text{const.}$



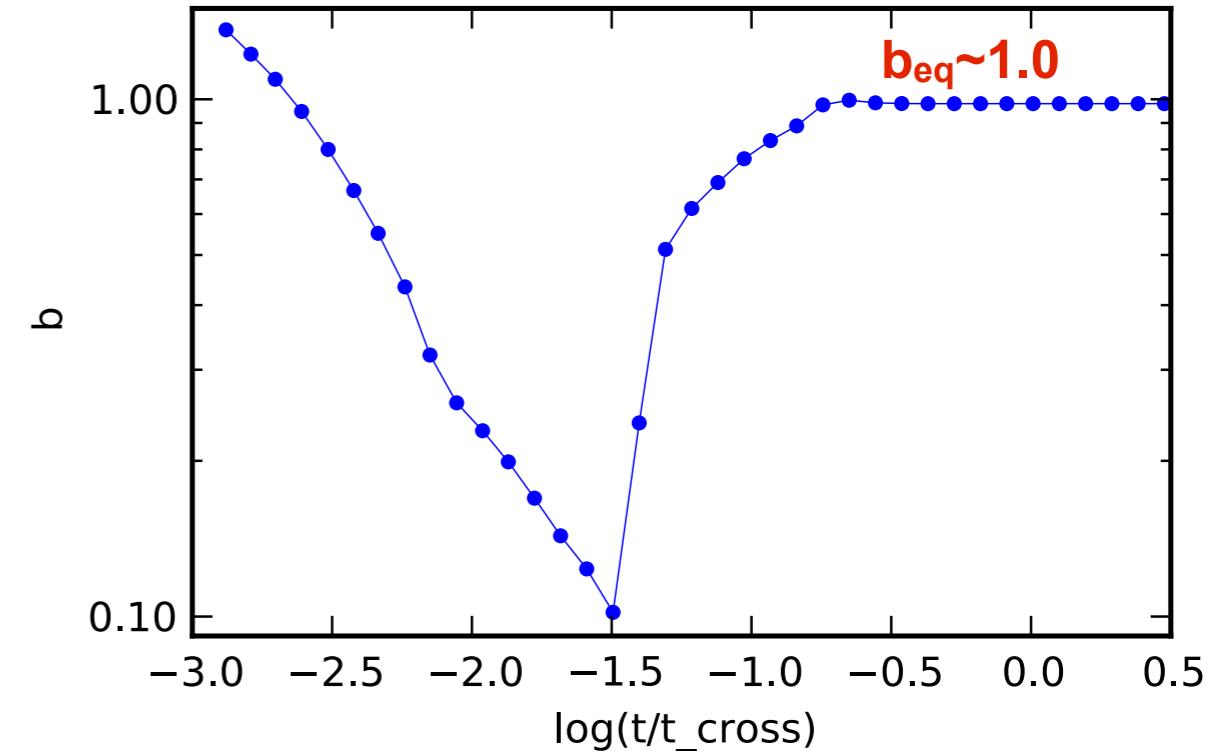


effect of λ_{\max} , λ_{coher}

$B=1.0 \text{ G}$, $t_{D0}=1E3 \text{ s}$, $q=2.0$, $\lambda_{\max}=10^9 \text{ cm}$



synch. peak curvature



$B=1.0 \text{ G}$, $t_{D0}=1E3 \text{ s}$, $q=2.0$, $\lambda_{\max}=10^{15} \text{ cm}$

